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ECONOMIC EFFICIENCY, CAPITAL-INTENSITY AND
CAPITAL-LABOUR SUBSTITUTION IN RETAIL TRADE
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Capital-Laboux Substitution in Retail Trade
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## I. Introduction

The problems of factor proportions, capital-intensity and technological change are quite familiar. Yet, in the measurement of capital-intensity, inclusion of working capital is rarely seen. This is likely to introduce serious biases in the estimates of both capital-intensity and the elasticity of substitution between capital and labour. The situation is likely to become worse in the case of distributive trades where the importance of fixed capital alone is rather limited.

One of the purposes of the present paper is to examine the economic position of retail tradesby taking account of the requirements of working capital (or inventory stocks). The choice of retail trades is guided by various reasons. First, it is felt that this category of services is a suitable example of non-material production. Second, it is often assumed that the small retail shops are highly labour-intensive. It would be interesting to explore whether this hypothesis remains valid if one considers inventory-sales ratios as a measure of capital-intensity. Justification for the use of inventory-sales ratio or inventory-labour ratio lies in the fact that the conventional indicators such as per capita availability of horsepower or "tons of steel" or value of equipment used for material
production are not very relevant. Besides, the stocks reflect more accurately the annual flow of capital services than the fixed capital in the measurement of relationship between output and capital input. Finally, the variations in size of inventory-sales ratios may also throw light on the relative economic efficiency of small and large establishments in retailing.

The degree of capital-intensity depends on the elasticity of substitution between capital and labour. A priori, one might expect that this elasticity is low in non-material production where by and large, labour is the end-product and quality of services is judged in terms of the amount of 1abour. The empirical observation of a rise in the share of labour in retail trades, and also in other services, without a corresponding rise in the share of output also suggests a low elasticity of substitution. However, contrary to expectations, the authors of the CES production function (Arrow et al.) obtained rather high estimates of this elasticity for trade (1.12) and transport services (1.74) ${ }^{1}$ from the data for Japan and the USA.

We shall explore whether retail trades indicate a high or low elasticity and whether the high estimates obtained by Arrow et al. are in fact, due to the exclusion of working capital. The CES estimated aggregate elasticity is for the trade sector as a whole. One may also expect that the large-scale department stores have a greater elasticity (due to easier credit facilities and capital accessibility) than the small-scale stores. If the former predominate in the sample, the elasticity estimate may turn out to be high. Besides, the CES production function may not be as applicable to individual service industries as to manufacturing which is perhaps the only sector that

[^1]has so far been considered for testing the CES function. ${ }^{1}$ This function has been hailed as one of the most 'generalised' versions of a production function since it can be easily extended to an n-factor case à la Uzawa. At least, empirically, there can be another interpretation of its generality; viz. that the derivation of the elasticity of subscitution via the indirect behaviourial equation(regressing labour productivity on the wage-rate) or the direct method is equally valid for all economic sectors. A test is made of the indirect behaviourial equation with the aid of cross-country data of six retail industry groups to determine whether this assumption and interpretation of generality holds. The behaviourial equation measures the elasticity of substítution under restrictive assumptions of constant returns to scale and perfect competition in factor and product markets. The empirical validity of these assumpions for retail industries is also examined. For the measurement of elasticity of substitution directly, ${ }^{2}$ we employ a three-level Uzawa version of a four-factor CES function. Assuming separability of components of varjables, fixed and working capital are considered separate inputs, as are wage-labour and own-account labour.

[^2]
## II. Indices of Capital-Intensity and Economic Efficiency

In economic literature, capital-labour as well as capital-output ratio have been frequently used as indicators of capital-intensity. Assuming that fixed capital is relatively insignificant in retailing, stock-sales ratio ${ }^{1}$ becomes analogous to the capital-output ratio ( $K / O$ ) and inventorylabour ratio to the capital-1abour (K/L) ratio. The fixed capital stock measures only a static relationship in an average capital-output ratio. On the other hand, inventory measures the flow of capital services and thus has a better economic meaning as a numerator in the capital-output or capitallabour ratio. In the following pages, we consider both inventory-labour and inventory-sales ratios as indices of capital-intensity.

A few limitations in the use of inventory-sales ratio as an index of capital-intensity are worth noting however. First, the stock-sales ratio, strictly speaking, is not the inverse of stock investment turnover, because the element of gross profit is included in each increment of stock investment. Neither is it identical to the rate of turnover of working capital which may also be affected by the promptness with which the customers settle their accounts. ${ }^{2}$ Second, we have assumed that all stocks held by
$1_{\text {In }}$ general, the stock-sales ratio presents a relationship between stocks at a given point of time and sales during a given period. However, we consider the ratio as a ratio of the average stocks over the year (average of the beginning-of-the-year and end-of-the-year stocks) to the sales for that year. Some witters have argued that the stock-sales ratio based on the beginning-of-the-year stocks is more valuabie since the size of the stocks held depended on the amount of sales the businessmen expected to make in future, End-of-the-year ratio is less reliable for setting ideal stocks during periods when sales are declining or increasing at below normal rates. See Carl M. Schmalz, Indexes of the Stock-Sales Relationship in Retail Stores, Harvard Business Review, Vol. 6, 1928, pp. 433-442.
${ }^{2}$ Cf. M. P. McNair, Significance of Stock-turn in Retail and Wholesale Merchandising, Harvard Business Review, Vol, I, 1922-23, pp. 87-96.
retailers represent "productive" investment. In underdeveloped countries, this need not necessarily be true. Apart from technical requirements, the size of inventory stocks may also be influenced by the nature of economic organisation. In retailing, for instance, household and the bulk of family labour provides the basis for economic operations. Working capital requirements in terms of final consumer goods may be reduced to some extent since the remuneration to additional self-employed labour does not accrue until the fruits of labour materialize. ${ }^{1}$ A fall in the family-based retailing may partly explain a rise in the working capital requirements since larger stocks held by traders reflect both "investment" and "consumption".

Despite the above limitations, under conditions of capital scarcity (that is almost proverbial in the LDCs), inventcry-sales ratio can be an appropriate index of dynamic economic efficiency. The lower the inventorysales ratio, for instance, the shorter the average length of time for which the retail stores have to hold their stocks. This would imply a reduction of costs and rise in profits when the reorder costs of more frequent purchases is less than the carrying costs, Although a low inventory-sales ratio need not be a cause of high economic efficiency, the latter being a function also of such factors as ability and foresight of good management, it does at least reflect economies of scale and superior management.

There is, as yet, no unanimous view regarding the optimum level of stocks in relation to sales. One can at best cite a number of prevailing

[^3]hypotheses, viz:
(a) Businessmen maintain a constant proportion of sales in stocks;
(b) Rational entrepreneur should vary his inventory stocks with the square root of sales rather than with sales; ...
(c) According to Boulding, "the optimum inventory is not independent of the amount of capital with which the firm starts. The more capital a firm has, the larger will be its inventory."1 Although Boulding does not provide any explanations for this relationship, it may be that the greater the capital the firm has, the more it pays to invest it in inventory stocks especially under conditions of expectations of price rises. This would be true if the returns to capital were greater in the larger firms than the smaller ones.

## III. Some Evidence of Inventory-Sales Ratios, Economies of Scale and Market Imperfections

In general, the diseconomies of small-scale would suggest higher ratio of stock to sales for smaller shops than those for larger shops. This hypothesis of an inverse correlation is borne out by the position of seven retail industry groups of Colombia (1954) as illustrated by the following graphs. On the vertical axis, we plot the inventory-sales ratios whereas the horizontal axis measures the size of stores in the ascending order of
${ }^{1}$ Kenneth Boulding: A Reconstruction of Economics, 1950, p. 113. This situation obtains when the indifference curves facing a firm are not parallel but circular. If the curves are parallel, i.e. they are separated by a constant vertical distance so that slopes of all curves are constant, then for any given amount of inventory, the inventory does not change with the change in capital since the whole profit is added to the liquid stock of the firm.

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the value of sales. :There are nine size-classes. In four cases out of seven, viz. general merchandise, textiles and clothing, automobiles and accessories, and hardware and construction materials, as the size of stones increases, the inventory-sales ratio $\left(K_{i} / S\right)$ continues to fall until it reaches the lowest level in the largest stores. In the case of food and beverages, the ratio declines until it reaches the lowest level in the medium-sized stores and then rises sharply again. For fuels, the size of stores seems to bear little influence on the magnitude of the ratio which is fairly stable across different size-classes. For furniture and domestic appliances, the medium-scale as well as large-scale stores indicate ratios which are almost as large as those for the small-scale stores. In general, the beginning-of-the-year inventory and end-of-the-year inventory move parallel to the average inventory for the whole year. Thus, the fact that the end-of-the-year stocks are more closely related to the last year's sales rather than those of the coming year does not seem to make any significant difference.

The above observations seem to contradict a number of commonly held hypotheses, viz. (a) that the inventory-sales ratios for the small stores would tend to be low since they often buy in small bulk and more frequently in order to lower carrying costs; (b) that the ratio will tend to be low for such perishable products as food, fruits and vegetables and high for durables like ornaments, watches and automobiles typical of erratic demand resulting from the caprice of consumers; and (c) the poor 1iquid and credit position of the small businessmen forces them to lower stock-sales ratio in order to save on carrying and storage costs. We notice that at least in
the Colombian case, even the stocks held by small retailers in food and beverages which would generally qualify as perishables, are quite large in relation to sales. Thus, even though there are savings in carrying costs, the more frequent the ordering of merchandise the greater are the reorder costs of delivery. If the sellers charge a higher price for smaller orders and a lower price for larger orders, the reorder costs will be still higher for the small shops.

It is also interesting to note that inventory labour ratio ( $\mathrm{K}_{\mathrm{i}} / \mathrm{L}$ ) and inventory-sales ratio ( $K_{i} / S$ ) both decline with an increase in the sales-size of the firms; ${ }^{1}$ sales labour productivity rises and so does the wage per employee (see Table I, Appendix I). This implies that the largex 'shops' make more economical use of both labour and capital resources than the smaller shops. However, this observation is inconsistent with the traditional neo-classical theory of production according to which, given constant returns to scale, all firms irrespective of their size, are on the same production function. Therefore, theoretically, an increase in capitallabour ratio should be associated with an increase in capital-output ratio, and an increase in output-labour ratio. This inconsistency between received theory and empirical facts of the retail trades can be reconcilled'by assuming increasing returns to scale and superior management in the large shops. ${ }^{2}$
$1_{\text {Ranking }}$ of shops according to size may vary depending on the criteria of 'scale' used. The two most popular criteria are the number of persons engaged and the volume of sales. Our choice of the latter is governed partly by the availability of data in this form, and partly for its greater economic significance in measuring the efficiency and economies arising from increase in sales.
${ }^{2}$ There is plenty of empirical evidence for the manufacturing sector that suggests a positive correlation between capital productivity and labour productivity. See J. C. Sandesara, Scale and Technology in Indian Industry, Bulletin of the Oxford University Institute of Economics and Statistics, August 1966; and M. Shinohara and D. Fisher, The Role of Small Industry in the Process of Economic Growth, The Hague, 1968.

It may seem that in retail distribution, the economies of scale are insignificant since the size of stores in general is quite small and the growth of total sales merely reflects the growth of commodity production. Yet, in practice the situation in retailing need not be any different from what prevails in manufacturing establishments. Large retail stores, e.g. supermarkets and chain stores, can use advanced techniques of distribution more economically at higher volume of sales. Similarly, expansion of sales enables fuller utilisation of existing equipment and staff. ${ }^{1}$

In order to verify the existence of economies of scale in the seven sub-groups of retail industries of Colombia, we fitted the following logarithmic equations:

$$
\begin{align*}
& \log \left(S / L_{p}\right)=\alpha_{0}+\beta_{0} \log (S)+\Sigma_{0}  \tag{1.a}\\
& \log \left(S / L_{e}\right)=\alpha_{1}+\beta_{1} \log (S)+\Sigma_{1}  \tag{1.b}\\
& \log \left(S / L_{e}\right)=\alpha_{2}+\beta_{2} \log (S)+\gamma_{2} \log \left(H_{e}\right)+\Sigma_{2} \tag{1.c}
\end{align*}
$$

where $S / L_{p}$ - is sales per person engaged, $S / L_{e}$ - sales per employee, $S$ total sales, and $W_{e}$ - wage per employee. The $\beta$-coefficient in these equations gives what is well-known as the "Verdoorn coefficient." ${ }^{2}$ This coefficient roughly indicates the size of economies of scale on the assumption that the productivity increase in response to expansions in total output

[^4]is explained by these economies. Inclusion of ( $W_{e}$ ) as an additional independent variable was made in order to examine any biases in the $\beta$-coefficient due to the omission of other explanatory variables. The results of these regressions are presented in Table I. In almost all cases, equation (1.c) with ( $W_{e}$ ) as one of the variables provides the best fit. The correlation between sales ${ }^{1}$ and sales per employee is positive and statistically significant for general merchandise, furniture and domestic applicances, automobiles and hardware and construction materials. Of these industry groups, it is significant to note that general merchandise, automobiles and hardware and construction materials also showed a decline in the inventorysales ratios with a rise in the scale of shops. One can therefore conclude that at least in these cases, the decline in the ratio can be attributed to economies of scale.

At present, there is however no satisfactory method of separating economies of scale from imperfections in the product market which are typical of retail trades. The identical articles often sell at very different prices in the same neighborhood. Small-sized shops are protected from the competition from large shops by the "loyalty of their clientele." Competition is imperfect and tends to operate not so much through a reduction of prices or distributive margins as through the multiplication of shops and elimination of abnormal profits.
$1_{\text {The }}$ limitations of sales as an indicator of output need to be borne in mind. For instance, sales do not respond to a change in size of transactions or to a deepening of operations (e.g. greater performance of service per week).
$\xrightarrow[\text { Colombia: } \frac{\text { Table I }}{\text { Retail }} \text { Industries }]{\text { "Verdoorn Coefficients" }}$

| Industry and <br> Dependent Variables | $\alpha$ | $\beta$ | $\mathbf{R}^{2}$$\mathrm{N}=$ Number <br> of obser- <br> vations |
| :---: | :---: | :---: | :---: |

I. Food \& Beverages

| $\log \left(S / L_{e}\right)$ | 6.534 | -0.335 |  | 0.489 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\log \left(S / L_{e}\right)$ | 5.956 | $(0.129)$ |  |  |  |
| $\log \left(S / L_{p}\right)$ | 7.437 | $(0.234$ | +0.234 | 0.595 | 9 |
|  |  | $(0.797)$ | $(0.186)$ |  | 0.193 |

II. General Merchandise

| $\log \left(S / L_{e}\right)$ | 4.384 | -.0 .118 |  | 0.137 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | $(0.112)$ |  |  |  |
| $\log \left(S / L_{e}\right)$ | 3.372 | 0.230 | -0.580 | 0.648 | 9 |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{p}}\right)$ |  | $(0.141)$ | $(0.196)$ |  |  |
|  | -1.240 | 1.151 |  | 0.775 | 9 |

III. Textiles \& Clothing

| $\log \left(S / L_{e}\right)$ | 4.150 | -0.0008 |  | 0.000 | 9 |
| :--- | :--- | :---: | :--- | :--- | :--- |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{e}}\right)$ | 4.176 | $(0.210)$ | 0.181 | 0.833 | 0.866 |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{p}}\right)$ |  | $(0.088)$ | $(0.133)$ |  | 9 |
|  | 0.672 | 0.629 |  | 0.407 | 9 |

IV. Furniture and

Domestic Appliances

| $\log \left(S / L_{e}\right)$ | 2.735 | 0.289 |  | 0.832 | 9 |
| :--- | :--- | :---: | :--- | :--- | :--- |
| $\log \left(S / L_{e}\right)$ | 2.774 | $(0.049)$ | 0.257 | $0.059 *$ | 0.834 |
| $\log \left(S / L_{p}\right)$ | 5.73 | $(0.1 .32)$ | $(0.223)$ |  | 9 |
|  |  | 0.862 |  | 0.970 | 9 |

V. Fuels

| $\log \left(S / L_{e}\right)$ | 3.122 | 0.216 |  | 0.219 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{e}}\right)$ | 3.664 | $(0.154)$ | $0.193 * \%$ | 0.863 | 0.780 |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{p}}\right)$ |  | $(0.137)$ | $(0.220)$ |  | 9 |
|  | 0.875 | 0.967 |  | 0.582 | 9 |

Table I, continued

| Industry and <br> Dependent Variables | $\alpha$ | $\beta$ | $\overline{\mathrm{R}}^{2}$$\mathrm{N}=$ Number <br> of Obser- <br> vations |
| :---: | :---: | :---: | :---: | :---: |

VI. Automobiles

| $\log \left(\mathrm{S} / \mathrm{L}_{\mathrm{e}}\right)$ | 2.763 | 0.422 |  | 0.964 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\log \left(\mathrm{~S} / \mathrm{L}_{\mathrm{e}}\right)$ |  | $(0.030)$ |  |  |  |
| $\log \left(\mathrm{S} / \mathrm{L}_{\mathrm{p}}\right)$ | 2.795 | 0.454 | $-0.098 *$ | 0.965 | 9 |
|  |  | 1.867 | $(0.087)$ | $(0.249)$ |  |
|  |  | 0.639 |  | 0.982 | 9 |

VII. Hardware

| $\log \left(S / L_{e}\right)$ | 3.628 | $0.329 * \%$ |  | 0.227 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\log \left(S / L_{e}\right)$ | 2.886 | $(0.229)$ | 0.918 | 0.963 | 9 |
| $\log \left(S / L_{p}\right)$ |  | 0.129 | $(0.057)$ | $(0.084)$ |  |
|  | 1.886 | 0.913 |  | 0.628 | 9 |

*     - not significant at $5 \%$ level of confidence. ** - significant at $10 \%$ level of confidence.
N.B. Figures in parentheses represent standard errors.

Factor markets in retaj. 1 trade appear to be no less imperfect. Shops of different sizes pay different wage-rates to the hired employees. In all the Colombian retail trades considered, the wage-rate rises continually with the size of shops. With the exception of general merchandise, these wage-differentials by size of shops are positively correlated with the sales per employee (see Table I, Appendix I). Besides, although information on returns to capital is not available, a strong possibility of differential accessibility to capital and finance would suggest that the price of capital is relatively low for large stores, ${ }^{l}$ which show larger size of owned capital.

## IV. Capital-Labour Substitution

In order to estimate the elasticity of substitution between capital and labour in retail trades, we assume the CES production function of the following form:

$$
\begin{equation*}
V=\left(\beta K^{-\rho}+\alpha L^{-\rho}\right)^{-1 / \rho} \tag{2.a}
\end{equation*}
$$

where $V$ is value added, $K$ - capital and $L$ - labour; and the elasticity of substitution $\sigma=\left(\frac{1}{1+\rho}\right)$. Arrow et al., the authors of this CES function provided its empirical basis with the following behaviourial equation which they tested with the cross-country data on manufacturing:

$$
\begin{equation*}
\log \left(\frac{V}{L}\right)_{i}=\log A_{i} \div b \log W_{i}+\Sigma \tag{2.b}
\end{equation*}
$$

where $\frac{V}{L}$ - is value added per unit of labour, $W$ - wage-rate per man-year,
$l_{\text {For }}$ the purpose of illustration, it may be worth noting that in Japan in 1958, small enterprises with a capitalization of $¥ 5$ million and less were charged an average intercst rate of 17 per cent, whereas the large enterprises with a capitalization of 100 million and over borrowed at a relatively low average interest rate of 11 per cent. See Kenichi Miyazawa, The Dual Structure of the Japanese Economy and Its Growth Pattern, The Developing Economies, June 1964 ,

A - constant term and subscript $i$ denotes individual industries. Given the assumptions of perfect competition in product and factor markets and constant returns to scale, it was shown that the relationship (2.b) was independent of the capital stock and that b-coefficient measured the Hicksian elasticity of substitution. However, for lack of data on capital stock the authors of the CES did not test the following equation:

$$
\begin{equation*}
\log \left(\frac{V}{L}\right)_{i}=\log A_{i}+b \log (W)_{i}+c \log \left(\frac{K}{L}\right)+\Sigma \tag{2,c}
\end{equation*}
$$

where $\frac{K}{L}$ is capital-labour ratio, and its coefficient $c$ is assumed to be equal to zero, and $b>0$ measures elasticity of substitution. We estimated equations (2.b) and (2.c) with the aid of cross-country data for all those LDCs for which comparable information were available. In equation (2.c) we use inventory-labour ratio as a measure of annual flow of capital services. The data for six major groups of retail industries (presented in Appendix II) were converted into U.S. dollars by using official exchange rates. Wherever multiple rates prevailed, the free rate of exchange was used. No allowance was made for changes in the purchasing power of the dollar over the different years of the sample. Unfortunately, data limitations did not permit the use of the same sample size for the two equations. Besides, sales per employee had to be used as an index of labour productivity in the absence of cross-country data suitable for estimation of "gross margin" (i.e. total sales minus cost of goods sold) which serves as a rough measure of value added. We feel however that it is illegitimate to exclude self-employment (e.g.owner-operators and unpaid family labour) which constitutes the bulk of total work-force in retailing. In order to use the concept of "total number of persons engaged," it is necessary to obtain information on labour income from self-employment which could not be found in any of the country
economic censuses reviewed. Resort was made to fit the data of twenty retail industries of Taiwan (1961) to our equations in order to examine whether the use of value added and total number of persons engaged makes any significant difference to the results. The estimates of labour income from self-employment in this case were improvised by assuming that 90 per cent of the owner-disbursements represent labour income. ${ }^{1}$ The results of these regressions are presented in Tables II and IIA below.

The coefficient of determination ( $\overline{\mathrm{R}}^{2}$ ) between the sales per employee ( $S / L_{e}$ ) and average wage and salary per employee ( $W_{e}$ ) is very low with only one exception. Thus, in general the "goodness of fit" of this relation is very poor. The introduction of capital variable in the relationship, improves the goodness of fit in all cases except one. Although the sample size in the two equations is not identical (in view of a small number of observations, it was decided not to sacrifice any information), the results suggest that the three-variable relationship is more significant. Exclusion of capital variable, whose coefficient is significantly different from zero in almost all industries, is likely to give biased estimates of $\beta$ coefficient. However, in this latter relationship, many of the , $\beta$-coefficients become non-significant at $5 \%$ level of confidence. On the other hand, with the two-variable behaviourial equation of the original CES formulation, the relation between sales per employee ( $S / L_{e}$ ) and the wage-rate ( $W_{e}$ ) is significant at any level of confidence, with only one exception.
${ }^{1}$ For a similar assumption, see Victor Fuchs, The Service Economy, 1968, p. 237, Appendix G, and Irving Leveson, "Non-farm Self-employment in the U.S.," unpublished Ph.D. dissertation, Columbia University, 1967, Chapter 4.
A. Inter-Country Cross-Section

Table II
Empirical Test of the CES with Retail Trade Data:
Cross-Country Regressions

|  | Industry | $\alpha$ | $\beta$ | $\gamma$ | $\mathrm{R}^{2}$ | $\mathrm{N}=$ Number of Observations |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A. Estimating Equation |  |  |  |  |  |  |
| $\log \left(\mathrm{S} / \mathrm{L}_{\mathrm{e}}\right)=\alpha+\beta \log \left(\mathrm{W}_{\mathrm{e}}\right)+\Sigma$ |  |  |  |  |  |  |
|  | Food \& Beverages | 6.861 | $\begin{gathered} 0.491 \\ (0.185) \end{gathered}$ |  | 0.303 | 18 |
|  | Textiles \& Clothing | -0.453 | $\begin{gathered} 1.455 \\ (0.028) \end{gathered}$ |  | 0.055 | 17 |
|  | Furniture \& domestic appliances | 7.734 | $\begin{gathered} 0.250 \% \\ (0.176) \end{gathered}$ |  | 0.143 | 14 |
|  | Pharmacies | 6.601 | $\begin{gathered} 0.414 \\ (0.161) \end{gathered}$ |  | 0.320 | 16 |
| 5. | Automobiles \& vehicles | -0.462 | $\begin{gathered} 1.462 \\ (0.021) \end{gathered}$ |  | 0.611 | 18 |
|  | Gas \& fuels | -0.541 | $\begin{gathered} 1.541 \\ (0.023) \end{gathered}$ |  | 0.116 | 16 |
| B. Estimating Equation |  |  |  |  |  |  |
| $\log \left(\mathrm{S} / L_{\mathrm{e}}\right)=\alpha+\beta \log \left(W_{e}\right)+\gamma \log \left(\mathrm{K}_{\mathrm{i}} / L_{\mathrm{e}}\right)+\Sigma$ |  |  |  |  |  |  |
|  | Food \& beverages | 5.478 | $\begin{gathered} 0.015 * \\ (0.261) \end{gathered}$ | $\begin{gathered} 0.585 \\ (0.202) \end{gathered}$ | 0.584 | 14 |
|  | Textiles \& clothing | -0.184 | $\begin{gathered} 0.261 \% \\ (0.195) \end{gathered}$ | $\begin{gathered} 0.922 \\ (0.149) \end{gathered}$ | 0.924 | 13 |
| 3. | Furniture and domestic appliances | 6.198 | $\begin{gathered} -0.214 * \\ (0.116) \end{gathered}$ | $\begin{gathered} 0.531 \\ (0.129) \end{gathered}$ | 0.794 | 9 |
| 4. | Pharmacies | 3.020 | $\begin{gathered} 0.223 * \\ (0.175) \end{gathered}$ | $\begin{gathered} 0.605 \\ (0.174) \end{gathered}$ | 0.740 | 10 |
| 5. | Automobiles \& vehicles | -0.357 | $\begin{gathered} 0.851 \\ (0.248) \end{gathered}$ | $\begin{gathered} 0.505 \\ (0.195) \end{gathered}$ | 0.542 | 14 |
|  | Gas and fuels | -0.549 | $\begin{gathered} 1.207 \\ (0.316) \end{gathered}$ | $\begin{gathered} 0.342 * \\ (0.308) \end{gathered}$ | 0.533 | 12 |

Source: For basic data, see Appencix II. For reasons of non-comparability, certain observations had to be sacrificed.
N.B. Figures in brackets indicate standard errors of the coefficients.

*     - not significant at $5 \%$ level of confidence. All other coefficients are statistically eignificant at this level.
B. Intra-Country Cross-Section

Table II. A
Retail Industries of Taiwan (1961)

|  | Dependent Variable | $\alpha$ | $\beta$ | $\gamma$ | $\mathrm{R}^{2}$ | N |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Sales per employee $\left(\log S / L_{e}\right)$ | 10.000 | $\begin{aligned} & -2.177 \\ & (0.623) \end{aligned}$ |  | 0.403 | 20 |
|  | Sales per empioyee $\left(\log S / L_{e}\right)$ | 11.316 | $\begin{aligned} & -2.351 \\ & (0.593) \end{aligned}$ | $\begin{aligned} & -0.306 \\ & (0.174) \end{aligned}$ | 0.495 | 20 |
|  | Sales per person $\left(\log S / L_{P}\right)$ | 2.250 | $\begin{aligned} & +1.116 \\ & (0.210) \end{aligned}$ |  | 0.609 | 20 |
|  | Sales per person $\left(\log S / L_{p}\right)$ | 1.990 | $\begin{gathered} 1.329 \\ (0.232) \end{gathered}$ | $\begin{aligned} & -0.079 \\ & (0.045) \end{aligned}$ | 0.670 | 20 |
|  | Value added per employee ( $\log \mathrm{V} / \mathrm{L}_{\mathrm{e}}$ ) | 9.498 | $\begin{aligned} & -2.964 \\ & (0.472) \end{aligned}$ |  | 0.685 | 20 |
|  | Value added per employee $\left(\log \mathrm{V} / \mathrm{L}_{\mathrm{e}}\right)$ | 8.496 | $\begin{aligned} & -2.832 \\ & (0.453) \end{aligned}$ | $\begin{aligned} & +0.234 \\ & (0.131) \end{aligned}$ | 0.735 | 20 |
|  | Value added per person ( $\log \mathrm{V} / \mathrm{L}_{\mathrm{p}}$ ) | 1.906 | $\begin{aligned} & +0.214 \% \\ & (0.496) \end{aligned}$ |  | 0.010 | 20 |
|  | Value added per person $\left(\log V / L_{p}\right)$ | 3.147 | $\begin{aligned} & -0.801 \\ & (0.358) \end{aligned}$ | $\begin{aligned} & +0.381 \\ & (0.069) \end{aligned}$ | 0.643 | 20 |

N.B. Figures in parentheses represent standard errors.

*     - not significant at $5 \%$ or $10 \%$ level of significance. All other coefficients are statistically significant at $5 \%$ level.

The intra-country regression estimates in Table IIA further support our contention that the inclusion of capital variable considerably improves the goodness of fit. Also the substitution of "value added" per employee for sales per employee leads to a better fit. However, use of value added per person leads to no gains.

Thus, one can conclude that the basic relation used by Arrow et al. is not independent of capital. Besides, the observations on Colombian retail industries suggest that the key assumptions of constant returns to scale and perfect competition in product and factor markets are also inconsistent with facts. In order to test the economies of scale hypothesis further with the cross-country sample, we relax for the moment, the popular and convenient assumption of constant returns to scale and assume the following Brown-de Cani version ${ }^{1}$ of the CES function:
or $\quad V=\left(K^{\sim \rho}+\frac{C_{L}-\rho}{\beta}\right)^{-v / \rho}$
where $v$ - economies of scale parameter has a value $r f v \frac{\geq}{<} 1$. By assuming competition in factor markets and not necessarily in product market, we consider the following side relation which states that the ratio of the factor prices (i.e. $m / r$ ) is equal to the marginal rate of substitution:

$$
\begin{align*}
\left(\frac{W}{r}\right)=\frac{\alpha^{V} V / \partial L}{\partial V / a K} & =\frac{(1)}{\left(-\frac{\alpha}{\beta}\right)}\left(\frac{K}{L}\right)^{\sigma} \\
& =\left(\frac{\beta}{\alpha}\right)\left(\frac{K}{L}\right)^{\sigma} \tag{2.f}
\end{align*}
$$

From (2.f) values of $\left(\frac{\alpha}{\beta}\right)$ and $\sigma$ were obtained by converting it into loga-

[^5]rithmic form. These values were inserted into (2.e) and a second use of linear least-squares gave us the value of $v$ - the economies of scale parameter. The estimated values of $\sigma, \rho$, and $\nu$, for three of the six industries in the cross-country sample, viz. food and beverages, textiles and clothing and automobiles, are presented in Table III. For the remaining three industries, viz. pharmacies, furniture and domestic appliances, and gas and fue1, the minimum number of observations could not be gathered.

The standard errors of $v$ - alone could not be estimated. The values of $\nu$ - appear to be very large and cannot be treated as anything more than an illustration. No other estimates are available with which these could be compared. On the other hand, the estimates of the elasticity of substitution are quite significant and suggest that the elasticity in retail trades is quite low if account is taken of working capital.

The preceding methods of estimation of the elasticity of substitution have no doubt an appeal of simplicity. Yet, they fail to measure the elasticity of substitution between components of aggregate variables. If this elasticity of substitution is less than infinite, it is more logical to treat components of capital and labour, e. g. fixed and working capital (or inventory stocks) and wage-1abour and self-employed labour as separate factor inputs. Although there may be a tendency for the private employers to increase the use of family labour in response to a rise in wage-costs, this substicution may or may not be limited. Also, there may be qualitative barriers between wage-labour and own-account labour. Intuitively, one might expect that the substitution of wage-labour for selfsupporting labour, at least up to a point, reduces underemployment and raises productivity in services such as retailing. It would therefore be

Table III
Elasticity of Substitution and Econonies of Scale:

interesting to examine the elasticity of substitution between these two categories, not only as a theoretical exercise but also as a useful guideline in the determination of employment policy. In view of differences in durability and response to economic fluctuations, among other technoeconomic characteristics, working and fixed capital also deserve a separate treatment.

In the light of the above considerations, we assume a generalized version of a four-factor CES production function of the following form:

$$
\begin{equation*}
\mathrm{V}=\beta\left(\alpha \mathrm{K}_{1}^{-\beta} 12+\phi \mathrm{K}_{2}^{-\beta 12}\right)^{-\rho_{1} / \beta} 12\left(\gamma \mathrm{~L}_{1}^{-\beta} 34+\delta \mathrm{L}_{2}^{-\beta} 34\right)^{-\rho_{2} / \beta_{34}} \tag{3.a}
\end{equation*}
$$

where $K_{1}$ - is fixed capital, $K_{2}$, working capital or stocks, and $K_{1}+K_{2}=K$; $\mathrm{L}_{1}$ - wage-1abour and $\mathrm{L}_{2}$ - self-employed labour including family workers, . $L_{1}+L_{2}=L ; \rho_{1}+\rho_{2}=1$, i.e. constant returns to scale. The relative factor prices are assumed to be equal to the relative marginal products, so that:

$$
\begin{equation*}
\left(\frac{r_{1}}{r_{2}}\right)=\left(\frac{\phi}{\alpha}\right)\left(\frac{K_{2}}{\mathrm{~K}_{1}}\right)^{\sigma} \tag{3.b}
\end{equation*}
$$

and $\quad\left(\frac{w_{1}}{w_{2}}\right)=\left(\frac{\delta}{\gamma}\right)\left(\frac{L_{2}}{L_{1}}\right)^{\sigma}$
$r_{1}$ - is rate of return to $K_{1}$ and $r_{2}$, rate of return to $K_{2}$, woty - labour compensation to $L_{1}$ and ${ }_{2}$ - labour compensation to $L_{2}$.

The production function (3.a) is treated at three different levels each of which is considered one by one below:
A. First Leve1

In the first stage, we specify an aggregate function for total capital:

$$
\begin{equation*}
\mathrm{K} *=\mathrm{f}\left(\mathrm{~K}_{1} \cdot \cdot \cdot \cdot \cdot \mathrm{~K}_{\mathrm{n}}\right) \tag{4,a}
\end{equation*}
$$

which is based essentially on the assumption of functional separability of variables. Thus, under this stringent condition, the production function could be written in the following form:

$$
\begin{equation*}
V=F\left\{L, g\left(K_{1} . \cdots \cdot \cdots K_{n}\right)\right\} \tag{4.b}
\end{equation*}
$$

Then the aggregate function for $K *$ which has CES properties can be written as:

$$
\begin{align*}
& \mathrm{K}^{*}=\left(\alpha \mathrm{K}_{1}^{-\beta}+\phi \mathrm{K}_{2}^{-\beta}\right)^{-1 / \beta}  \tag{4.c}\\
& \mathrm{K}^{*}=\left(\mathrm{K}_{1}^{-\beta}+\frac{\left.\phi_{\mathrm{K}_{2}}^{-\beta}\right)^{-1 / \beta}}{}\right. \tag{4.c.1}
\end{align*}
$$

In order to estimate $K *$ from (4.c), we need prior information on $\beta$ the substitution parameter and on $\alpha$ and $\phi$ - the distribution parameters. Such information can be obtained by fitting the following logarithmic form of equation (3.b):

$$
\begin{equation*}
\log \left(\frac{r_{1}}{r_{2}}\right)=\left(\frac{\phi}{\alpha}\right)+\sigma \log \left(\frac{\mathrm{K}_{2}}{\mathrm{~K}_{1}}\right)+\Sigma \tag{3.b.1}
\end{equation*}
$$

where $\Sigma$ - is the stochastic term, and $\beta=\left(\frac{1-\sigma}{\sigma}\right)$. In order to be able to estimate $(3 . b .1)$, we need $\left(\frac{{ }^{r} 1}{r_{2}}\right)$, the ratio of the rates of return from $K_{1}$ and $K_{2}$.

In both wholesale and retail business, net profit on total investment is affected, to a large extent, by the percentage of net profit on capital invested in stocks of merchandise. It is therefore desirable to estimate rates of return separately since they are unlikely to be identical due to differences in durability and the range of alternative uses of $\mathrm{K}_{1}$ and $\mathrm{K}_{2}$. In the absence of any better recourse, we assume that the stocks of retailers $\left(\mathrm{K}_{2}\right)$ which have a short life-cycle, earn short-term interest rate

## 1

The separation of $L$ in this equation, it must be borne in mind, implies a rather unrealistic assumption that the relative marginal productivities of different types of capital goods remain unaffected by labour.
and the residual of total profits accrues to fixed capital $\left(K_{1}\right)$. Thus, if $P$ is total profits, $r_{1}$ - rate of return from $K_{1}$ and $r_{2}$ - rate of return from $K_{2}$, $V$ - value added or "gross margin," w - wage-rate, and L , labour, then,

$$
\mathrm{P}=\mathrm{V}-\dot{\mathrm{w}} \cdot \mathrm{~L}=\mathrm{r}_{1} \mathrm{~K}_{1}+\mathrm{r}_{2} \mathrm{~K}_{2}
$$

and $r_{1} K_{1}=P-r_{2} K_{2}$. Under competitive condj.tions, $r_{1}=\frac{\partial V}{\partial K_{1}}$ and $r_{2}=\frac{\partial V}{\partial K_{2}}$, so that

$$
P=\frac{\partial V}{\partial K_{1}} K_{1}+\frac{\partial V}{\partial K_{2}} K_{2} .
$$

For lack of adequate number of observations, and the data on fixed capital, our cross-country sample could not be used to estimate equations (3.b.1) and (4.c). As Taiwan is one of the very few less developed countries with fairly detailed statistics on retail trades, we used information on twenty retail industries for 1961. The estimated equation (3.b.1) is as follows:

$$
\begin{align*}
& \log \left(\frac{{ }^{r} 1}{r_{2}}\right)=-1.349-\underset{(0.201)}{0.533} \log \left(\frac{\mathrm{~K}_{2}}{\mathrm{~K}_{1}}\right)  \tag{3.b.1}\\
& \overline{\mathrm{R}}^{2}=0.281 ; \text { since } \sigma=0.533, \beta=\frac{1-\sigma}{\sigma}=0.876 .
\end{align*}
$$

Thus, given the elasticity of substitution , which turns out to be less than unity as is to be expected, the aggregate K * function (4.c.1) was solved as:

$$
\begin{equation*}
\mathrm{K}^{*}=\left(\mathrm{K}_{1}^{.876}+1.349 \mathrm{~K}_{2}^{.876}\right)^{1 / .876} \tag{4.c.1}
\end{equation*}
$$

$1_{\text {For }} 1961, r_{\text {r }}$ for Taiwan (central bank call loan rate) is estimated at $16.2 \%$ (Cf. IMF, International Financial Statistics.) $K_{2}$ represents book-value of fixed capital assets, and $\mathrm{K}_{1}$, average inventory stocks.

## B. Second Level

Having estimated the aggregate $K^{*}$, we specify the aggregate labour function as:

$$
\begin{equation*}
L^{*}=f\left(L_{1} \cdot \cdots \cdot L_{n}\right) \tag{5.a}
\end{equation*}
$$

where the underlying production function is of the form:

$$
\begin{equation*}
\mathrm{V}=\mathrm{F}\left\{\mathrm{~K}, \mathrm{~g}\left(\mathrm{~L}_{1} \cdot \cdots \cdot \mathrm{~L}_{\mathrm{n}}\right)\right\} \tag{5.b}
\end{equation*}
$$

This stringent condition (5.b) need not be as unrealistic as (4.b) at least in retail trades. After all, if fixed capital plays a minor role in the growth of output in non-material production, it must be the quality of labour ("human capital") that mainly accounts for it. It may therefore be assumed that the relative marginal productivities of different types of labour remain unaffected by capital.

The function (5.a) with CES properties takes the following form:

$$
\begin{equation*}
L^{*}=\left(\gamma L_{1}^{-\beta}+\delta L_{2}^{-\beta}\right)^{-1 / \beta} \tag{5.c}
\end{equation*}
$$

The elasticity of substitution between $L_{1}$ and $L_{2}$ was estimated by transforming equation (3.c) into logarichmic form. The estimate of this equation is:

$$
\begin{aligned}
& \log \left(\frac{W_{1}}{W_{2}}\right)=-0.345-0.037 \log \left(\frac{L_{2}}{L_{1}}\right) \\
& \bar{R}^{2}=0.049 .
\end{aligned}
$$

As there is no relationship between ratio of earnings and the marginal rate of substitution, ${ }^{1}$ for convenience, we assume an infinite elasticity of substitution ( $\sigma$ ) between $L_{1}$ and $L_{2}$. When $\sigma=\infty, \beta=-1$. Therefore the aggregate function (5.c) simplifies as follows:
${ }^{1}$ The equation (3.c.1) was run twice taking $L_{2}$, first inclusive of family workers and then exclusive of them. No significant difference was made to the results. In the estimate presented above, $\mathrm{L}_{2}$ refers to owner-operators only.

$$
\begin{align*}
L^{*} & =\left(\gamma L_{1}+\delta L_{2}\right)  \tag{5.d}\\
L^{*} & =\left(\frac{\gamma}{\delta} L_{1}+L_{2}\right)  \tag{5.e}\\
& =\left(.702 L_{1}+L_{2}\right),
\end{align*}
$$

where $\left(\frac{\gamma}{\delta}=.702\right)$ is the mean relative earnings of the two types of labour.

## C. Third Level

Given the values of $\mathrm{K} *$ and $\mathrm{L}^{*}$, the aggregate CES production function can be estimated by assuming that:

$$
\begin{equation*}
\mathrm{V}=\left(\alpha \mathrm{K} *^{-\rho}+\beta \mathrm{L}^{-\rho}\right)^{-1 / \rho} \tag{6.a}
\end{equation*}
$$

If the elasticity of substitution between $\mathrm{K}^{*}$ and $\mathrm{L}^{*}$ is unity, as assumed by Uzawa, ${ }^{1}$ the above CES function simply reduces to the familiar Cobb-Douglas form:

$$
\mathrm{V}=\mathrm{K} *^{\alpha} \cdot \mathrm{L} *^{\beta}
$$

In order to examine whether the restrictive assumption of unit elasticity holds, we invoke the side relation (2.f) again so that,

$$
\begin{equation*}
\left(\frac{\mathrm{W}}{\mathrm{r}}\right)=\left(\frac{\alpha}{\beta}\right)\left(\frac{\mathrm{K}^{*}}{\mathrm{~L}^{*}}\right)^{\sigma} \tag{2.f}
\end{equation*}
$$

By transforming this relation into logarithms we obtained the following regression equation:

$$
\begin{align*}
& \log \left(\frac{\mathrm{W}}{\mathrm{r}}\right)=-9.279+\frac{1.022}{(0.373)} \log \left(\frac{\mathrm{K}^{*}}{\mathrm{~L}^{*}}\right)  \tag{2.f.1}\\
& \overline{\mathrm{R}}^{2}=0.294 \quad \sigma=1.022
\end{align*}
$$

Although the $\bar{R}^{2}$ adjusted for degrees of freedom is too low for comfort,
${ }^{1}$ Cf. H. Uzawa, Production Functions with Constant Elasticities of Substitution, Review of Economic Studies 29 (1962) pp. 291-99. Also Murray Brown, On the Theory and Measurement of Technological Change, 1966, Appendix B.
$\sigma$ - coefficient is quite significant. Admittedly, our estimates are very preliminary and may well be quite fortuitous. Yet, it is of some interest to note that the value of $\sigma$ at 1.02 suggests that our estimating function a la Uzawa, is a hybrid between Cobb-Douglas and CES since $\sigma$ is different from unity within pairs but equal to unity across pairs.

## Conclusions:

We have attempted to traverse a rather uncharted territory purely in the spirit of a preliminary exploration. The inadequacies of data and the small size of our sample do not warrant any conclusive generalisations. Also our use of some coefficients in spite of discomforting $\overline{\mathrm{R}}^{2}$ may be open to question. However, one of the explanations for the low $\overline{\mathrm{R}}^{2}$ may be found in the wrong specification of the side relation with which the CES elasticity of substitution is measured. Logically, the use of empirical facts of retailing which is typical of imperfect competition may not be expected to generate an estimate of elasticity of substitution which corresponds to the world of perfect factor and product markets.

Nevertheless, interest in exploring the elasticity of substitution between capital and labour is not merely theoretical. It bears a great policy significance which is often overlooked in the discussion on choice of techniques. Under conditions of low elasticity of substitution and low employment elasticity of output in manufacturing, the LDCs are planning for much of labour absorption to occur in the tertiary sector. A knowledge of the elasticity of substitution in different tertiary sub-sectors would provide a useful guideline for such employment planning.

Any information on economic indicators for retail distribution in the LDCs is, in our knowledge, very rare. We therefore decided to produce the basic data which were used in the text. Six main sub-categories of retail trades were considered. Most of the statistics are computed from national census reports. In certain cases, data had to be grouped into these categories somewhat arbitrarily. Since the LDCs do not follow any standard international classification for compiling retail trade statistics, full comparability cannot be guaranteed. The following notations are used in the tables:

```
        S: total sales
            r: total rate of return to aggregate capital (K)
            r_
            r}\mp@subsup{\mp@code{2}}{\mathrm{ : rate of return to working K}}{2
            S/L}\mp@subsup{e}{e}{:}\mathrm{ sales per employee
            S/L
                    V/L
                    V/L
                    K/L}\mp@subsup{e}{e}{: total capital per employee
                    K/L L
                    K
                    K
                        K
```

$$
\begin{aligned}
W / L_{e}: & \text { annual wage per employee } \\
K_{2} / K_{1} & \text { : ratio of working capital to fixed capital } \\
L_{2} / L_{1}: & \text { ratio of self-employed (excluding family labour) to wage-labour } \\
K / L: & \text { total capital-labour ratio } \\
r_{1} / r_{2}: & \text { ratio of rates of return from } K_{1} \text { and } K_{2} \\
W_{1} / W_{2}: & \text { ratio of earnings of } L_{1} \text { and } L_{2} \\
W / r: & \text { ratio of wage-rate to total rate of return }
\end{aligned}
$$

N.B. Data on fixed capital represent undeflated book-values of fixed capital assets. ${ }^{1}$ Data on working capital represent average inventory stocks for the whole year.

For a similar use of undeflated book value census data in a crosssectional analysis, see Phoebus J. Dhrymes, Some Extensions and Tests for the CES Class of Production Functions, Review of Economics and Statistics, November 1965. Also for a defence of the use of such data, see T. C. Liu and G. H. Hildebrand, Manufacturing Production Functions in the United States, 1957 (1965), Cornell Univ. Press, pp. 133-135.

# Appendix I <br> Table I: COLOMBIA (1954) <br> Data on Retail Industries 


I. Food \& Beverages

| Sales less than 5,000 pesos | 65.77 | 113.79 | 1.86 | 20.961 | 0.34 | 18.41 | 0.45 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5,000-24,999 pesos | 356.05 | 124.10 | 7.74 | 10.48 | 0.65 | 8.45 | 0.74 |
| -25,000-49,999: | 263.95 | 108.00 | 20.2 | 9.00 | 1.67 | 8.28 | 0.98 |
| 50,000-99,999 | 249.09 | 108.4 | 34.2 | 9.12 | 2.87 | 8.40 | 1.27 |
| 100,000-249,999 | 239.37 | 115.2 | 56.9 | 8.58 | 4.23 | 7.45 | 1.66 |
| 250,000-499,999 | 118.86 | 115.1 | 77.5 | 13.01 | 8.76 | 1.13 | 2.07 |
| 500,000-999,999 | 75.37 | 140.1 | 106.6 | 24.54 | 18.67 | 17.51 | 2.30 |
| 1,000,000-2,499,999 | 44.11 | 154.2 | 132.5 | 30.54 | 26.2 | 19.80 | 2.98 |
| 2,500,000 \& above | 30.80 | 410.6 | 342.2 | 18.08 | 15.0 | 4.40 | 4.09 |

II. General Merchandise

| Sales less than 5,000 pesos | 5.12 | 60.97 | 1.77 | 25.21 | 0.75 | 41.35 | 0.51 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5,000-24,999 pesos | 37.73 | 70.92 | 7.20 | 30.49 | 3.09 | 42.99 | 0.82 |
| 25,000-49,999 | 39.02 | 60.59 | 15.80 | 22.23 | 5.80 | 36.69 | 1.25 |
| 50,000-99,999 | 43.90 | 61.75 | 25.8 | 22.35 | 9.35 | 36.19 | 1.46 |
| 100,000-249,999 | 70.28 | 59.31 | 37.7 | 19.71 | 12.54 | 33.23 | 2.01 |
| 250,000-499,999 | 46.64 | 54.30 | 44.6 | 15.09 | 12.42 | 27.80 | 2.47 |
| 500,000-999,999 | 36.95 | 39.73 | 36.8 | 8.89 | 8.24 | 22.37 | 2.12 |
| 1,000,000-2,499,999 | 53.21 | 35.76 | 34.8 | 9.25 | 9.01 | 25.87 | 2.55 |
| 2,500,000 \& above | 90.22 | 35.97 | 35.6 | 6.14 | 6.07 | 17.07 | 3.02 |

III. Textiles \& Clothing

| Sales less than 5,000 pesos | 4.71 | 28.03 | 2.34 | 13.71 | 1.06 | 48.92 | 0.70 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5,000-24,999 pesos | 40.27 | 42.26 | 7.20 | 18.00 | 3.27 | 42.59 | 0.92 |
| 25,000-49,999 | 52.10 | 49.67 | 11.25 | 20.09 | 6.68 | 40.44 | 1.69 |
| 50,000-99,999 | 78.16 | 50.10 | 25.85 | 20.35 | 10.16 | 40.62 | 1.53 |
| 100,000-249,999 | 132.13 | 55.52 | 37.72 | 19.75 | 13.32 | 35.58 | 3.31 |
| 250,000-499,999 | 78.19 | 66.10 | 44.67 | 20.41 | 16.38 | 30.88 | 2.96 |
| 500,000-999,999 | 54.51 | 71.92 | 36.34 | 16.17 | 14.45 | 23.04 | 3.15 |
| 1,000,000-2,499,999 | 27.29 | 101.84 | 34.85 | 23.78 | 21.24 | 23.26 | 3.19 |
| 2,500,000 \& above | 13.74 | 205.07 | 35.57 | 25.36 | 22.65 | 12.37 | 5.45 |

IV. Furniture and

Domestic Appliances

| Sales less than 5,000 pesos | 1.00 | 17.03 | 1.82 | 4.76 | 0.51 | 27.96 | 0.675 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| $5,000-24,999$ pesos | 6.62 | 23.32 | 7.04 | 5.12 | 1.54 | 21.95 | 1.12 |
| $25,000-49,999$ " | 10.13 | 27.84 | 14.97 | 5.89 | 3.16 | 21.17 | 1.43 |
| $50,000-99,999 "$ | 15.39 | 35.23 | 22.94 | 11.15 | 7.27 | 31.66 | 1.87 |

Table I, Appendix I, cont.

VI. Automobiles \&

Accessories

| Sales less than 5,000 pesos | 0.10. | 6.66 | 1.61 | 6.76 | 1.63 | 101.00 | 0.66 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5,000-24,999 pesos | 1.67 | 17.61 | 7.58 | 21.37 | 7.80 | 121.40 | 1.27 |
| 25,000-49,999 | 3.11 | 26.35 | 14.46 | 13.59 | 7.46 | 51.56 | 1.79 |
| 50,000-99,999 | 7.15 | 30.06 | 20.92 | 12.87 | 8.95 | 42.80 | 4.94 |
| 100,000-249,999 | 21.36 | 44.69 | 33.54 | 17.28 | 12.97 | 38.68 | 2.88 |
| 250,000-499,999 | 20.85 | 71.45 | 56.70 | 16.43 | 13.04 | 23.48 | 3.30 |
| 500,000-999,999 | 29.87 | 76.41 | 68.06 | 16.45 | 14.65 | 21.36 | 4.61 |
| 1,000,000-2,499,999 | 55.47 | 80.05 | 75.58 | 14.88 | 14.05 | 18.60 | 5.17 |
| 2,500,000 \& above | 62.61 | 105.34 | 102.15 | 13.49 | 13.09 | 12.82 | 4.76 |

VII. Hardware and

Construction


Source: Colombia, Departamento Administrativo Nacional de Estadistica: Censo Nacional de Comercio y Servicios for 1954 (April 1957).

## Appendix I

Table 2: TAIWAN
Data on Retail Trades


Source: Industrial and Commercial Census of Taiwan, Vol. IV.
N.B. Total number of persons engaged refers to regular employees, owneroperators and unpaid family workers.

Table III
Taiwan: Ratios of Capital to Labour, Capital to Capital, Labour to Labour, etc.

| Industry | $\left(\mathrm{K}_{2} / \mathrm{K}_{1}\right)$ | $\left(L_{2} / L_{1}\right)$ | (K/L) | $\left(\frac{r_{1}}{r_{2}}\right)$ | $\left(\frac{W_{1}}{W_{2}}\right)$ | $\left(\frac{W}{r}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 0.11 | 3.56 | 53.61 | 0.66 | 0.62 | 7.67 |
| 2. | 0.03 | 5.17 | 13.92 | -3.29 | 0.61 | -1.81 |
| 3. | 0.03 | 8.07 | 29.91. | 0.66 | 0.88 | 5.40 |
| 4. | 0.09 | 6.37 | 43.65 | 0.73 | 0.77 | 5.74 |
| 5. | 0.13 | 14.93 | 37.12 | 1.15 | 0.59 | 4.19 |
| 6. | 0.12 | 4.12 | 65.28 | 0.45 | 0.58 | 11.20 |
| 7. | 0.09 | 2.01 | 48.62 | 0.85 | 0.80 | 5.64 |
| 8. | 0.29 | 2.63 | 63.43 | 0.58 | 0.62 | 10.16 |
| 9. | 0.18 | 1.41 | 66.81 | 1.21 | 0.66 | 4.51 |
| 10. | 0.18 | 3.56 | 56.41 | 0.74 | 0.74 | 6.72 |
| 11. | 0.31 | 1.04 | 68.24 | 0.62 | 0.79 | 9.01 |
| 12. | 0.16 | 0.61 | 63.10 | 0.68 | 0.60 | 7.70 |
| 13. | 0.15 | 1.45 | 74.50 | 0.68 | 0.59 | 7.66 |
| 14. | 0.31 | 1.15 | 64.83 | 0.85 | 0.63 | 6.93 |
| 15. | 0.21 | 1.13 | 59.11 | 0.84 | 0.64 | 6.68 |
| 16. | 0.14 | 4.11 | 55.05 | 1.60 | 0.62 | 2.97 |
| 17. | 0.47 | 0.39 | 61.23 | 1.19 | 0.82 | 6.91 |
| 18. | 0.29 | 0.55 | 68.19 | 0.42 | 0.70 | 14.89 |
| 19. | 0.44 | 0.58 | 54.26 | 0.24 | 1.16 | 30.93 |
| 20. | 0.55 | 0.41 | 70.63 | 0.05 | 0.63 | 166.49 |

## Appendix II

Table I

1. Food \& Beverages, Eating \& Drinking Places

| $\left(S / L_{e}\right)$ | $\left(\mathrm{K}_{2} / L_{e}\right)$ | $\left(\mathrm{W} / \mathrm{L}_{\mathrm{e}}\right)$ | $(\mathrm{r})$ |
| :--- | :---: | :---: | :---: |
| $(\$)$ | $(\$)$ | $(\$)$. | $(\%)$ |


| Puerto Rico | 1958 |  | 30328 | n.a. | 1179 |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| Kenya | 1960 | 12448 | (1) 1152 | (2) 543 |  |  |
| Trinidad \& Tobago | 1957 | (4) 23014 | (3) $1365 \times$ | 805 |  |  |
| Philippines | 1961 | (4) $21556 \times$ | (5) $1051 \times$ | 496 x | 5.00 |  |
| Ecuador (5) | 1965 |  | 17288 | 1475 | 318 | 5.00 |
| Costa Rica | 1964 | 23812 | 2196 | 620 | 5.00 |  |
| Colombia | 1954 | 33811 | 3232 | 368 | 4.00 |  |
| Chile | 1967 | 26943 | n.a. | 674 | 15.84 |  |
| Chile | 1964 | 19184 | n.a. | 514 | 14.63 |  |
| Argentina | 1954 | 26930 | 3961 | 640 |  |  |
| Panama | 1961 | 59521 | 6664 | 2798 | n.a. |  |
| Peru | 1963 | 10377 | 960 | 274 | 9.50 |  |
| Cyprus | 1956 | 38820 | 4371 | 407 |  |  |
| El Salvador | 1956 | 23147 | 373 | 222 | 3.00 |  |
| Taiwan | 1961 | 19281 | 375 | 163 | 16.2 |  |
| Puerto Rico | 1963 | (4) 30584 | $n . a$. | 1714 | n.a. |  |
| Zambia | 1962 |  | 5571 | 483 | 477 | n.a. |
| Brazil | 1959 | 4220 | (1) 524 | 108 | 8.0 |  |
| Paraguay | 1963 | 52197 | 499 | 531 | 6.0 |  |
| Rhodesia | 1962 | 11398 | 937 | 821 | n.a. |  |

(1) end of the year stock
(2) cash and non-cash
(3) data on stocks by types of business were only collected for firms employing 25 or more. These data were used as the basis for estimating the breakdown by types for firms employing 5-24 persons.
(4) gross receipts
(5) for large establishments only
$x$ excluded from sample for regression
n.a. not available

Table II
2. Textiles and Clothing and Other Dry Goods


Table III
3. Furniture and Domestic Appliances
$\left(\mathrm{S} / \mathrm{L}_{\mathrm{e}}\right)$
$(\$)$
$\left(K_{2} / L_{e}\right)$
(\$)
(W/Le)
(\$)

| Puerto Rico | 1958 |  | 18838 |  |  | n.a. |  |  | 2202 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Kenya (1) | 1960 |  | 9542 | x | (2) | 2200 | x | (7) | 697 x |
| Trinidad \& Tobag | 1957 |  | 18741 | x | (6) | 6139 | x |  | 1437 x |
| Philippines (3) | 1961 | (4) | 15034 | X |  | 1449 | x |  | 1124 x |
| Ecuador (3) | 1965 |  | 12846 | x |  | 8315 | x |  | 848 x |
| Costa Rica | 1964 |  | 16517 |  |  | 5545 |  |  | 1329 |
| Colombia | 1954 |  | 12065 |  |  | 3117 |  |  | 1059 |
| Chile | 1967 |  | 26876 |  |  | n.a. |  |  | 1073 |
| Chile | 1964 |  | 14538 |  |  | n.a. |  |  | 879 |
| Argentina | 1954 |  | 16378 |  |  | 5693 |  |  | 981 |
| Panama | 1961 |  | 20267 |  |  | n.a. |  |  | 915 |
| El Salvador | 1961 |  | 10784 |  |  | 2722 |  |  | 1351 |
| Taiwan | 1961 |  | 7324 |  |  | 692 |  |  | 140 |
| Puerto Rico | 1963 | (5) | 21920 |  |  | n.a. |  |  | 2312 |
| Zambia | 1962 |  | 6485 |  |  | 1864 |  |  | 1210 |
| Brazil | 1959 |  | 7260 |  |  | 1935 |  |  | 1509 |
| Paraguay | 1963 |  | 9841 |  |  | 1279 |  |  | 864 |
| Rhodesia | 1962 |  | 11517 |  |  | 3051 |  |  | 1694 |

(1) included building materials \& timber
(2) end of the year stock
(3) large establishments
(4) sales \& resales
(5) gross receipts
(6) Data by types of business were only collected from firms employing 25 persons or more. These were used as the basis for estimating the breakdown by types for firms engaging 5-24.
(7) cash and non-cash

$$
\begin{aligned}
x & =\text { excluded from the sample } \\
\text { n.a. } & =\text { not available }
\end{aligned}
$$

Table IV
4. Pharmacies and Drugstores

| $\left(S / L_{e}\right)$ | $\left(K_{2} / L_{e}\right)$ | $\left(W / L_{e}\right)$ |
| :---: | :---: | :---: |
| $(\$)$ | $(\$)$ | $(\$)$ |


| Puerto Rico | 1958 |  | 16059 |  |  | n.a. |  | 1584 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Kenya (1) | 1960 |  | 10635 | x | (2) | 2471 x | (6) | 1125 x |
| Trinidad | 1957 |  | 9553 |  |  | n.a. |  | 677 |
| Philippines (3) | 1961 | (5) | 9846 | x |  | 6074 x |  | 815 x |
| Ecuador (3) | 1965 |  | 8236 | x |  | 9640 x |  | 839 x |
| Costa Rica | 1964 |  | 12758 |  |  | 2511 |  | 884 |
| Colombia | 1954 |  | 10820 |  |  | n.a. |  | 344 |
| Chile | 1967 |  | 13521 |  |  | n.a. |  | 762 |
| Chile | 1964 |  | 12991 |  |  | n.a. |  | 636 |
| Argentina | 1954 |  | 10021 |  |  | 3315 |  | 436 |
| Panama | 1961 |  | 38051. |  |  | 8859 |  | 3923 |
| Peru | 1963 |  | 6664 |  |  | 2069 |  | 592 |
| Cyprus | 1956 |  | 16607 |  |  | 6917 |  | 667 |
| E1 Salvador | 1961 |  | 10120 |  |  | 1193 |  | 514 |
| Puerto Rico | 1963 | (4) | 20406 |  |  | n.a. |  | 2002 |
| Zambia | 1962 |  | 7681 |  |  | 1419 |  | 1086 |
| Brazil | 1959 |  | 5822 |  | (2) | 1943 |  | 1000 |
| Paraguay | 1963 |  | 16589 |  |  | 4068 |  | 672 |
| Rhodesia | 1962 |  | 10257 |  |  | 2084 |  | 1652 |

(1) includes photographic goods
(2) end of the year stock
(3) large establishments
(4) gross receipts
(5) sales and resales
(6) cash and non-cash

$$
\begin{aligned}
x & =\text { excluded from sample for regression } \\
\text { n.a. } & =\text { not available }
\end{aligned}
$$

Table V
5. Automobiles and Vehicles

| $\left(\mathrm{S} / \mathrm{L}_{\mathrm{e}}\right)$ | $\left(\mathrm{K}_{2} / \mathrm{L}_{\mathrm{e}}\right)$ | $\left(\mathrm{W} / \mathrm{L}_{\mathrm{e}}\right)$ |
| :---: | :---: | :---: |
| $(\$)$ | $(\$)$ | $(\$)$ |
|  |  |  |
| 57843 | n.a. | 2766 |
| 10539 | $(1)$ | 3361 |
| 41725 | $(3) 6623$ | 1265 |
| 25030 x | 3541 x | 1891 |
| 22197 x | 5762 x | 897 x |
| 23044 | 7916 | 1264 x |
| 19823 | 4376 | 1372 |
| 21029 | n.a. | 1185 |
| 14187 | n.a. | 1920 |
| 19535 | 6574 | 1034 |
| 23008 | 4170 | 890 |
| 60536 | 6809 | 1275 |
| 9478 | 8811 | 1033 |
| 21259 | 5438 | 503 |
| 4566 | 880 | 1488 |
| 68288 | $\mathrm{n} . \mathrm{a}$. | 225 |
| 9884 | 1019 | 3606 |
| 11962 | 2257 | 912 |
| 23425 | 4300 | 2119 |
| 10928 | 1552 | 917 |

(1) end of the year stock
(2) cash and non-cash
(3) Data by types of business were only collected from firms employing 25 or more persons. These were used as the basis for estimating the breakdown by types for firws engaging 5-24.

$$
\begin{aligned}
x & =\text { excluded from sample for regression } \\
\text { n.a. } & =\text { not available }
\end{aligned}
$$

Table VI
6. Gas and Fuel
$\left(S / L_{e}\right) \quad\left(K_{2} / L_{e}\right) \quad\left(W / L_{e}\right)$
(\$)
(\$)
(\$)

| Puerto Rico | 1958 | 20019 | n.a. | 1231 |
| :--- | ---: | ---: | ---: | ---: |
| Kenya | 1960 | 8783 | (1) 291 | (2) 527 |
| Trinidad | 1957 | (3) 12781 | (4) 1099 | 907 |
| Philippines | 1961 | (3) $23265 \times$ | (5) $315 \times$ | $711 \times$ |
| Ecuador (5) | 1965 | $1758 \times$ | $446 \times$ | $1263 \times$ |
| Costa Rica | 1964 | 12081 | 625 | 746 |
| Colombia | 1954 | 10906 | 651 | 516 |
| Chile | 1967 | 17497 | n.a. | 582 |
| Chile | 1964 | 14857 | n.a. | 516 |
| Argentina | 1954 | 19666 | 1499 | 718 |
| Panama | 1961 | 5341 | 354 | 375 |
| Peru | 1963 | 11323 | 842 | 530 |
| Cyprus | 1956 | 32180 | 834 | 698 |
| Puerto Rico | 1963 | (3) 19648 | $n . a$. | 1574 |
| Zambia | 1962 | 4300 | 155 | 400 |
| Brazil | 1959 | 9480 | (1) 761 | 382 |
| Paraguay | 1963 | 1596 | 581 | 651 |
| Rhodesia | 1962 | 12734 | 3051 | 1687 |

(1) end of the year stock
(2) cash and non-cask.
(3) gross receipts
(4) Data on stocks by types of busizess were only collected for firms employing 25 persons or more. These data were used as the basis for estimating the breakdown for firms engaging $5-24$ persons.
(5) large establishments only

$$
\begin{aligned}
x & =\text { excluded from sample for regression } \\
\text { n.a. } & =\text { not available }
\end{aligned}
$$


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[^1]:    ${ }^{1}$ K. Arrow, H. B. Chenery, R. Solow, and B. Minhas, "Capital-Labour Substitution and Economic Efficiency," Review of Economics and Statistics, August 1961.

[^2]:    ${ }^{1}$ Most authors have so far concentrated on manufacturing for lack of data of good quality for agriculture and service sectors. For a recent review, see Marc Nerlove, "Recent Empiricai Studies of the CES and Related Production Functions," in Murray Brown (ed.), The Theory and Empirical Analysis of Production, NBER, New York, 1967.
    ${ }^{2}$ In the words of Bagicha Minhas, ". . . any estimates of the elasticities of substitution between capital and labour in these sectors (j.e. agriculture and services) which further research may produce would be very useful." (B. Minhas, An International Comparison of Factor Cost and Factor Use, NorthHolland Publishing Co., 1963, p. $97 \%$ ) The present attempt should be treated as only a modest exercise which is undertaken in full zecognition of the inadequacy and poor quality of comparable data. One of the objectives of the present study is to malke a beginnimg with the processing of requisite data.

[^3]:    $1_{\text {See Amartya Kumar Sen, "Working Capital in the Indian Economy: A Con- }}$ ceptual Framework and Some Estimates," in $P$, N. Rosenstein-Rodan (editor), "Pricing and Fiscal Policies" -- Studies in the Economic Development of India, Series No. 3, MIT.

[^4]:    ${ }^{1}$ For fuller details of the types of economies associated with expansion of output of retail distribution, see Margaret Hall, John Knapp, and Christopher Winsten, Distribution in Great Britain and North America, Oxford University Press, 1961, Chapter Seven on "Economies of Scale."
    ${ }^{2}$ Cf. J. P. Verdoorn, Complementarity and Long-range Projections, Econometrica, 1956. According to Verdoorn, a stable, long-run relationship exists between labour productivity and the level of output. The statistical basis of the relation was shown by the logarithmic regression of output per man on output. The regression coefficient was significant and varied from 0.45 to 0.60 .

[^5]:    ${ }^{1}$ See Muxray Brown and John S. de Cani, Technological Change and the Distribution of Income, International Economic Review, September 1963.
    ${ }^{2}$ In the absence of any data on fixed capital, $K$ - represented working capital only. r - ite rate of return was assumed to be equal to the shortterm interest rate. The data on these interest rates were taken from the IMF International Financial Statistics.

