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# Modeling extreme events: time-varying extreme tail shape\*

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#### Abstract

We propose a dynamic semi-parametric framework to study time variation in tail parameters. The framework builds on the Generalized Pareto Distribution (GPD) for modeling peaks over thresholds as in Extreme Value Theory, but casts the model in a conditional framework to allow for time-variation in the tail shape parameters. The score-driven updates used improve the expected Kullback-Leibler divergence between the model and the true data generating process on every step even if the GPD only fits approximately and the model is mis-specified, as will be the case in any finite sample. This is confirmed in simulations. Using the model, we find that Eurosystem sovereign bond purchases during the euro area sovereign debt crisis had a beneficial impact on extreme upper tail quantiles, leaning against the risk of extremely adverse market outcomes while active.

**Keywords:** dynamic tail risk, observation-driven models, extreme value theory, European Central Bank (ECB), Securities Markets Programme (SMP).

JEL classification: C22, G11.

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## 1 Introduction

This paper proposes a novel semi-parametric framework to study time variation in tail fatness for long univariate time series, applied to high-frequency government bond returns during times of unconventional central bank policies. The new method builds on ideas from Extreme Value Theory (EVT) by using a conditional Generalized Pareto Distribution (GPD) to approximate the tail beyond a given threshold, and endowing this conditional GPD distribution with time-varying parameters. The GPD is an appropriate tail approximation for most heavy-tailed densities used in econometrics and actuarial sciences; see, for example, Embrechts et al. (1997), Coles (2001), and McNeil et al. (2010, Chapter 7). As a result, the GPD plays a central role in the study of extremes, comparable to the role the normal distribution plays when studying observations in the center of the distribution. Our framework allows us to study the time-variation in tail parameters associated with time series observations from a wide class of heavy-tailed distributions; see Rocco (2014) for a recent survey of EVT methods in finance. We discuss the handling of non-tail time series observations, inference on deterministic and time-varying parameters, and ways to relate time-varying parameters to observed covariates. In this context we also study the effect of time-varying pre-filtering methods possibly applied to the data before the dynamic GPD model is fitted.

In our model, the time-varying tail shape and tail scale parameters of the GPD are driven by the score of the local (time t) objective function; see e.g. Creal et al. (2013) and Harvey (2013). In this approach, the time-varying parameters are perfectly predictable one step ahead. This makes the model observation-driven in the terminology of Cox (1981). The log-likelihood is known in closed form, facilitating parameter estimation and inference via standard maximum likelihood methods. Simulation evidence reveals that our model and estimation approach is able to recover the time-varying tail shape and tail scale parameters sufficiently accurately, as well as EVT-based market risk measures such as Value-at-Risk (VaR) and Expected Shortfall (ES) at high confidence levels (say, 99%). This is the case even if the model is misspecified or the GPD approximation is not exact. The latter is particularly important in our finite sample setting, where the limiting result of the GPD can only hold approximately given the choice of a finite exceedance threshold in any particular sample.

We apply our modeling framework to study the location, scale, and upper tail impact of bond purchases undertaken by the Eurosystem – the European Central Bank (ECB) and its 17 national central banks at the time – during the euro area sovereign debt crisis between 2010 and 2012. We focus on bond purchases within the Eurosystem's Securities Markets Programme (SMP), which targeted sovereign bonds of five euro area countries: Greece, Ireland, Italy, Portugal, and Spain. Based on high-frequency data for five-year benchmark bonds, and explicitly accounting for time-variation in fat tails, we find that purchases lowered the conditional location (mean) of future bond yields by up to -2.9 basis points (bps) per  $\leq 1$ bn of purchases. The impact estimates for the two largest SMP countries, Italy and Spain, are -1.5 bps and -2.6 bps per  $\leq 1$  bn of purchases, respectively. These impact estimates are marginally smaller in absolute value than earlier estimates based on different methodologies; see Eser and Schwaab (2016), Ghysels et al. (2017), and Pooter et al. (2018).

In addition, we find that SMP purchases had a beneficial impact on the extreme upper tail quantiles of yield changes. This suggests that central bank bond purchases lean against the risk of extremely adverse market outcomes while they are active. The beneficial impact is mostly explained by moving the center of the predictive distribution to the left and narrowing it. Beneficial secondary effects come about via the SMP's effect on tail shape and tail scale for large economies such as Spain and Italy. The impact of purchases on tail quantiles is larger than their impact on the conditional location (mean). We estimate that the 97.5% VaR was reduced by 3.8, 6.0, 5.9, 2.1, and 6.9 bps per  $\leq$ 1 bn Eurosystem intervention in Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bonds, respectively. The impact grows with the extremeness of the VaR. We estimate that the 99.5% VaR was reduced, respectively, by 5.1, 10.1, 12.5, 2.9, and 15.4 bps per  $\leq$ 1 bn of Eurosystem purchases in the above bonds. The tail impact of the SMP purchases is economically relevant because extreme tail risks alone can force dealer banks and market makers to retreat from supplying liquidity to important segments of the sovereign bond market, particularly when their own VaR constraints are binding; see Vayanos and Vila (2009) and Adrian and Shin (2014). In turn, malfunctioning sovereign bond markets can impair the transmission of the common monetary policy to all parts of the euro area. Pelizzon et al. (2013, 2016) provide evidence that market makers withdrew from trading Italian debt securities in 2011.

Our paper is related to at least two strands of literature: one on modeling time-variation in tail parameters and one on assessing the effectiveness of central bank unconventional monetary policy measures. Regarding the first, several papers propose methodology to study time variation in the tail index. Davidson and Smith (1990), Coles (2001, Chapter 5.3), and Wang and Tsai (2009), among others, also index the GPD tail parameters with time subscripts and equip them with a parameterized structure. Our approach is different in that their "tail index regression" approach requires conditioning variables that explain (all of) the tail variation. Such variables are not always available. By contrast, our "filtering approach" does not require such conditioning variables, and is arguably better suited for the real-time monitoring of extreme risks. Second, Quintos et al. (2001), Einmahl et al. (2016), Hoga (2017), and Lin and Kao (2018) derive formal tests for a structural break in the tail index. A number of subsequent studies applied such tests to financial time series data. Werner and Upper (2004) identify a break in the tail behavior of high-frequency German Bund future returns. Galbraith and Zernov (2004) argues that certain regulatory changes in U.S. equity markets have altered the tail index dynamics of equities returns, and Wagner (2005)demonstrates that changes in government bond yields appear to exhibit time-variation in the tail shape for both the U.S. and the euro area. de Haan and Zhou (2020) propose a non-parametric approach to estimating the extreme value index locally. Our paper adds to this strand of conditional EVT literature by proposing a model that allows us to study both the tail shape and tail scale dynamics directly in a semi-parametric way. Explanatory covariates can be included in the dynamics of both parameters, and likelihood ratio tests are available to test economically relevant hypotheses. Finally, unlike Patton et al. (2019), our tail VaR and ES dynamics explicitly account for fat tail shape beyond a threshold as emerging from EVT. The dynamics based on the score for the GPD contain weights for extreme observations. Such weights are absent in the elicitable score functions of Patton et al.. The resulting dynamics in our model are, as a result, more robust, particularly for

the ES.

A second strand of literature assesses the impact of central bank asset purchases on bond yields and yield volatility. For example, Ghysels et al. (2017) study the yield impact of SMP bond purchases by considering bond yields and purchases at 15-minute intervals. In this way they mitigate a bias that unobserved factors could have introduced. The authors estimate that SMP interventions had an impact on the conditional mean of 10-year maturity bonds of between -0.2 and -4.2 bps per  $\leq$ 1 bn of purchases. Eser and Schwaab (2016) study yield impact based on daily data. In their framework, identification is based on a panel model that exploits the cross-sectional dimension of the data. They find that, in addition to large announcement effects, purchases of 1/1000 of the respective outstanding debt had an impact of approximately -3 bps at the five-year maturity. Pooter et al. (2018) use the published weekly data of aggregate SMP purchases to test for an impact on country-specific sovereign bond liquidity premia. The authors find an average impact of -2.3 bps for purchases of 1/1000 of the outstanding debt. Our paper adds to the growing literature on assessing the effectiveness of central bank asset purchase programs by developing methodology for the extreme tail of the distribution.

Whereas de Haan and Zhou (2020) take a non-parametric perspective, the methodological part of this paper is closest to Massacci (2017), who also proposes a dynamic parametric model for the GPD parameters. Our framework is different in that we specify both parameters as functions of their respective scores, and adopt a non-diagonal scaling function. We cover inference on both deterministic and time-varying parameters, explain how to introduce additional conditioning variables, and provide Monte Carlo evidence. Owing to a novel autoregressive specification of the EVT threshold following Patton et al. (2019), our model can be fitted to both prefiltered and non-prefiltered time series data.<sup>1</sup>

We proceed as follows. Section 2 presents our statistical model. Section 3 discusses our simulation results. Section 4 studies the tail impact of Eurosystem asset purchases. Section 5 concludes. A Web Appendix derives the score and scaling function for the tail shape model

<sup>&</sup>lt;sup>1</sup>For computer code and an enumeration of recent work on score-driven models see http://www.gasmodel.com/code.htm.

and provides further technical and empirical results.

## 2 Statistical model

## 2.1 Time-varying tail shape and scale

This section introduces our model with time-varying tail shape and tail scale for a univariate time series  $y_t$ , t = 1, ..., T, where T denotes the number of observations. We assume

$$y_t = \mu_t + \sigma_t \,\varepsilon_t,\tag{1}$$

where  $g(\varepsilon_t | \mathcal{F}_{t-1})$  is the conditional probability density function (pdf) of  $\varepsilon_t$ ,  $\mu_t$  and  $\sigma_t$  are the conditional location and scale of  $y_t$ , and  $\mathcal{F}_{t-1} = \{y_{t-1}, y_{t-2}, \ldots, y_1\}$  denotes the information set. The parameters  $\mu_t$  and  $\sigma_t$  can take on many forms ranging from constant values to specifications with autoregressive and conditional volatility dynamics. Key, however, is that these parameters are typically mainly used to describe well the *center* of the distribution. In this paper, by contrast, we concentrate on the *tail* of the distribution using a dynamic extension of arguments from extreme value theory, similar to Patton's (2006) extension of copula theory to the dynamic, observation driven setting.

We assume the conditional pdf  $g(\varepsilon_t | \mathcal{F}_{t-1})$  has heavy tails with time-varying tail index  $\alpha_t > 0$ . A prime example is the univariate Student's t distribution with  $\nu_t = \alpha_t$  degrees of freedom. Other examples include the Pareto, inverse gamma, log-gamma, log-logistic, F, Fréchet, and Burr distribution with one or more time-varying shape parameters. Rather, however, than modeling the (dynamic) tail shape by an arbitrarily chosen parametric family of distributions, we appeal to well-known results from the extreme value theory (EVT) literature. From EVT, we know that the conditional cumulative distribution function (cdf)  $G(\varepsilon_t | \mathcal{F}_{t-1})$  of  $\varepsilon_t$  can under very general conditions be approximated by  $G(e_t | \mathcal{F}_{t-1}) =$  $G(\tau | \mathcal{F}_{t-1}) + (1 - G(\tau | \mathcal{F}_{t-1}))P(x_t; \delta_t, \xi_t)$  with  $x_t = e_t - \tau$  for sufficiently high thresholds  $\tau \in \mathbb{R}_+$ , or more precisely,

$$\lim_{\tau \to \infty} \sup_{e_t \ge \tau} \left| \mathbb{P} \left[ \varepsilon_t \le e_t + \tau \mid \varepsilon_t > \tau, \ \mathcal{F}_{t-1} \right] - P_{\xi_t, \delta_t}(e_t - \tau) \right|$$
$$= \lim_{\tau \to \infty} \sup_{e_t \ge \tau} \left| \frac{G(e_t + \tau \mid \mathcal{F}_{t-1}) - G(e_t \mid \mathcal{F}_{t-1})}{1 - G(e_t \mid \mathcal{F}_{t-1})} - P_{\xi_t, \delta_t}(e_t - \tau) \right| = 0,$$
(2)

for parameters  $\xi_t = \alpha_t^{-1}$  and  $\delta_t$ , both possibly depending on  $\tau$ . Here,  $P(x_t; \delta_t, \xi_t)$  denotes the cdf of the Generalized Pareto Distribution (GPD), with cdf and pdf given by

$$P(x_t; \delta_t, \xi_t) = 1 - \left(1 + \xi_t \frac{x_t}{\delta_t}\right)^{-\xi_t^{-1}}, \qquad p(x_t; \delta_t, \xi_t) = \delta_t^{-1} \cdot \left(1 + \xi_t \frac{x_t}{\delta_t}\right)^{-\xi_t^{-1} - 1}, \quad (3)$$

respectively (see, for example, McNeil et al., 2010). The quantity  $x_t = \varepsilon_t - \tau > 0$  is the so-called peak-over-threshold (POT), or exceedance, of heavy-tailed data  $\varepsilon_t$  over a predetermined threshold  $\tau$ , and  $\delta_t > 0$  and  $\xi_t > 0$  are the scale and tail shape parameter of the GPD, respectively. Most continuous distributions used in statistics and the actuarial sciences lie in the Maximum Domain of Attraction (MDA) of the GPD (see McNeil et al., 2010, Chapter 7.1), meaning that they allow for the above tail shape approximation. By focusing on the tail area directly using EVT arguments, we avoid having to make more ad-hoc assumptions on the parametric form of the tail.

The result in (2) is a limiting result. In any finite sample, the threshold  $\tau_t$  has to be set to a specific, finite value, such that the GPD approximation will be inexact and the distribution is in that sense misspecified. This will also be the case in our setting. The score-driven updates that we define later on for  $\xi_t$  and  $\delta_t$ , however, still ensure that the expected Kullback-Leibler divergence between the approximate GPD model and the true, unknown conditional distribution  $\mathbb{P} [\varepsilon_t \leq e_t + \tau | \varepsilon_t > \tau, \mathcal{F}_{t-1}]$  is improved every time for sufficiently small steps, even if the GPD model is misspecified; see Blasques et al. (2015). The choice of the threshold  $\tau$  is subject to a well-known bias-efficiency trade-off; see, for instance, McNeil and Frey (2000). In theory, the GPD tail approximation only becomes exact for  $\tau \to +\infty$ . A high threshold, however, also implies a smaller number of exceedances  $\varepsilon_t > \tau$ , and more estimation error for the parameters of the GPD. Common choices for  $\tau$  from the literature are the 90%, 95%, and 99% empirical quantiles of  $\varepsilon_t$ ; see Chavez-Demoulin et al. (2014). We return to the choice, and modeling, of the threshold further below.

A key step in (3) is that we use the conditional probabilities based on the information set  $\mathcal{F}_{t-1}$ . As a result, the tail shape parameters become time-varying. To capture this timevariation, we model  $(\xi_t, \delta_t)'$  using the score-driven (GAS) dynamics introduced by Creal et al. (2013) and Harvey (2013). In our time series setting, that implies that both  $\delta_t$  and  $\xi_t$  are measurable with respect to  $\mathcal{F}_{t-1}$ . We ensure positivity of  $\delta_t$  and  $\xi_t$  by using an (element-wise) exponential link function  $(\xi_t, \delta_t)' = \exp(f_t)$  for  $f_t = (f_t^{\xi}, f_t^{\delta})' \in \mathbb{R}^2$ .<sup>2</sup> The transition dynamics for  $f_t$  are given by so-called GAS(p, q)-dynamics as

$$f_{t+1} = \omega + \sum_{i=0}^{p-1} A_i s_{t-i} + \sum_{j=0}^{q-1} B_j f_{t-j},$$

$$s_t = \mathcal{S}_t \nabla_t, \qquad \nabla_t = \partial \ln p(x_t \mid \mathcal{F}_{t-1}; f_t, \theta) / \partial f_t,$$
(4)

where vector  $\omega = (\omega^{\xi}, \omega^{\delta})' = \omega(\theta)$  and matrices  $A_i = A_i(\theta)$  and  $B_j = B_j(\theta)$  depend on the deterministic parameter vector  $\theta$ , which needs to be estimated. The scaling matrix  $S_t$  may depend both on  $\theta$ ,  $f_t$ , and  $\mathcal{F}_{t-1}$ . Effectively, the recursion (4) updates  $f_t$  at every time point in time via a scaled steepest ascent step to improve the fit to the GPD. The score of (3) required in (4) is given by

$$\nabla_{t} = \begin{bmatrix} \xi_{t}^{-1} \cdot \log\left(1 + \xi_{t} \, \delta_{t}^{-1} x_{t}\right) - \left(1 + \xi_{t}^{-1}\right) \frac{\xi_{t} x_{t}}{\delta_{t} + \xi_{t} x_{t}} \\ \frac{x_{t} - \delta_{t}}{\delta_{t} + \xi_{t} x_{t}} \end{bmatrix},$$
(5)

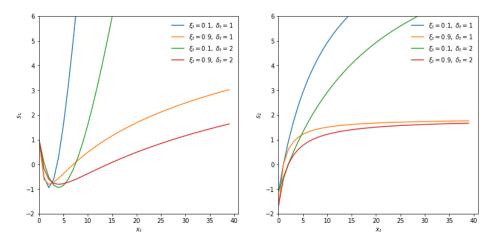
where  $\log(\cdot)$  denotes the natural logarithm; see Appendix A.1 for a derivation. We take  $A_i$  and  $B_j$  as diagonal matrices.

Following Creal et al. (2014) we select the square-root inverse conditional Fisher information of the conditional observation density to scale (5), i.e.,  $S_t = L'_t$ , with  $L_t$  the choleski decomposition of the inverse conditional Fisher information matrix  $\mathcal{I}_t = (L_t L'_t)^{-1} = \mathbb{E}[\nabla_t \nabla'_t]$ 

<sup>&</sup>lt;sup>2</sup>Given that  $\xi_t > 0 \forall t$ , (3) is also the cdf and pdf of a Pareto type-II distribution with two time-varying parameters  $\alpha_t = \xi_t^{-1}$  and  $\sigma_t = \delta_t \xi_t^{-1}$ .

#### Figure 1: News impact curves

The first element (left panel) and second element (right panel) of  $s_t$  in (7) is plotted against  $x_t$  for different values of  $\xi_t$  and  $\delta_t$ .



 $\mathcal{F}_{t-1}; f_t, \theta] = \mathbb{E}[-\partial \nabla_t / \partial f'_t \mid \mathcal{F}_{t-1}; f_t, \theta]$ , such that the conditional variance of  $s_t$  is equal to the unit matrix. For the GPD, we have

$$L_t = \begin{bmatrix} 1 + \xi_t^{-1} & 0\\ -1 & \sqrt{1 + 2\xi_t} \end{bmatrix},$$
 (6)

see Appendix A.2 for a derivation. Combining terms yields the scaled score as

$$s_{t} = L_{t}' \nabla_{t} = \begin{bmatrix} \xi_{t}^{-2} (1+\xi_{t}) \cdot \log\left(1+\xi_{t} \,\delta_{t}^{-1} x_{t}\right) + \frac{\delta_{t} - (\xi_{t}+3+\xi_{t}^{-1}) \cdot x_{t}}{\delta_{t}+\xi_{t} x_{t}} \\ \sqrt{1+2\xi_{t}} \frac{x_{t} - \delta_{t}}{\delta_{t}+\xi_{t} x_{t}} \end{bmatrix}.$$
 (7)

Though the scaled score in (7) seems unstable at first sight for  $\xi_t$  near zero, the expression actually has a finite limit equal to  $\lim_{\xi_t \downarrow 0} s_{1,t} = 1 - 2\delta_t^{-1}x_t + \frac{1}{2}\delta_t^{-2}x_t^2$ .

Figure 1 plots the two elements of (7) as a function of  $x_t$  for different values of  $\xi_t$  and  $\delta_t$ . The behavior of the scaled score is intuitive: Large  $x_t$  imply that  $f_t$  is adjusted upwards. For high realization of  $x_t$  the adjustments are greatest when the current tail shape and tail scale are low. The function shapes become increasingly concave as  $x \to \infty$  in line with robust updates of the time-varying parameters. This distinguishes our current set-up sharply from an approach directly based on quantile functions; see Patton et al. (2019) and Catania and Luati (2019), in particular for risk measures such as ES. In Patton et al. (2019), ES reacts linearly to the VaR exceedance. This can result in noisy or unstable ES estimates. Using the GPD shape as emanating from EVT, Figure 1 shows that  $\xi_t$  and  $\delta_t$  react more modestly to large POT observations. This makes sense, as we expect such 'outliers' to occur more often for higher values of  $\xi_t$ . For extremely high  $\xi_t \geq 1$ , the ES even ceases to exist. We also note that small realizations of  $x_t$  imply downward adjustments of both elements of  $f_t$ , up to the point where  $x_t$  becomes very small. In that case  $f_t^{\xi}$  is adjusted upward, as observations near the center of a fat-tailed distribution signal increased peakedness (=leptokurtosis); see also Lucas and Zhang (2016). The score-driven steps in (7) can thus result in more stable and interpretable parameter paths due to the concavity of the news impact curves.

When there is no tail observation, i.e.  $x_t = \varepsilon_t - \tau \leq 0$ , then the new observation carries no information about  $\xi_t$  and  $\delta_t$ ; see McNeil et al. (2010, Chapter 7). In such cases we set the score to zero, and continue to use (4) to update  $f_t$ .<sup>3</sup> Long consecutive stretches of zero scores can lead to erratic paths for  $f_t$  and thus  $(\xi_t, \delta_t)$ . In addition, such stretches of zero scores can be problematic for inference on  $\theta$ ; see Blasques et al. (2018). Both issues can be addressed by taking into account lagged values of the scaled score via the exponentially-weighted moving average specification

$$f_{t+1} = \omega + A\tilde{s}_t + Bf_t,\tag{8}$$

where  $\tilde{s}_t = (1 - \lambda)s_t + \lambda \tilde{s}_{t-1}, \lambda \in (0, 1)$  is an additional parameter to be estimated, and  $s_t$ is given by (7). While  $s_t$  is most often zero,  $\tilde{s}_t$  is not. Clearly, (4) is a special case of (8) for  $\lambda \to 0$ . Specification (8) leads to a GAS(1,2) specification for  $f_t$ ,

$$(\mathbf{I}_2 - BL)(1-\lambda)^{-1}(1-\lambda L)f_{t+1} = \omega + As_t,$$

where L is the lag operator. To see this, first rewrite (8) to  $(I_2 - BL)f_{t+1} = \omega + A\tilde{s}_t$ , and then multiply both sides by  $(1 - \lambda L)/(1 - \lambda)$ , using  $(1 - \lambda L)\tilde{s}_t = (1 - \lambda)s_t$ . The smoothing

<sup>&</sup>lt;sup>3</sup>If  $\omega = 0$ ,  $B = I_2$ , and p = q = 1 in (4), then a zero score implies that both tail parameters retain their current values. We adopt this specification in Section 4 below.

approach in (8) is similar to the approach in Patton (2006) that uses up to ten lags of the driver (in our case the score) to smooth the dynamics of the time-varying parameter.

The transition equation for  $f_t$  can be extended further if additional conditioning variables are available. For example, central bank sovereign bond purchases may help explain the timevariation in the tail shape and tail scale parameters associated with changes in sovereign bond yields; see Section 4. Such additional variables can be taken into account in a straightforward way via the modified transition equation,

$$f_{t+1} = \omega + A\tilde{s}_t + Bf_t + C \cdot z_t, \tag{9}$$

where all explanatory variables are stacked into vector  $z_t$ , and C is a conformable matrix of impact coefficients that needs to be estimated.

We consider three different ways to set the relevant thresholds. The thresholds can be either time-invariant ( $\tau$ ) or time-varying ( $\tau_t$ ). The construction of the thresholds can be important in practice because  $\tau_t$  determines whether an observation lies in the tail, and, if so, what is the magnitude of the exceedance  $x_t = \varepsilon_t - \tau_t > 0$ . The  $\kappa$ -quantile  $Q_{1:T}^{\kappa}$  ({ $\varepsilon_1, \ldots, \varepsilon_T$ }) associated with the full sample is an obvious first candidate,  $\kappa \in (0, 1)$ . In this case,  $\tau =$  $Q_{1:T}^{\kappa}$  ({ $\varepsilon_1, \ldots, \varepsilon_T$ }) is time-invariant. Alternatively, we can compute the quantile recursively up to time t and set  $\tau_t = Q_{1:t}^{\kappa}$  ({ $\varepsilon_1, \ldots, \varepsilon_t$ }), such that  $\tau_t$  is time-varying. Finally, we consider a dynamic specification as suggested by Patton et al. (2019), according to which

$$\tau_{t+1} = \tau_t + a^{\tau} \cdot \left( 1\{\varepsilon_t > \tau_t\} - (1-\kappa) \right), \tag{10}$$

where  $a^{\tau}$  is a parameter to be estimated, and  $\tau_1 = Q_{1:T}^{\kappa}$  is used to initialize the process. The recursive specification (10) is a martingale since  $\mathbb{E}[1\{\varepsilon_t > \tau_t\} \mid \mathcal{F}_{t-1}, \theta] = (1 - \kappa)$ . The threshold  $\tau_t$  can now respond to changes in the underlying location, scale, and higher-order moments of  $\varepsilon_t$  in a straightforward way. This is particularly relevant if the data  $y_t$  is not pre-filtered based on an appropriate location–scale model in a first step, for instance if we set  $\mu_t = 0$  and  $\sigma_t = 1$  in (1), thus modeling the conditional extreme tail shape of  $y_t$  directly. We close this section with a brief comment on parameter interpretability. The tail shape parameter  $\xi_t$  can always be interpreted as observation  $y_t$ 's contemporaneous inverse tail index  $\alpha_t^{-1}$ . By contrast, the estimated scale parameter  $\delta_t$  need not have a straightforward interpretation in terms of  $y_t$ 's conditional variance. For example, assume that  $y_t$  were GPD distributed with time-varying tail shape parameter  $\alpha_t^{-1}$  and scale  $\sigma_t$ . We can then show that the derived POT  $x_t$  also has an exact GPD-distribution, with the same tail shape parameter  $\xi_t = \alpha_t^{-1}$ , but a different scale parameter  $\delta_{t,\tau} = \sigma_t + \alpha_t^{-1} \cdot \tau$ ; see Web Appendix B.1 for details. As a result,  $\delta_{t,\tau}$  increases with the threshold, varies positively with the tail shape parameter  $\xi_t$ , and, importantly, should not be expected to provide a consistent estimate of  $\sigma_t$ . A similar result can be derived if the time series data  $y_t$  were Student's t-distributed with scale  $\sigma_t$  and tail index  $\alpha_t$ ; see Web Appendix B.2. We return to this issue in our simulation Section 3, where we consider pseudo-true values of both parameters to benchmark how well the model can estimates these.

## 2.2 Confidence bands for tail shape and scale

Confidence (or standard error) bands allow us to visualize the impact of estimation uncertainty associated with the maximum likelihood estimate  $\hat{\theta}$  on the filtered estimates  $\hat{f}_t(\hat{\theta})$ , and, by extension, also  $(\hat{\xi}_t, \hat{\delta}_t)' = \exp(\hat{f}_t(\hat{\theta}))$ . Quantifying the uncertainty about these parameter paths is important, as classical EVT estimators of time-invariant tail shape parameters are already typically associated with sizeable standard errors; see e.g. Hill (1975) and Huisman et al. (2001). Our confidence bands are based on the variance of  $\hat{f}_t$ , which we denote  $V_t = \operatorname{Var}(\hat{f}_t)$ . There exist two possible ways to construct these bands. Delta-method-based bands can be devised using a linear approximation of the non-linear transition function for  $f_t$ , thus extending Blasques et al. (2016, Section 3.2) to the case of multiple lags. We provide the equations in Web Appendix C. In our empirical application below, however, the linear approximations are typically insufficient to capture the uncertainty in the highly non-linear dynamics for some countries. As a result, delta-method-based bands can become unstable. Therefore, we instead use simulation-based bands as in Blasques et al. (2016, Section 3.3).

Simulation-based confidence bands build on the asymptotic normality of  $\hat{\theta}$ . In particular,

we draw S parameter values  $\hat{\theta}^s$ ,  $s = 1, \ldots, S$  from the distribution  $N(\hat{\theta}, \hat{W})$ , where  $\hat{W}$  is the estimated covariance matrix of  $\hat{\theta}$ , e.g., a sandwich covariance matrix estimator. If the finitesample distribution of  $\hat{\theta}$  were known, that could be used instead. For each draw  $\hat{\theta}^s$  we now run the filter for  $f_t$  from t = 1 to t = T, thus obtaining S paths  $\hat{f}_t^s$ , for  $s = 1, \ldots, S$  and  $t = 1, \ldots, T$ . These paths account automatically for all non-linearities in the dynamics for  $f_t$ . The simulated bands can now be obtained directly by calculating the appropriate percentiles for each t over the S draws of the paths  $\hat{f}_t^s$  for  $s = 1, \ldots, S$ .

## 2.3 Parameter estimation

Parameter estimates can be obtained in a standard way by numerically maximizing the loglikelihood function. Observation-driven time series models such as (3) – (10) are attractive because the log-likelihood is known in closed form. For a given set of time series observations  $x_1, \ldots, x_T$ , the vector of unknown parameters  $\theta$  can be estimated by maximizing the loglikelihood function with respect to  $\theta$ . The average log-likelihood function is given by

$$\mathcal{L}(\theta|\mathcal{F}_{T}) = (T^{*})^{-1} \sum_{t=1}^{T} 1\{x_{t} > 0\} \cdot \ln p(x_{t}; \delta_{t}, \xi_{t})$$
$$= (T^{*})^{-1} \sum_{t=1}^{T} 1\{x_{t} > 0\} \cdot \left[ -\ln(\delta_{t}) - \left(1 + \frac{1}{\xi_{t}}\right) \ln \left(1 + \xi_{t} \frac{x_{t}}{\delta_{t}}\right) \right], \quad (11)$$

where  $T^* = \sum_{t=1}^{T} 1\{x_t > 0\}$  is the number of POT values in the sample. Maximization of (11) can be carried out using a conveniently chosen quasi-Newton optimization method.

Blasques et al. (2020) provide conditions under which the maximum likelihood estimator of  $\theta$  is consistent and asymptotically normally distributed within the class of correctlyspecified score-driven models. They also prove that (quasi-)maximum likelihood estimation of  $\theta$  can remain consistent (to pseudo-true values) and asymptotically normal even if the score-driven model is misspecified in terms of  $\ln p(x_t; f_t)$ . This is reassuring since the GPD is never exact for any finite value of  $\tau < \infty$ . In the presence of misspecification, score updates continue to minimize the local Kullback-Leibler divergence between the true conditional density and the model-implied conditional density, and remain optimal in this sense; see Blasques et al. (2015). The asymptotic covariance matrix  $W = \text{Var}(\hat{\theta})$  then takes its usual sandwich form; see e.g. Davidson and MacKinnon (2004, Ch. 10) and Blasques et al. (2020).

The autoregressive parameter  $a^{\tau}$  in (10) cannot be estimated using (11). Another objective function is needed in this case. We suggest using the average quantile regression check function of Koenker (2005, Ch. 3). The optimization problem can be formulated as

$$\min_{\{a^{\tau}\}} T^{-1} \sum_{t=1}^{T} \rho_{\kappa} \left(\epsilon_{t} - \tau_{t}\right) \iff \min_{\{a^{\tau}\}} T^{-1} \sum_{t=1}^{T} \left(\epsilon_{t} - \tau_{t}\right) \left(\kappa - 1\{\epsilon_{t} < \tau_{t}\}\right) \\
\iff \max_{\{a^{\tau}\}} T^{-1} \sum_{t=1}^{T} \left(\epsilon_{t} - \tau_{t}\right) \left((1 - \kappa) - 1\{\epsilon_{t} > \tau_{t}\}\right),$$
(12)

where  $\rho_{\kappa}(u_t) = u_t (\kappa - 1\{u_t < 0\})$ , and  $\tau_t$  evolves as in (10). See also Engle and Manganelli (2004) and Catania and Luati (2019) for the use of this objective function in a different dynamic context. In practice, we estimate all thresholds  $\tau_t$  via (12) before maximizing (11).<sup>4</sup>

## 2.4 A conditional location–scale–df model

This section introduces a score-driven location-scale-df model that can be used to pre-filter univariate time series data  $y_t$  that is arbitrarily fat-tailed, where df denotes the degrees of freedom. The model modifies the setting of Lucas and Zhang (2016) with a Student's t distribution with time-varying volatility and degrees of freedom parameters to a setting that also allows for a time-varying location  $\mu_t$  parameter and to more extreme tails ( $\nu_t < 2$ ), in which case the volatility no longer exists, but a time varying scale parameter  $\sigma_t > 0$  does exist. Since all parameters are time-varying, using this model minimizes the risk of mistaking time-variation in the center of the distribution for time-variation in the tail, and vice versa. The restriction  $\nu_t > 0$  aligns closely with the assumption  $\alpha_t > 0$  and  $\xi_t > 0$  in Section 2.1.

<sup>&</sup>lt;sup>4</sup>Numerical gradient-based optimizers, such as e.g. MaxBFGS, may only indicate weak convergence at the optimum of (12). This is due to the piecewise linear objective function. The optimizer at hand may not be suited for such a function, and will end up in a kink. This is not a problem, assuming we are not interested in standard errors for  $a^{\tau}$ . Alternatively the interior point algorithm of Koenker and Park (1996) could be used.

For the purposes of pre-filtering, in this section  $y_t$  is assumed to be generated by

$$y_t \sim t(y_t; \mu_t, \sigma_t, \nu_t), \tag{13}$$

where  $\mu_t = \mathbb{E}[y_t | \mathcal{F}_{t-1}]$  if  $\nu_t > 1$ , and  $\sqrt{\nu_t/(\nu_t - 2)} \sigma_t$  is the conditional volatility of  $y_t$  if  $\nu_t > 2$ . All time-varying parameters are modeled in a score-driven way as

$$\mu_{t+1} = \omega^{\mu} + a^{\mu}s_t^{\mu} + b^{\mu}\mu_t + c^{\mu}z_t + d^{\mu}y_t, \qquad (14)$$

$$\ln \sigma_{t+1} = \omega^{\sigma} + a^{\sigma} s_t^{\sigma} + b^{\sigma} \ln \sigma_t + c^{\sigma} z_t + d^{\sigma} \mathbb{1}\{y_t > \mu_t\} s_t^{\text{Lev}},\tag{15}$$

$$\nu_{t+1} = \omega^{\nu} + a^{\nu} s_t^{\nu} + b^{\nu} \nu_t + c^{\nu} z_t, \tag{16}$$

where  $\omega^{(\cdot)}$ ,  $a^{(\cdot)}$ ,  $b^{(\cdot)}$ ,  $c^{(\cdot)}$ , and  $d^{(\cdot)}$  are scalar parameters to be estimated, and  $z_t$  is a vector of additional conditioning variables which may be available. The required scaled scores are

$$s_t^{\mu} = \frac{(\nu_t + 3)(y_t - \mu_t)}{\nu_t + \sigma_t^{-2}(y_t - \mu_t)^2},\tag{17}$$

$$s_t^{\sigma} = \frac{\nu_t + 3}{2\nu_t} \cdot \left( \frac{(\nu_t + 1)(y_t - \mu_t)^2}{\nu_t \sigma_t^2 + (y_t - \mu_t)^2} - 1 \right),\tag{18}$$

$$s_{t}^{\nu} = \frac{1}{2} \left[ \frac{\nu_{t}}{4} \gamma'' \left( \frac{\nu_{t}+1}{2} \right) - \frac{\nu_{t}}{4} \gamma'' \left( \frac{\nu_{t}}{2} \right) + \frac{1}{2} \frac{\nu_{t}+5}{(\nu_{t}+1)(\nu_{t}+3)} \right]^{-1} \\ \left[ \frac{1}{\nu_{t}} + \gamma' \left( \frac{\nu_{t}}{2} \right) - \gamma' \left( \frac{\nu_{t}+1}{2} \right) + \ln \left( 1 + \frac{(y_{t}-\mu_{t})^{2}}{\nu_{t}\sigma_{t}^{2}} \right) - \frac{\nu_{t}+1}{\nu_{t}} \frac{(y_{t}-\mu_{t})^{2}}{\nu_{t}\sigma_{t}^{2} + (y_{t}-\mu_{t})^{2}} \right], \quad (19)$$

where the functions  $\gamma'(x)$  and  $\gamma''(x)$  are the first and second derivatives of the log-gamma function. We refer to Web Appendix D for a derivation of (17) - (19).

The "leverage" term  $d^{\sigma} \cdot 1\{y_t > \mu_t\}s_t^{\text{Lev}}$  in (15) allows  $\ln \sigma_{t+1}$  to be higher (or lower, depending on the sign of  $d^{\sigma}$ ) when  $y_t$  is above its location  $\mu_t$ . The term  $s_t^{\text{Lev}} = s_t^{\sigma}(y_t) - s_t^{\sigma}(\mu_t)$ is constructed such that the score is continuous at  $\mu_t$ . Leverage specifications are often found to be valuable in many empirical applications; see e.g. Engle and Patton (2001). The deterministic parameters in (14) – (16) can be estimated by (quasi-)maximum likelihood methods in line with the discussion in Section 2.3.

## 2.5 Market risk measures

Market risk measurement is a major application of EVT methods in practice; see Manganelli and Engle (2004) and McNeil et al. (2010). We consider the conditional VaR and conditional ES as measures of one-step-ahead market risk. The GPD approximation (2) – (3) yields useful closed-form estimators of the VaR and ES for high upper quantiles  $\gamma > G(\tau | \mathcal{F}_{t-1})$ ; see McNeil and Frey (2000) and Rocco (2014). We can estimate the  $1 - \gamma$  tail probability of  $y_t$  based on the GPD cdf for  $x_t$ , obtaining

$$\operatorname{VaR}^{\gamma}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta) = \tau_{t} + \delta_{t} \xi_{t}^{-1} \left[ \left( \frac{1-\gamma}{t^{*}/t} \right)^{-\xi_{t}} - 1 \right],$$
$$\operatorname{VaR}^{\gamma}(y_{t} \mid \mathcal{F}_{t-1}, \theta) = \mu_{t} + \sigma_{t} \operatorname{VaR}^{\gamma}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta),$$
(20)

where  $\mu_t$  and  $\sigma_t$  are defined below (1), and  $t^*$  is the number of observations of  $x_t > 0$  up to time t, i.e., the number of observations  $y_s$  for  $s = 1, \ldots, t$  for which  $y_s > \tau_s$ . Put differently,  $t^*/t$  is an estimator of the tail probability  $\kappa_t = G(\tau_t \mid \mathcal{F}_{t-1})$ .

The conditional ES is the average conditional VaR in the tail across all quantiles  $\gamma$  (see McNeil et al., 2010, Chapter 2), provided  $\xi_t < 1$ . The closed-form expressions are

$$\mathrm{ES}^{\gamma}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta) = \frac{1}{1 - \gamma} \int_{\gamma}^{1} \mathrm{VaR}^{\tilde{\gamma}}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta) \mathrm{d}\tilde{\gamma}$$

$$= \frac{\mathrm{VaR}^{\gamma}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta)}{1 - \xi_{t}} + \frac{\delta_{t} - \xi_{t}\tau_{t}}{1 - \xi_{t}},$$

$$\mathrm{ES}^{\gamma}(y_{t} \mid \mathcal{F}_{t-1}, \theta) = \mu_{t} + \sigma_{t} \mathrm{ES}^{\gamma}(\epsilon_{t} \mid \mathcal{F}_{t-1}, \theta);$$

$$(21)$$

see Web Appendix E for a derivation of (20) - (21). The  $\mathrm{ES}^{\gamma}(y_t|\cdot)$  is strictly higher than the  $\mathrm{VaR}^{\gamma}(y_t|\cdot)$  at the same confidence level, as it "looks further into the tail." It can be shown that the ratio  $\mathrm{ES}^{\gamma}(y_t|\cdot)/\mathrm{VaR}^{\gamma}(y_t|\cdot)$  increases monotonically in  $\xi_t$  for  $\gamma \to 1$ , indicating that expected losses beyond the VaR become increasingly worse for heavier-tailed (higher  $\xi_t$ ) distributions. Maximum likelihood estimators of the conditional VaR and conditional ES can be obtained by inserting filtered estimates of  $\mu_t$ ,  $\sigma_t$ ,  $\xi_t$  and  $\delta_t$  into (20) and (21).

For later reference, the sensitivity of VaR<sup> $\gamma$ </sup>( $y_t$ ) to bond purchases  $z_{t-1}$  is given by

$$\frac{\mathrm{dVaR}^{\gamma}(y_t)}{\mathrm{d}z_{t-1}} = \frac{\partial \mathrm{VaR}}{\partial \mu_t} \frac{\mathrm{d}\mu_t}{\mathrm{d}z_{t-1}} + \frac{\partial \mathrm{VaR}}{\partial \sigma_t} \frac{\mathrm{d}\sigma_t}{\mathrm{d}\ln\sigma_t} \frac{\mathrm{d}\ln\sigma_t}{\mathrm{d}z_{t-1}} + \frac{\partial \mathrm{VaR}}{\partial \delta_t} \frac{\mathrm{d}\delta_t}{\mathrm{d}f_t^{\delta}} \frac{\mathrm{d}f_t^{\delta}}{\mathrm{d}z_{t-1}} + \frac{\partial \mathrm{VaR}}{\partial \xi_t} \frac{\mathrm{d}\xi_t}{\mathrm{d}f_t^{\xi}} \frac{\mathrm{d}f_t^{\xi}}{\mathrm{d}z_{t-1}}.$$

The expression is intuitive: extreme upper quantiles can change if bond purchases  $z_{t-1}$  affect the conditional location  $\mu_t$ , the conditional scale  $\sigma_t$ , the tail scale  $\delta_t$ , or the tail shape  $\xi_t$ . The derivative is given by

$$\frac{\mathrm{d}\mathrm{VaR}^{\gamma}(y_{t})}{\mathrm{d}z_{t-1}} = c^{\mu} + \sigma_{t}\mathrm{VaR}^{\gamma}(\epsilon_{t})c^{\sigma} + \sigma_{t}\left(\mathrm{VaR}^{\gamma}(\epsilon_{t}) - \tau_{t}\right)c^{\delta} \\ -\sigma_{t}\left\{\mathrm{VaR}^{\gamma}(\epsilon_{t}) - \tau_{t} + \delta_{t}\left(\frac{1-\gamma}{t^{*}/t}\right)^{-\xi_{t}}\ln\left(\frac{1-\gamma}{t^{*}/t}\right)\right\}c^{\xi},$$
(22)

where  $\mu_t$  and  $\sigma_t$  are given by (14) and (15),  $f_t^{\xi}$  and  $f_t^{\delta}$  are given by (9) with  $C = (c^{\delta}, c^{\xi})'$ .

# 3 Simulation study

This section studies the question whether our score-driven modeling approach can reliably recover the time series variation in tail shape and tail scale in a variety of potentially challenging settings. In addition, we are interested in how to best choose the thresholds  $\tau_t$ , as well as the accuracy of EVT-based market risk measures when used in combination with our modeling approach.

## 3.1 Simulation design

Our simulation design considers D = 2 different densities (GPD and t), P = 4 different parameter paths for tail shape and tail scale, and H = 3 different ways to obtain the appropriate thresholds  $\tau_t$ . This yields  $2 \times 4 \times 3 = 24$  simulation experiments. In each experiment, we draw S = 100 univariate simulation samples of length T = 25,000. We focus on the upper  $1 - \kappa = 5\%$  tail. As a result, approximately  $25,000 \cdot 0.05 = 1,250$  observations are available in each simulation to compute informative POTs  $x_t > 0$ . The time series dimension T is chosen to resemble that of the empirical data considered in Section 4. **GPD and t-densities:** We first simulate  $y_t$  from a GPD distribution with time-varying tail shape  $\alpha_t^{-1}$  and tail scale  $\sigma_t$ ,  $y_t \sim \text{GPD}(\alpha_t^{-1}, \sigma_t)$ . We then consider a Student's *t* distribution with time-varying scale  $\sigma_t$  and degrees of freedom  $\alpha_t$ ,  $y_t \sim t(0, \sigma_t, \alpha_t)$ . POT values  $x_t$  are obtained as  $x_t = y_t - \tau_t$ .

**Parameter paths:** We consider four different paths for the tail shape  $\alpha_t^{-1}$  and tail scale  $\sigma_t$  parameters. For both GPD and t densities we consider

- (1) Constant:  $\alpha_t^{-1} = 0.5, \, \sigma_t = 1;$
- (2) Sine and constant:  $\alpha_t^{-1} = 0.5 + 0.3 \sin(4\pi t/T), \ \sigma_t = 1;$
- (3) Slow sine and frequent sine:  $\alpha_t^{-1} = 0.5 + 0.3 \sin(4\pi t/T), \ \sigma_t = 1 + 0.5 \sin(16\pi t/T);$
- (4) Synchronized sines:  $\alpha_t^{-1} = 0.5 + 0.3 \sin(4\pi t/T), \ \sigma_t = 1 + 0.5 \sin(4\pi t/T).$

Path (1) considers the special case of time-invariant tail shape and scale parameters. Naturally, we would want our dynamic framework to cover constant parameters as a special case. Path (2) allows the tail shape to vary considerably between 0.2 and 0.8, while keeping the scale (volatility) of the data constant. This parameter path corresponds to the empirical practice of working with volatility pre-filtered data. Path (3) stipulates that both parameters vary over time. Finally, Path (4) considers the case of synchronized variation in both parameters. This setting may be particularly challenging for two reasons. First, the tail observations occur most frequently when both tail shape and scale are high, making it potentially difficult to disentangle the two effects. Second, less information about the tail is available when both parameters are low simultaneously.

**Different thresholds:** We consider three thresholds  $\tau_t$ . First, we use the true time-varying 95%-quantile based on our knowledge of the true density and of  $\alpha_t$  and  $\sigma_t$ . This constitutes an infeasible best benchmark. Second, we construct  $\tau_t$  as the 95%-quantile of the expanding window of data up to time t, i.e.  $\tau_t = Q_{1:t}^{0.95} (\{\varepsilon_1, \ldots, \varepsilon_t\})$ . Finally, we use the recursive specification (10), with  $a^{\tau}$  fixed at 0.25, and initialized at  $\tau_1 = Q_{1:T}^{0.95}$ .

**Evaluation metrics:** Our main metric for evaluating model performance is the root mean squared error RMSE =  $\frac{1}{S} \sum_{s=1}^{S} \sqrt{\frac{1}{T} \sum_{t=1}^{T} (\hat{\xi}_{st} - \bar{\xi}_{st})^2}$ , where  $\hat{\xi}_{st}$  is the estimated tail

shape parameter in simulation s,  $\bar{\xi}_{st}$  is the corresponding (pseudo-)true tail shape,  $s = 1, \ldots, S$  denotes the simulation run, and  $t = 1, \ldots, T$  is the number of observations in each draw. The RMSE for the tail scale parameter  $\delta_t$  is obtained analogously, RMSE =  $\frac{1}{S}\sum_{s=1}^{S} \sqrt{\frac{1}{T}\sum_{t=1}^{T} (\hat{\delta}_{st} - \bar{\delta}_{st})^2}$ , where  $\bar{\delta}_{st}$  denotes the pseudo-true value of  $\delta_{st}$ . The pseudo-true values  $\bar{\xi}_{st}$  and  $\bar{\delta}_{st}$  are obtained by numerically minimizing the Kullback-Leibler divergence between the GPD and the data generating process beyond the true time-varying 95% quantile  $\tau_t$ . As the true conditional density is known at all times in a simulation setting, these pseudo-true benchmarks are easily computed. We note that particularly the GPD scale parameter  $\bar{\delta}_t$  may have very different dynamics from  $\sigma_t$ , as it combines dynamics in  $\alpha_t$  and  $\sigma_t$  via the EVT limiting expression in (2).

## 3.2 Simulation results

Table 1 presents root mean squared error (RMSE) statistics for tail shape  $\hat{\xi}_{s,t}$ , tail scale  $\hat{\delta}_{s,t}$ , and Value-at-Risk  $\widehat{\text{VaR}}_{s,t}$  estimates. Figures F.1 and F.2 in Web Appendix F.1 compare median estimated parameter paths for  $\hat{\xi}_t$ ,  $\hat{\xi}_t$ ,  $\widehat{\text{VaR}}^{0.99}$ , and  $\widehat{\text{ES}}^{0.99}$  to their (pseudo-)true values. Figure 2 is a representative example of the simulation outcomes when  $y_t$  is generated by a Student's t distribution.

We focus on three main findings. First, all models seem to work well in recovering the true underlying  $\xi_t$  and  $\delta_t$  dynamics. The median estimates in Figures F.1 and F.2 tend to be close to their (pseudo-)true values. Particularly the sometimes highly non-linear patters of  $\delta_t$  are recovered well. The model also captures well the peaks of  $\xi_t$ , so the fattest tails. The model needs some time to recognize that the extreme tail has become more benign, i.e., that  $\xi_t$  has gone down. The good fit is corroborated by Table 1. Both estimation methods for  $\tau_t$  only loose about 10% RMSE for  $\xi_t$  and  $\delta_t$  compared to the use of the true (infeasible)  $\tau_t$ .

Second, when comparing the recursive estimate  $\hat{\tau}_t$  versus the dynamic  $\tau_t^*$  of Patton et al. (2019) in Table 1, differences are mostly small and insignificant. If there is no time-variation (path (1)), the recursive estimate does slightly better, as expected. The converse is true for  $\delta_t$  if the true parameters vary over time.

#### Table 1: Simulation RMSE results

Root mean squared error (RMSE) statistics for two different distributions (GPD and t, in columns) and for four different parameter paths for tail shape  $\xi_t$  and tail scale  $\delta_t$  (paths (1) – (4), in rows). Thresholds  $\tau_t$ ,  $\hat{\tau}_t$ , and  $\hat{\tau}_t^*$  denote *i*) the infeasible true time-varying threshold, *ii*) the empirical quantile associated with an expanding window of observations  $y_1, \ldots, y_t$ , and *iii*) the estimated conditional quantile using (12) with  $a^{\tau} = 0.25$ , respectively. We consider 100 simulations for each DGP, and a time series of 25,000 observations in each simulation. Model performance is measured by the RMSE from the true  $\bar{\xi}_t$  and  $\bar{\delta}_t$  in each draw. For VaR, model performance is measured in relative terms as RMSE rescaled by the squared VaR<sub>t</sub>.

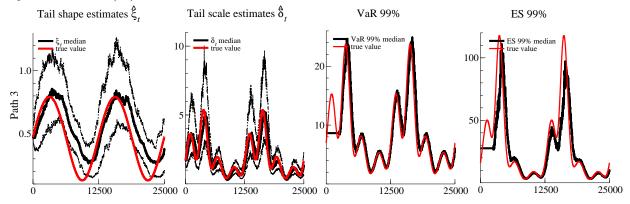
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Model	$\operatorname{GPD}(\tau_t)$	$\text{GPD}(\hat{\tau}_t)$	$\operatorname{GPD}(\hat{\tau}_t^*)$	$t(\tau_t)$	$t(\hat{\tau}_t)$	$t(\hat{\tau}_t^*)$		
	(infeasible)	(infeasible)						
	RMSE $\hat{\xi}_{s,t}$							
(1)	0.000	0.000	0.000	0.000	0.000	0.000		
( )	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)		
(2)	0.171	0.177	0.178	0.182	0.188	0.189		
	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)		
(3)	0.182	0.188	0.189	0.190	0.197	0.197		
	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)		
(4)	0.177	0.186	0.183	0.188	0.195	0.192		
	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)		
			RMSE	$\hat{\delta}_{s,t}$				
(1)	0.005	0.014	0.068	0.005	0.010	0.034		
	(0.003)	(0.006)	(0.013)	(0.002)	(0.004)	(0.006)		
(2)	1.646	1.774	1.753	0.580	0.589	0.588		
	(0.034)	(0.040)	(0.036)	(0.013)	(0.012)	(0.013)		
(3)	2.421	2.913	2.813	0.836	0.960	0.924		
	(0.054)	(0.054)	(0.049)	(0.015)	(0.020)	(0.017)		
(4)	2.608	2.904	2.844	0.925	0.970	0.964		
	(0.057)	(0.059)	(0.059)	(0.020)	(0.020)	(0.022)		
	$\text{RMSE }\widehat{\text{VaR}}_{s,t}$							
(1)	0.001	0.003	0.016	0.124	0.124	0.149		
	(0.001)	(0.002)	(0.003)	(0.001)	(0.001)	(0.002)		
(2)	0.924	0.987	0.964	0.249	0.243	0.257		
. /	(0.027)	(0.032)	(0.031)	(0.003)	(0.003)	(0.003)		
(3)	1.063	1.304	1.209	0.322	0.344	0.349		
	(0.025)	(0.041)	(0.033)	(0.004)	(0.005)	(0.004)		
(4)	1.020	1.120	1.083	0.302	0.297	0.319		
	(0.027)	(0.028)	(0.028)	(0.003)	(0.003)	(0.003)		

Third, Figure 2 as well as Figures F.1 and F.2 in Web Appendix F.1 corroborate that our EVT-based market risk measures, such as VaR and ES at a high confidence level  $\gamma = 0.99$ , tend to be estimated sufficiently accurately when used in combination with our modeling approach. The low and high frequency dynamics of the VaR and ES are both captured well. There only appears some under-estimation of the ES at its very peak where tails are extremely fat. Overall, we conclude that the model captures well the dynamics of the

### Figure 2: Simulation results: a representative example

Time series data is here generated as  $y_t \sim t(0, \sigma_t, \alpha_t)$ , where  $\alpha_t^{-1} = 0.5 + 0.3 \sin(4\pi t/T)$  and  $\sigma_t = 1 + 0.5 \sin(16\pi t/T)$ . This is Path 3 in Section 3.1. Pseudo-true parameter values are reported in solid red. The four panels report estimates of  $\xi_t$ ,  $\delta_t$ ,  $\operatorname{VaR}_t$ , and  $\operatorname{ES}_t$ , respectively. Median filtered values are plotted in solid black. The first two panels also indicate the lower 5% and upper 95% quantiles of the estimates (black dots). The time-varying threshold  $\hat{\tau}_t$  is estimated based on the recursive specification (10) in conjunction with the objective function (12).



tails, even if the model does not coincide with the data generating process and is therefore misspecified.

## 4 The tail impact of Eurosystem asset purchases

## 4.1 Data

#### 4.1.1 High-frequency data on bond yields

We obtain high-frequency data on changes in euro area sovereign bond yields from Thomson Reuters/Datastream, focusing on Spanish (EN), Greek (GR), Irish (IE), Italian (IT), and Portuguese (PT) five-year sovereign benchmark bonds. These market segments were among the most affected by the euro area debt crisis; see e.g. ECB (2014). SMP bond purchases undertaken during the debt crisis predominantly targeted the two- to ten-year maturity bracket, with the five-year maturity approximately in the middle of that spectrum. We focus on the impact on five-year benchmark bonds for this reason. We model the midpoint between ask and bid prices. Bond prices are expressed in yields-to-maturity and are obtained from continuous dealer quotes. Our sample ranges from 04 January 2010 to 31 December 2012, covering the most intense phase of the euro area sovereign debt crisis. The bond yields are sampled at the 15-minute frequency between 8AM and 6PM. Following Ghysels et al. (2017) we do not consider overnight changes in yield, such that the first 15-minute interval covers 8AM to 8:15AM. This yields 40 intra-daily observations per trading day. This yields 40 intra-daily observations per day, with  $T \approx 3 \times 260 \times 40 \approx 31,000$  observations per country.

The Greek data are an exception. Greek bonds experienced a credit event on 09 March 2012. In January and February 2012 the five-year benchmark bond continued trading, infrequently and at low prices, until approximately one week before the credit event. Our Greek data sample ends on 02 March 2012 for this reason. We include the Greek pre-default data as a truly extreme case, allowing us to "stress-test" our EVT estimation methodology.

Figure F.3 in the Web Appendix F.2 plots the yield-to-maturity of our five benchmark bond yields in levels and in first differences. All five yields exhibited large and sudden moves, leading to volatility clustering and extreme realizations of yield changes during the euro area sovereign debt crisis.

Table 2 provides summary statistics for changes in our five benchmark bond yields sampled at the 15-minute frequency. All time series have significant non-Gaussian features under standard tests and significance levels. In particular, we note the non-zero skewness and large values of kurtosis for almost all time series in the sample. Yield changes are covariance stationary according to standard unit root (ADF) tests. Most yield changes are below one bps in absolute value. This suggests that the data are not only heavy-tailed, but also extremely peaked around zero in the center. The pronounced non-Gaussian data features strongly suggest a non-Gaussian empirical framework for modeling conditional location, dispersion, and higher-order moments.

#### 4.1.2 High–frequency data on Eurosystem bond purchases

We study the impact of SMP bond purchases between 2010 and 2012 for five euro area countries: Greece, Ireland, Italy, Portugal, and Spain. At the end of our sample, the Eurosystem held  $\in$ 99.0 bn in Italian sovereign bonds,  $\in$ 30.8 bn in Greek debt,  $\in$ 43.7 bn in Spanish debt,

#### Table 2: Data descriptive statistics

Summary statistics for changes in five-year sovereign benchmark bond yields measured in percentage points. Columns labeled EN, GR, IE, IT, and PT refer to Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bond yields. The sample ranges from 04 January 2010 to 28 December 2012. The Greek sample ends on 02 March 2012. Reported p-values for skewness and kurtosis refer to D'Agostino et al. (1990)'s test. The last row reports the fraction of yield changes smaller than one basis point in absolute value.

	EN	GR	IE	IT	PT
Median	0.00	0.00	0.00	0.00	0.00
Std. dev.	0.02	0.46	0.06	0.03	0.08
Minimum	-0.74	-20.73	-0.91	-0.39	-1.15
Maximum	0.47	14.77	1.45	0.43	1.20
Skewness	-42.29	-104.76	34.11	14.91	12.40
Skew. p-value	0.00	0.00	0.00	0.00	0.00
Kurtosis	357.94	195.05	301.26	293.40	279.44
Kurt. p-value	0.00	0.00	0.00	0.00	0.00
Fraction $y_t < 1$ bp	81%	77%	81%	81%	77%

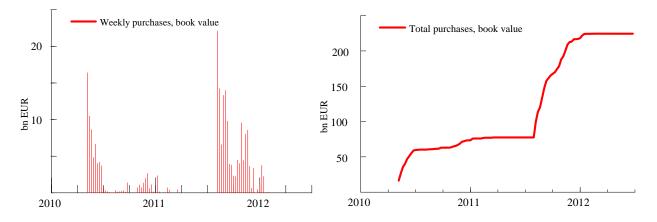
 $\in$ 21.6 bn in Portuguese debt, and  $\in$ 13.6 bn in Irish bonds; see the ECB (2013)'s Annual Report. The SMP's daily cross-country breakdown of the purchase data is still confidential at the time of writing. We use the country-specific data on SMP purchases when studying the impact of the program.

The SMP had the objective of helping to restore the monetary policy transmission mechanism by addressing the malfunctioning of certain government bond markets. The SMP consisted of interventions in the form of outright secondary market purchases. Implicit in the concept of malfunctioning markets is the notion that government bond yields can be unjustifiably high and volatile.

Figure 3 plots weekly total SMP purchases across countries as well as their accumulated book value over time. Approximately  $\in$ 214 billion (bn) of bonds were acquired within the SMP between 2010 and early 2012. The SMP was announced on 10 May 2010 and initially focused on Greek, Irish, and Portuguese debt securities. The program was extended to include Italian and Spanish bonds on 8 August 2011. The SMP was replaced by the Outright Monetary Transactions (OMTs) program on 6 September 2012; see Cœuré (2013). Visibly, the purchase data are unevenly spread over time. Between 10 May 2010 and Spring 2012 there are long periods during which the SMP was open but inactive.

#### Figure 3: Weekly and total SMP purchase amounts.

The figure plots the book value of settled SMP purchases as of the end of a given week. We report weekly purchases across countries (left panel) as well as the cumulative amounts (right panel). Maturing amounts are excluded.



The SMP purchase data are time-stamped, allowing us to construct time series data  $z_t$  of country-specific SMP purchases at the high (15-minute) frequency. The 15-minute frequency is chosen because 15 minutes is the regulatory limit for the recording of trades by the Eurosystem. Observations  $z_t$  contain *all* sovereign bond purchases at par (nominal) value between t - 1 and t for the respective country, not only purchases of the five-year benchmark bond.

## 4.2 Location–scale–df model estimates

This section applies our novel location–scale–df model of Section 2.4 to study changes in the yield-to-maturity of five-year sovereign benchmark bonds as discussed in Section 4.1.1. We are particularly interested in each series' location, scale, and degrees of freedom, and how these respond to Eurosystem bond purchases.

We apply the model to the raw data series after removing a (negligible) intra-daily pattern via dummy variable regression. We introduce two simplifications to the general specification. First, preliminary analyses suggest that the location parameters are approximately timeinvariant, such that  $a^{\mu}$  and  $b^{\mu}$  are close to zero. We proceed by imposing this restriction. Note that the specification for the mean still includes  $d^{\mu} \cdot y_{t-1}$  to accommodate a potentially

#### Table 3: Parameter estimates for the location-scale-df model

Parameter estimates for the univariate location–scale–df model (13). Rows labeled EN, GR, IE, IT, and PT refer to Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bond yields. The estimation sample ranges from 04 January 2010 to 28 December 2012 for all countries except Greece. Standard error estimates are in round brackets and are taken from a sandwich covariance matrix. P-values are provided in square brackets.

	EN	$\operatorname{GR}$	IE	IT	$\mathbf{PT}$
$\omega^{\mu}$	0.013	-0.038	0.003	-0.003	-0.016
	(0.007)	(0.024)	(0.005)	(0.007)	(0.006)
	[0.046]	[0.108]	[0.641]	[0.618]	[0.004]
$c^{\mu}$	-2.623	-2.856	0.017	-1.479	-0.053
(SMP)	(0.941)	(2.483)	(1.594)	(0.552)	(2.068)
. ,	[0.005]	[0.250]	[0.992]	[0.007]	[0.980]
$d^{\mu}$	-0.039	-0.000	-0.010	-0.029	-0.004
(AR1)	(0.007)	(0.000)	(0.002)	(0.010)	(0.001)
	[0.000]	[0.200]	[0.000]	[0.004]	[0.003]
$a^{\sigma}$	0.107	0.141	0.135	0.124	0.089
	(0.015)	(0.011)	(0.012)	(0.013)	(0.011)
	[0.000]	[0.000]	[0.000]	[0.000]	[0.000]
$c^{\sigma}$	-0.126	-0.055	-0.461	-0.049	-0.441
(SMP)	(0.089)	(0.115)	(0.324)	(0.050)	(0.228)
	[0.158]	[0.635]	[0.155]	[0.325]	[0.053]
$d^{\sigma}$	0.004	-0.004	-0.000	0.005	-0.000
(LEV)	(0.001)	(0.001)	(0.001)	(0.002)	(0.001)
	[0.006]	[0.001]	[0.885]	[0.002]	[0.641]
$a^{\nu}$	0.004	0.018	0.007	0.006	0.008
	(0.001)	(0.002)	(0.001)	(0.001)	(0.001)
	[0.000]	[0.000]	[0.000]	[0.000]	[0.000]
$c^{\nu}$	0.031	0.042	0.022	0.013	0.000
(SMP)	(0.014)	(0.027)	(0.035)	(0.007)	(0.028)
	[0.033]	[0.122]	[0.530]	[0.052]	[0.993]
loglik	-56226.2	-68788.4	-68584.7	-56218.6	-78164.0
AIC	112468.4	137592.9	137185.4	112453.2	156343.9
BIC	112534.9	137656.8	137252.0	112519.8	156410.6

negative serial correlation at the 15-minute frequency; see e.g. Roll (1984). Second, we find that the persistence  $(b^{\sigma} \text{ and } b^{\nu})$  in volatility and degrees of freedom parameters is very high. We therefore set  $\omega^{\sigma} = \omega^{\nu} = 0$  and  $b^{\sigma} = b^{\nu} = 1$ , thus adopting the EWMA restricted score dynamics of Lucas and Zhang (2016) for the scale and df parameters. A comparison of model selection criteria (AIC, BIC) across model specifications confirms these choices. With these simplifications in place, Table 3 now presents the parameter estimates.

We focus on three findings in Table 3. First, SMP bond purchases tended to lower the conditional location of future bond yields for most countries. The estimate of  $c^{\mu}$  is negative

for four out of five countries, and is statistically significantly negative for two of them. The estimated impacts for the two largest SMP countries, Italy and Spain, are -1.5 bps and -2.6 bps per  $\in$ 1 bn of purchases, respectively. The highest impact per  $\in$ 1 bn is observed for Greek bonds, at -2.9 bps per  $\in$ 1 bn of purchases. Greek bonds were the most illiquid at the time. The estimates of  $c^{\mu}$  for IE and PT are smaller in magnitude and not significant.<sup>5</sup> Since the yields are modeled in first differences and  $a^{\mu} = b^{\mu} = 0$ , these impacts are associated with long-lasting (permanent) changes in yield *levels*. Overall, our  $c^{\mu}$  estimates are in line with those obtained by Eser and Schwaab (2016) based on daily data and factor modeling techniques, and marginally smaller and less dispersed than those obtained by Ghysels et al. (2017) based on high-frequency data and VAR/GARCH modeling techniques.

Second, our parameter estimates for  $c^{\sigma}$  suggest a reduction in scale (volatility) following SMP bond purchases. The point estimates are all negative, although none are statistically significant at a 5% confidence level. Sizeable standard error estimates for  $c^{\sigma}$  are intuitive because the SMP intervention data is scarce even at the 15-minute frequency and the logscale is subject to pronounced time series variation.

Third, the point estimates of  $c^{\nu}$  are all positive, and statistically significant in one case (EN, with IT a borderline case). As a result, the time-varying degrees of freedom  $\nu_t$  tend to increase following SMP bond purchases, suggesting an increasingly "Gaussian" tail shape when the central bank is active as a buyer-of-last-resort. Taken together, the estimates of  $c^{\mu} < 0$ ,  $c^{\sigma} < 0$ , and  $c^{\nu} > 0$  suggest an overall beneficial, market-stabilizing impact of the bond purchases on sovereign bond yields.<sup>6</sup>

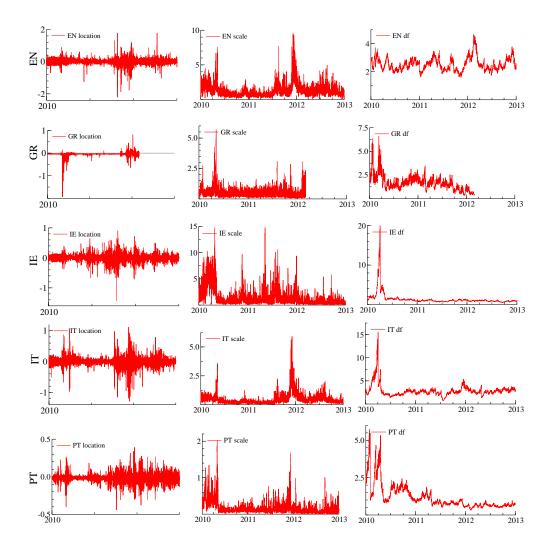
Figure 4.2 plots all time-varying parameters  $\mu_t$ ,  $\sigma_t$ , and  $\nu_t$ . The conditional location parameters  $\mu_t$  (left column) tend to be small and rarely exceed one bp in absolute value. The

<sup>&</sup>lt;sup>5</sup>If SMP purchases were more likely to occur following an increase in yields, then the impact estimates of Table 3 would constitute a lower bound to (the absolute value of) the true impact. This endogeneity is unlikely to be pronounced at the intra-daily frequency because the daily purchase volumes were predetermined before markets opened, constraining the latitude of central bank portfolio managers; see Eser and Schwaab (2016, Section 3.3) for a discussion.

<sup>&</sup>lt;sup>6</sup>The remaining parameter estimates in Table 3 can be interpreted as follows. The autoregressive coefficients  $d^{\mu}$  associated with lagged  $y_{t-1}$  are all negative. The implied negative autocorrelation is in line with severely illiquid markets for all five sovereign bonds during our sample; see Roll (1984). The intercept terms  $\omega^{\mu}$  are small and statistically different from zero only in two out of five cases (for EN and PT). The leverage terms  $d^{\sigma}$  are positive and statistically significant for EN and IT. In these cases an increase in yield has a greater influence on future log-scale than a decrease.

#### Figure 4: Filtered location, scale, and degrees of freedom parameters

Filtered location (first column), scale (second column) and degrees of freedom (third column) parameters associated with the location–scale–df model introduced in Section 2.4. Rows labeled EN, GR, IE, IT, and PT refer to Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bond yields. Greek bonds discontinued trading after 02 March 2012, and experienced a credit event on 09 March 2012.



observed time-variation is due to the inclusion of the lagged term  $y_{t-1}$  and bond purchases  $z_{t-1}$ . High values for the conditional scale  $\sigma_t$  (middle column) are visible for Greece, Ireland and Portugal in 2010, and for Spain and Italy in late 2011. The conditional df parameters  $\nu_t$  (right column) suggest that the conditional distribution is profoundly heavy-tailed, even after allowing for time-variation in the location and scale parameters. The df parameter associated with the Greek data declines almost monotonically until the credit event in March 2012.<sup>7</sup>

<sup>&</sup>lt;sup>7</sup>Quintos et al. (2001) and Lin and Kao (2018) propose Markov-Switching models for the tail index. The

#### Table 4: Parameter estimates

Parameter estimates for the extended (with SMP purchases  $z_t$ ) tail shape model. Columns labeled EN, GR, IE, IT, and PT refer to Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bond yields. The estimation sample ranges from 04 January 2010 to 28 December 2012 for all countries except Greece. Standard error estimates are in round brackets and are constructed from a sandwich covariance matrix. P-values are in square brackets.

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		EN	GR	IE	IT	PT
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$a^{\xi}$	0.006	0.032	0.021	0.055	0.026
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		(0.006)	(0.006)	(0.007)	(0.012)	(0.011)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		[0.291]	[0.000]	[0.005]	[0.000]	[0.023]
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$a^{\delta}$	0.027	0.144	0.078	0.027	0.103
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.007)	(0.026)	(0.014)	(0.006)	(0.015)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		[0.000]	[0.000]	[0.000]	[0.000]	[0.000]
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$c^{\xi}$	0.001	0.005	0.033	-0.009	-0.033
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.006)	(0.014)	(0.045)	(0.010)	(0.029)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		[0.847]	[0.705]	[0.467]	[0.376]	[0.258]
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$c^{\delta}$	-0.013	-0.031	0.060	-0.011	0.107
$a^{\tau}$ 0.0100.3120.1430.0270.263T3027921839307993051930719T*30032223309330413084loglik-102027.1-152861.1-226080.5-103050.5-306523.8AIC204062.1305730.2452168.9206109.0613055.7		(0.014)	(0.034)	(0.077)	(0.005)	(0.083)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		[0.344]	[0.362]	[0.433]	[0.036]	[0.196]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$a^{\tau}$	0.010	0.312	0.143	0.027	0.263
loglik         -102027.1         -152861.1         -226080.5         -103050.5         -306523.8           AIC         204062.1         305730.2         452168.9         206109.0         613055.7	T	30279	21839	30799	30519	30719
AIC 204062.1 305730.2 452168.9 206109.0 613055.7	$T^*$	3003	2223	3093	3041	3084
	loglik	-102027.1	-152861.1	-226080.5	-103050.5	-306523.8
BIC 204095.4 305762.2 452202.3 206142.3 613089.0	AIC	204062.1	305730.2	452168.9	206109.0	613055.7
	BIC	204095.4	305762.2	452202.3	206142.3	613089.0

The location-scale-df model (13) is not without drawbacks in our empirical setting. First, it makes an explicit distributional assumption that may or may not be appropriate. Second, it implicitly requires the tail impact of SMP purchases to be symmetric in the lower and upper tail. Since the Eurosystem acted only as a buyer-of-last-resort of bonds between 2010-2012, and has not sold any SMP bonds to date, it is not clear why that should be the case. The next section provides a semi-parametric perspective focussed on the extreme upper ("bad") tail.

### 4.3 Tail shape and tail scale estimates

This section discusses our time-varying tail shape  $(\xi_t)$  and tail scale  $(\delta_t)$  estimates associated with the extreme upper tail of changes in sovereign bond yields. We focus on results obtained

location–scale–df estimates reported in Figure 4.2 suggest that these may not be appropriate for our data at hand.

from pre-filtered data, where we used the fitted location-scale-df model from Section 4.2 to clean  $y_t$  from location and scale effects. Web Appendix G presents the analogous tail shape and scale estimates from raw bond yield data, allowing us to compare the two approaches; see Section 4.4. Our main results are based on POT observations  $x_t = (y_t - \hat{\mu}_t)/\hat{\sigma}_t - \hat{\tau}_t$  if  $(y_t - \hat{\mu}_t)/\hat{\sigma}_t > \hat{\tau}_t$  and  $x_t = missing$  otherwise, where  $\hat{\mu}_t$  and  $\hat{\sigma}_t$  are the location and scale estimates as reported in Figure 4.2, and where  $\hat{\tau}_t$  was obtained using the autoregressive specification (10) in conjunction with the objective function (12).

Preliminary analyses suggest that changes in the tail shape and scale parameters are highly persistent for our high-frequency data. We thus set  $\omega^{\xi} = \omega^{\delta} = 0$  and  $b^{\xi} = b^{\delta} = 1$ to simplify the model, again adopting the EWMA restricted score dynamics of Lucas and Zhang (2016) for these parameters. We also set the smoothing parameter  $\lambda = 0$ , see (7), given the absence of mean reversion in  $\ln \xi_t$  and  $\ln \delta_t$  at the 15-minute frequency.<sup>8</sup> We allow  $C \neq 0$  such that SMP bond purchases  $z_{t-1}$  can impact both  $\ln \xi_t$  and  $\ln \delta_t$  via their impact coefficients  $c^{\xi}$  and  $c^{\delta}$ . A comparison of unreported model selection criteria (AIC, BIC) across different model specifications supports these choices.

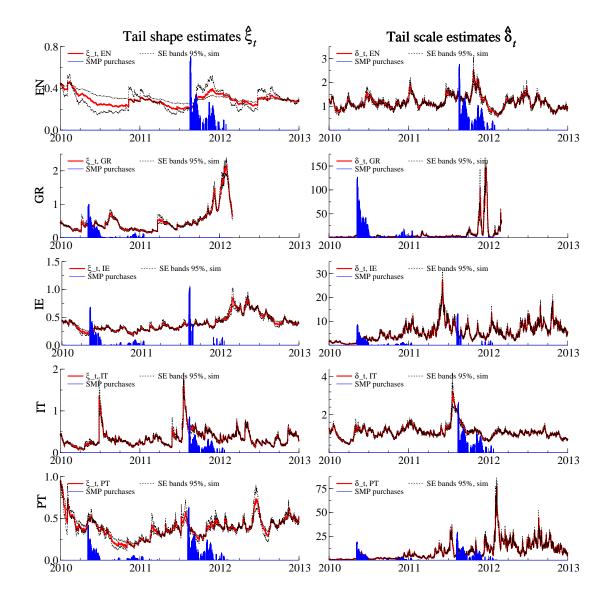
Table 4 presents tail shape estimates based on pre-filtered data. Parameters  $a^{\xi}$  and  $a^{\delta}$  can be interpreted as the standard deviations of the scores driving  $\ln \xi_t$  and  $\ln \delta_t$ , respectively; see the statements above (6). The associated estimates suggest pronounced time series variation in both parameters. The SMP impact parameters  $c^{\xi}$  are estimated negatively in two out of five cases, but are not statistically significant according to their t-values. Estimates of  $c^{\delta}$ are negative in three out of five cases, and are significantly negative in one case (IT). As a result, most of the tail impact of SMP purchases appears to have come about through its impact on the center of the distribution ( $\mu_t$ ,  $\sigma_t$ ) and not on its tail shape ( $\delta_t$ ,  $\xi_t$ ).

Figure 5 plots the corresponding filtered estimates for time-varying tail shape  $\xi_t$  and tail scale  $\delta_t$ . Blue bars indicate the approximate timing of SMP purchases in the respective markets. Time series variation is present and pronounced in both tail shape and tail scale parameters. The heaviest tail is estimated for Greek bonds during the weeks preceding the

<sup>&</sup>lt;sup>8</sup>The smoothing parameter  $\lambda$  is hard to estimate numerically given the absence of mean reversion in our high-frequency data. Fixing it to reasonable alternative values has little effect on our empirical findings.

#### Figure 5: Filtered tail shape and tail scale estimates

Filtered  $\xi_t$  and  $\delta_t$  estimates for Spanish (EN), Greek (GR), Irish (IE), Italian (IT), and Portuguese (PT) five-year sovereign benchmark bond yields between 2010 and 2012. The sample for Greek bonds is shorter as these bonds discontinued trading on 02 March 2012 and experienced a credit event on 09 March 2012. Standard error bands are simulated at a 95% confidence level. Blue bars indicate the approximate timing of SMP purchases in the respective markets. The SMP amounts are first aggregated over all five SMP countries, then smoothed using a centered one-week moving average. The resulting common time series is reported in the respective panel if the SMP was active for the respective market segment at the time; see Section 4.1.2 for the respective announcement days. The scaling of the purchase amounts is omitted and differs between left and right panels only for visibility.



### Table 5: Impact of €1 bn of SMP purchases on 97.5% VaR and 99.5% VaR

The table reports the impact of  $\leq 1$  bn of SMP bond purchases on the 97.5% and 99.5% VaR. The total impact is estimated as  $(1/\sum_{t}^{T} z_t) \sum_{t}^{T} (d\text{VaR}^{\gamma}(y_t)/dz_{t-1}) z_{t-1}$ , where  $d\text{VaR}^{\gamma}(y_t)/dz_{t-1}$  is given by (22). The total impact is decomposed into the impact on the conditional location  $\mu_t$ , scale  $\sigma_t$ , tail scale  $\delta_t$ , and tail shape  $\xi_t$  by setting the non-active summands in (22) to zero. Columns labeled EN, GR, IE, IT, and PT refer to Spanish, Greek, Irish, Italian, and Portuguese five-year benchmark bond yields.

97.5% VaR							
	$\mathbf{EN}$	$\operatorname{GR}$	IE	IT	$\mathbf{PT}$		
$\mu_t$	-2.623	-2.856	0.017	-1.479	-0.053		
$\sigma_t$	-1.155	-2.439	-6.570	-0.537	-8.006		
$\delta_t$	-0.068	-0.702	0.587	-0.042	1.216		
$\xi_t$	0.001	0.037	0.068	-0.013	-0.040		
Total	-3.845	-5.961	-5.899	-2.071	-6.883		
		99.5	% VaR				
	$\mathbf{EN}$	$\operatorname{GR}$	IE	IT	$\mathbf{PT}$		
$\mu_t$	-2.623	-2.856	0.017	-1.479	-0.053		
$\sigma_t$	-2.302	-5.361	-14.604	-1.163	-18.578		
$\delta_t$	-0.190	-2.120	1.638	-0.131	3.556		
$\xi_t$	0.009	0.260	0.443	-0.096	-0.278		
Total	-5.106	-10.077	-12.507	-2.870	-15.352		

credit event on 09 March 2012. The tail shape parameter can be above one, suggesting that no conditional mean, variance, and ES exist at such times. The other estimates for  $\xi_t$ typically vary between zero and one. Estimates above one can occur but are temporary and rare. Time-variation in  $\delta_t$  is pronounced as well.

The tail shape and scale parameters of Figure 5 are difficult to interpret in economic (or probabilistic) terms when considered in isolation. Table 5 therefore addresses the relevant economic question how market risk measures responded on average to a  $\leq 1$  bn bond purchase intervention. The total impact is decomposed into the impact on the conditional location, scale, tail scale, and tail shape by setting the non-active summands in (22) to zero. The estimates corroborate that most of the SMP's effect on extreme market risk came from its impact on location and scale, and thus from its impact on the center of the distribution. We estimate that the 97.5% VaR was reduced by 3.8, 6.0, 5.9, 2.1, and 6.9 bps per  $\leq 1$  bn Eurosystem intervention in Spanish, Greek, Irish, Italian, and Portuguese five-year bench-

mark bonds, respectively. The impact grows with the extremeness of the VaR. The 99.5% VaR estimate is reduced, respectively, by 5.1, 10.1, 12.5, 2.9, and 15.4 bps per  $\leq 1$  bn of Eurosystem purchases in the above bonds. These are economically meaningful reductions in market risk. Lower market risks likely helped market makers and dealer banks at the time to remain in the market and to continue to supply liquidity to turbulent bond market segments; see e.g. Pelizzon et al. (2013, 2016). High market risks can force dealer banks to retreat, in particular when their own VaR constraints are binding; see Vayanos and Vila (2009) and Adrian and Shin (2014). In turn, malfunctioning sovereign bond markets can impair a balanced transmission of the common monetary policy stance to all parts of the euro area. Table 5 also shows that these improvements were obtained without worsening the tail parameters. If anything, additional beneficial secondary effects came about via the SMP's effect on tail shape and tail scale parameters for large economies such as Spain and Italy.<sup>9</sup>

## 4.4 Tail shape and tail scale estimates from raw data

We conclude our empirical study with a discussion of tail shape and tail scale estimates from raw (un-prefiltered) data  $y_t$ . The dynamic tail shape and tail scale model of Section 2 could be robust to omitted variation in the center of the distribution  $g(y_t | \mathcal{F}_{t-1})$ . This is because of two effects. First, the autoregressive specification of  $\tau_t$  via (10) implies that  $\tau_t$ can adjust to time variation in the center of the distribution. The resulting exceedances  $\tilde{x}_t = y_t - \tilde{\tau}_t$  from unfiltered data can therefore in practice still be close to the exceedances  $x_t = (y_t - \mu_t)/\sigma_t - \tau_t$  from pre-filtered data. Second, the dynamic specification of  $\delta_t$  via (7) implies that the tail scale could mop up omitted time-variation in  $\sigma_t$ , leaving  $\xi_t$  free to fit the time-variation in tail shape.

Web Appendix G discusses our tail shape and tail scale estimates obtained from POTs  $\tilde{x}_t = y_t - \tilde{\tau}_t$ , along with the model's deterministic parameters. The estimates of  $c^{\delta}$ , the SMP impact on tail scale, are now negative in all five cases, and are statistically significantly

<sup>&</sup>lt;sup>9</sup>Additional, beneficial SMP announcement effects are not taken into account in Table 5. This is because both the 09 May 2010 and 08 August 2011 SMP announcements occurred when markets were closed, and are therefore not part of our sample. The VaR impact estimates are conservative in this sense.

negative at a 5% confidence level in two cases. This is intuitive, as  $\delta_t$  now not only captures dispersion in the tail, but to some extent also in the center. The point estimates of  $c^{\xi}$  remain statistically insignificant. The estimates  $\hat{\xi}_t$  and  $\hat{\delta}_t$  from un-prefiltered data are more volatile, and visibly different from the estimates from pre-filtered data as reported in Figure 5. This suggests that the score-driven updates of  $\tau_t$  and  $\delta_t$  do not fully absorb all variation in  $\mu_t$  and  $\sigma_t$  for our data at hand. We therefore prefer the estimates based on appropriately prefiltered data.

# 5 Conclusion

We introduced a semi-parametric modeling framework to study time variation in tail parameters for long univariate time series. To this end we modeled the time variation in the shape and scale parameters of the Generalized Pareto Distribution, which approximates the tail of most heavy-tailed densities used in econometrics and the actuarial sciences. We discussed the handling of non-tail time series observations, inference on deterministic and time-varying parameters, and how to relate tail variation to observed covariates if such variables are available. The model therefore complements and extends recent work based on different methodologies, such as the non-parametric approach to tail index variation of de Haan and Zhou (2020), the time-varying quantile (and ES) approaches of Patton et al. (2019) and Catania and Luati (2019), and the parametric modeling approach of Massacci (2017). We applied the model to study the impact of bond purchases within the Eurosystem's SMP between 2010 and 2012 on the extreme upper tail of sovereign bond yield changes measured at a high frequency, concluding that the program had a beneficial impact on extreme tail quantiles, leaning against the risk of extremely adverse market outcomes while active. This beneficial impact is mostly explained by moving the center of the predicative distribution to the left and narrowing it, rather than via an impact on tail shape or tail scale parameters.

Evidently, our model for time-varying tail parameters is focussed on capturing marginal features. In many applications it may also be of interest to study the time-varying nature of joint extremes; see e.g. Castro-Camilo et al. (2018), Escobar-Bach et al. (2018), and

Mhalla et al. (2019). In terms of the current application, one could wonder, for example, if the extreme bond yield changes for Portuguese and Greek sovereign bonds, say, were more dependent at certain points in time. We leave such research for future work; but see also Lucas et al. (2014) and Patton and Oh (2018) in this regard.

## References

- Adrian, T. and H. S. Shin (2014). Procyclical leverage and Value-at-Risk. Review of Financial Studies 27(2), 373–403.
- Blasques, F., P. Gorgi, and S. J. Koopman (2018). Missing observations in observation-driven time series models. *Tinbergen Institute Discussion Paper 2018-013/III*, 1–39.
- Blasques, F., S. J. Koopman, K. Lasak, and A. Lucas (2016). In-sample confidence bands and outof-sample forecast bands for time-varying parameters in observation-driven models. *International Journal of Forecasting 32*, 875–887.
- Blasques, F., S. J. Koopman, and A. Lucas (2015). Information theoretic optimality of observation driven time series models for continuous responses. *Biometrika* 102(2), 325–343.
- Blasques, F., S. J. Koopman, and A. Lucas (2020). Meximum likelihood estimation for score-driven models. *Tinbergen Institute discussion papers 2014-029/III, update July 2020*, 1–54.
- Castro-Camilo, D., M. de Carvalho, and J. Wadsworth (2018). Time-varying extreme value dependence with application to leading European stock markets. Annals of Applied Statistics 12(1), 283–309.
- Catania, L. and A. Luati (2019). Semiparametric modeling of multiple quantiles. Available at SSRN 3494995.
- Chavez-Demoulin, V., P. Embrechts, and S. Sardy (2014). Extreme-quantile tracking for financial time series. *Journal of Econometrics* 181(1), 44–52.
- Cœuré, B. (2013). Outright Monetary Transactions, one year on. Speech at the conference "The ECB and its OMT programme," Berlin, 2 September 2013.

Coles, S. (2001). An introduction to statistical modeling of extreme values. Springer Press, London.

- Cox, D. R. (1981). Statistical analysis of time series: some recent developments. Scandinavian Journal of Statistics 8, 93–115.
- Creal, D., S. J. Koopman, and A. Lucas (2013). Generalized autoregressive score models with applications. *Journal of Applied Econometrics* 28(5), 777–795.
- Creal, D., B. Schwaab, S. J. Koopman, and A. Lucas (2014). An observation driven mixed measurement dynamic factor model with application to credit risk. *The Review of Economics and Statistics* 96(5), 898915.
- D'Agostino, R. B., A. Belanger, and R. B. D'Agostino Jr (1990). A suggestion for using powerful and informative tests of normality. *The American Statistician* 44(4), 316–321.
- Davidson, A. C. and R. L. Smith (1990). Models for exceedances over high thresholds. Journal of the Royal Statistical Association, Series B 52(3), 393–442.
- Davidson, R. and J. G. MacKinnon (2004). *Econometric theory and methods*. Oxford University press.
- de Haan, L. and C. Zhou (2020). Trends in extreme value indices. *Journal of the Americal Statistical Association, forthcoming*.
- ECB (2013). European Central Bank Annual Report 2012.
- ECB (2014). The determinants of euro area sovereign bond yield spreads during the crisis. ECB Monthly Bulletin article, May 2014.
- Einmahl, J., L. de Haan, and C. Zhou (2016). Statistics of heteroscedastic extremes. Journal of the Royal Statistical Society, Series B 78, 31–51.
- Embrechts, P., C. Klüppelberg, and T. Mikosch (1997). Modelling extremal events for insurance and finance. Springer Verlag, Berlin.
- Engle, R. F. and S. Manganelli (2004). CAViaR: Conditional autoregressive value at risk by regression quantiles. *Journal of Business & Economic Statistics* 22(4), 367–381.

- Engle, R. F. and A. J. Patton (2001). What good is a volatility model? *Quantitative Finance* 1(2), 237–245.
- Escobar-Bach, M., Y. Goegebeur, and A. Guillou (2018). Local robust estimation of the Pickands dependence function. Annals of Statistics 46(6A), 2806–2843.
- Eser, F. and B. Schwaab (2016). Evaluating the impact of unconventional monetary policy measures: Empirical evidence from the ECB's Securities Markets Programme. Journal of Financial Economics 119(1), 147–167.
- Galbraith, J. W. and S. Zernov (2004). Circuit breakers and the tail index of equity returns. *Journal* of Financial Econometrics 2(1), 109–129.
- Ghysels, E., J. Idier, S. Manganelli, and O. Vergote (2017). A high frequency assessment of the ECB Securities Markets Programme. *Journal of European Economic Association* 15(1), 218–243.
- Harvey, A. C. (2013). Dynamic models for volatility and heavy tails with applications to financial and economic time series. Cambridge University Press.
- Hill, B. (1975). A simple general approach to inference about the tail of a distribution. The Annals of Statistics 3(5), 1163–1174.
- Hoga, Y. (2017). Testing for changes in (Extreme) VaR. Econometrics Journal 20, 23-51.
- Huisman, R., K. Koedijk, C. Kool, and F. Palm (2001). Tail-index estimates in small samples. Journal of Business & Economic Statistics 19(1), 208–216.
- Koenker, R. (2005). Quantile Regression. Cambridge: Cambridge University Press.
- Koenker, R. and B. J. Park (1996). An interior point algorithm for nonlinear quantile regression. Journal of Econometrics 71(1-2), 265–283.
- Lin, C.-H. and T.-C. Kao (2018). Multiple structural changes in the tail behavior: evidence from stock market futures returns. Nonlinear Analysis: Real World Applications 9, 1702–1713.
- Lucas, A., B. Schwaab, and X. Zhang (2014). Conditional euro area sovereign default risk. Journal of Business and Economics Statistics 32(2), 271–284.

- Lucas, A. and X. Zhang (2016). Score driven exponentially weighted moving average and value-atrisk forecasting. *International Journal of Forecasting 32*, 293–302.
- Manganelli, S. and R. F. Engle (2004). A comparison of value at risk models in finance. In G. Szego (Ed.), Risk Measures for the 21st Century. Wiley Finance.
- Massacci, D. (2017). Tail risk dynamics in stock returns: Links to the macroeconomy and global markets connectedness. *Management Science* 63(9), 112–132.
- McNeil, A. and R. Frey (2000). Estimation of tail-related risk measures for heteroscedastic financial time series: An Extreme Value approach. *Journal of Empirical Finance* 7(3-4), 271–300.
- McNeil, A. J., R. Frey, and P. Embrechts (2010). *Quantitative risk management: Concepts, techniques, and tools.* Princeton University press.
- Mhalla, L., M. de Carvalho, and V. ChavezDemoulin (2019). Regressiontype models for extremal dependence. *Scandinavian Journal of Statistics* 46(4), 1141–1167.
- Patton, A. (2006). Modelling asymmetric exchange rate dependence. International Economic Review 47(2), 527–556.
- Patton, A. J. and D. H. Oh (2018). Time-varying systemic risk: evidence from a dynamic copula model of CDS spreads. *Journal of Business & Economic Statistics* 36(2), 181–195.
- Patton, A. J., J. F. Ziegel, and R. Chen (2019). Dynamic semiparametric models for Expected Shortfall (and Value-at-Risk). *Journal of Econometrics* 211(2), 388–413.
- Pelizzon, L., M. Subrahmanyam, D. Tomio, and J. Uno (2013). The microstructure of the European sovereign bond market: A study of the Eurozone crisis. Unpublished working paper, University of Venice, New York University, Copenhagen Business School, and Waseda University.
- Pelizzon, L., M. Subrahmanyam, D. Tomio, and J. Uno (2016). Sovereign credit risk, liquidity, and ECB intervention: Deus Ex Machina? *Journal of Financial Economics* 122(1), 44–52.
- Pooter, M. D., R. F. Martin, and S. Pruitt (2018). The liquidity effects of official bond market intervention. *Journal of Financial and Quantitative Analysis* 53(1), 243–268.

- Quintos, C., Z. Fan, and P. C. Phillips (2001). Structural change tests in tail behaviour and the asian crisis. The Review of Economic Studies 68(3), 633–663.
- Rocco, M. (2014). Extreme value theory in finance: A survey. Journal of Economic Surveys 28(1), 82–108.
- Roll, R. (1984). A simple implicit measure of the effective bid-ask spread in an efficient market. The Journal of Finance 39(4), 1127–1139.
- Vayanos, D. and J.-L. Vila (2009). A preferred habitat model of the term structure of interest rates. NBER Working Paper 15487.
- Wagner, N. (2005). Autoregressive conditional tail behavior and results on government bond yield spreads. International Review of Financial Analysis 14(2), 247–261.
- Wang, H. and C.-L. Tsai (2009). Tail Index Regression. Journal of the American Statistical Association 104(487), 1233–1240.
- Werner, T. and C. Upper (2004). Time variation in the tail behavior of bund future returns. *Journal* of Futures Markets 24 (4), 387–398.

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