

Reimers, Hans-Eggert; Dreger, Christian

### Working Paper

## Panel Seasonal Unit Root Test With An Application for Unemployment Data

IWH Discussion Papers, No. 191/2004

### Provided in Cooperation with:

Halle Institute for Economic Research (IWH) – Member of the Leibniz Association

*Suggested Citation:* Reimers, Hans-Eggert; Dreger, Christian (2004) : Panel Seasonal Unit Root Test With An Application for Unemployment Data, IWH Discussion Papers, No. 191/2004, Leibniz-Institut für Wirtschaftsforschung Halle (IWH), Halle (Saale),  
<https://nbn-resolving.de/urn:nbn:de:gbv:3:2-482>

This Version is available at:

<https://hdl.handle.net/10419/23728>

#### Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

#### Terms of use:

*Documents in EconStor may be saved and copied for your personal and scholarly purposes.*

*You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.*

*If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.*



Das Institut für Wirtschaftsforschung Halle ist Mitglied der Leibniz-Gemeinschaft

Panel Seasonal Unit Root Test With  
An Application for Unemployment Data

*Christian Dreger  
Hans-Eggert Reimers*

Juli 2004

Nr. 191

Diskussionspapiere  
*Discussion Papers*

Hans-Eggert Reimers  
Hochschule Wismar  
University of Technology, Business and Design  
23952 Wismar, Germany

Tel.: +49 (3841) 753 601  
Fax: +49 (3841) 753 131  
Email: h.reimers@wi.hs-wismar.de

Christian Dreger  
Halle Institute for Economic Research  
06017 Halle/Saale, Germany

Tel.: +49/345/7753 854  
Fax: +49/345/7753 820  
Email: cdr@iwh-halle.de

Diskussionspapiere stehen in der alleinigen Verantwortung der jeweiligen Autoren. Die darin vertretenen Auffassungen stellen keine Meinungsäußerung des IWH dar.

Herausgeber:

INSTITUT FÜR WIRTSCHAFTSFORSCHUNG HALLE (IWH)

Postanschrift: Postfach 11 03 61, 06017 Halle(Saale)  
Hausanschrift: Kleine Märkerstraße 8, 06108 Halle (Saale)

Telefon: (0345) 77 53-60  
Telefax: (0345) 77 53-8 20  
Internet: <http://www.iwh-halle.de>

Christian Dreger<sup>1</sup> and

Hans-Eggert Reimers

Institute of Economic Research  
Kleine Märkerstr. 8  
D - Halle  
GERMANY

Hochschule Wismar  
University of Technology,  
Business and Design  
Postfach 12 10  
D - 23952 Wismar  
GERMANY

## **Abstract**

In this paper the seasonal unit root test of Hylleberg et al. (1990) is generalized to cover a heterogenous panel. The procedure follows the work of Im, Pesaran and Shin (2002). Test statistics are proposed and critical values are obtained by simulations. Moreover, the properties of the tests are analyzed for different deterministic and dynamic specifications. Evidence is presented that for a small time dimension the power is slow even for increasing cross section dimension. Therefore, it seems necessary to have a higher time dimension than cross section dimension. The new test is applied for unemployment behaviour in industrialized countries. In some cases seasonal unit roots are detected. However, the null hypotheses of panel seasonal unit roots are rejected. The null hypothesis of a unit root at the zero frequency is not rejected, thereby supporting the presence of hysteresis effects.

**Keywords:** Panel seasonal unit root test; IPS-approach; Unemployment data.

**JEL Classification:** C22, C23

---

<sup>1</sup>The research of this paper was supported by the Deutsche Forschungsgemeinschaft.

## 1 Introduction

It has become a common practice in macroeconomic analysis to test for unit roots. However, the power of the tests is often very small. It can be increased if the information base is extended by pooling data over individual cross sections (countries, regions, sectors). Therefore, panel unit root tests are proposed (see Banerjee 1999 for a survey).

Usually, the tests concentrate on unit roots at the zero or long run frequency, implying that the analysis is limited to seasonal adjusted data. Strong seasonality can bias the results of these tests. In some cases the seasonal pattern may be described by deterministic seasonal intercepts, or stochastic dynamic effects. However, even the seasonal pattern may be subject to stochastic trends, indicating that the series may be well approximated by seasonal unit roots. These series include additional unit roots at the annual and half yearly frequency. Hylleberg et al. (1990) suggest a test strategy for this problem. The test generalizes the Dickey-Fuller test to cover seasonal frequencies. An extension to the panel framework is clearly recommended.

Therefore, this paper discusses a seasonal unit root test in the line of Hylleberg et al. (1990) for a heterogenous panel. The procedure is build upon the work of Im, Pesaran and Shin (2002). Test statistics are proposed and critical values are obtained by simulations. Moreover, the properties of the tests are analyzed for different deterministic and dynamic specifications. The new test is applied for unemployment behaviour in industrialized countries. In some cases seasonal unit roots are detected. However, the null hypotheses of panel seasonal unit roots are rejected. The null hypothesis of a unit root at the zero frequency is not rejected, thereby supporting the presence of hysteresis effects.

The paper proceeds as follows. The next section (section 2) gives the statistical framework. In section 3 simulations are described and results are presented. The empirical example is discussed in section 4, and section 5 concludes.

## 2 Statistical framework of seasonal processes

### 2.1 Seasonal integration HEGY-test

To test the unit root properties of variables with a substantial seasonal pattern Hylleberg et al. (1990) have proposed a generalization to the Dickey-Fuller approach, denoted as HEGY-test and applied in Engle et al. (1993). The procedure is based on the assumption that the individual time series is generated by a finite autoregressive process

$$\phi(B)x_t = \epsilon_t \quad (1)$$

with  $\epsilon_t$  as a zero mean white noise. The operator  $B$  denotes the backshift operator ( $Bx_t = x_{t-1}$ ). If this process  $x_t$  is integrated and seasonally integrated then  $\phi(z) = 0$  has

roots at 1,  $-1$ , and  $\pm i$ , where a maximum integration order of one is imposed. These roots correspond to zero frequency, frequency  $\omega$  (two cycles a year, biannual), and frequency  $\omega/2$  (one cycle a year, annual). Under this hypothesis  $\phi(B)$  contains the factors

$$(1 - B^4) = (1 - B)(1 + B)(1 + B^2). \quad (2)$$

To analyze the unit roots at all seasonal frequencies and zero frequency the process is rearranged as

$$\phi^*(B)\Delta_4x_t = \pi_1z_{1,t-1} + \pi_2z_{2,t-1} + \pi_3z_{3,t-2} + \pi_4z_{3,t-1} + \epsilon_t \quad (3)$$

where

$$\begin{aligned} z_{1,t} &= (1 + B + B^2 + B^3)x_t \\ z_{2,t} &= -(1 - B + B^2 - B^3)x_t \\ z_{3,t} &= -(1 - B^2)x_t \\ \Delta_4x_t &= (1 - B^4)x_t \end{aligned}$$

and  $\phi^*(B)$  is a stationary polynomial in the lag operator  $B$ . The last transformation eliminates all roots on the unit circle, which correspond to seasonal frequencies and to zero frequency.  $\Delta_4x_t$  is stationary. By contrast,  $z_{1,t}$  contains a stochastic trend, as seasonal unit roots have been filtered out. In  $z_{2,t}$  the stochastic trend and the roots  $\pm i$  are eliminated, whereas in  $z_{3,t}$  the roots  $\pm 1$  are removed. Hylleberg et al. (1990) suggest the following procedure. Estimate equation (3) by OLS and test the following hypotheses:

- i) existence of the root 1 :  $\pi_1 = 0$
- ii) existence of the root -1 :  $\pi_2 = 0$
- iii) existence of the roots  $\pm i$  :  $\pi_3 = \pi_4 = 0$

The alternative hypothesis is stationarity of the process. It is accepted, if the conditions  $\pi_1 < 0$ ,  $\pi_2 < 0$  as well as  $\pi_3$  and  $\pi_4$  not both equal to zero are satisfied. The alternative may be augmented by allowing for the possibility of a deterministic component like an intercept (I), linear trend (T), and for seasonal dummies (S) in the test regression. The test statistics of i) and ii) are corresponding to t-values and for iii) an F-test has to be conducted. Hylleberg et al. (1990) compute the appropriate critical values for these tests by Monte Carlo simulations.

## 2.2 Panel seasonal integration test

Assuming that there are  $N$  cross-sectional units for which the test equation (3) is applied. The Im Pesaran Shin (IPS) panel unit root test is based on the null of non-stationarity ( $\pi_{1i} = 0 \forall i$ ) against the alternative of no unit root ( $\pi_{1i} < 0 \forall i$ ). The IPS test does not

assume that all cross-sectional units converge towards the equilibrium value at the same speed under the alternative. Instead, the speed may be different. Following Im, Pesaran and Shin (2002) it is assumed that the  $\epsilon_{it}$ ,  $i = 1, \dots, N$ ,  $t = 1, \dots, T$  in (3) are independently and identically distributed random variables for all  $i$  and  $t$  with zero means and finite heterogeneous variances  $\sigma_i^2$ . For the zero frequency the IPS test is based on the standardized  $t$ -bar statistic as follows:

$$\Gamma_{1t} = \frac{\sqrt{N}(\bar{t}_{1NT} - N^{-1} \sum_1^N E\{t_{1iT}(p_i) | \pi_{1i} = 0\})}{\sqrt{N^{-1} \sum_1^N Var\{t_{1iT}(p_i) | \pi_{1i} = 0\}}} \sim N(0, 1), \quad (4)$$

where  $\bar{t}_{1NT}$  is the average of the  $N$  cross-section ADF( $p_i$ )  $t$ -statistics,  $E\{t_{1iT}(p_i) | \pi_{1i} = 0\}$  and  $Var\{t_{1iT}(p_i) | \pi_{1i} = 0\}$  are the mean and variance respectively of the average ADF( $p_i$ ) statistics under the null for the zero frequency. The values are tabulated by Im et al. (2002, Tables 3) for different  $T$  and lag orders  $p_i$ . They show that under the null of a unit root  $\Gamma_{1t}$  is distributed as  $N(0, 1)$ .

For the bi-annual frequency the same procedure is adopted. The test statistic is:

$$\Gamma_{2t} = \frac{\sqrt{N}(\bar{t}_{2NT} - N^{-1} \sum_1^N E\{t_{2iT}(p_i) | \pi_{2i} = 0\})}{\sqrt{N^{-1} \sum_1^N Var\{t_{2iT}(p_i) | \pi_{2i} = 0\}}} \sim N(0, 1), \quad (5)$$

where  $\bar{t}_{2NT}$  is the average of the  $N$  cross-section ADF( $p_i$ )  $t$ -statistics,  $E\{t_{2iT}(p_i) | \pi_{2i} = 0\}$  and  $Var\{t_{2iT}(p_i) | \pi_{2i} = 0\}$  are the mean and variance respectively of the average ADF( $p_i$ ) statistics under the null for the bi-annual frequency. Since HEGY show that the test statistic for the zero and the bi-annual frequency have the same asymptotic distribution the identical values of the mean and variance are used.

For the annual frequency the null of  $\pi_{i3} = \pi_{i4} = 0 \forall i$  is tested by a  $F$ -test, which is used in the panel approach.

$$\Gamma_{3t} = \frac{\sqrt{N}(\bar{F}_{NT} - N^{-1} \sum_1^N E\{F_{iT}(p_i) | \pi_{3i} = \pi_{4i} = 0\})}{\sqrt{N^{-1} \sum_1^N Var\{F_{iT}(p_i) | \pi_{3i} = \pi_{4i} = 0\}}} \sim N(0, 1), \quad (6)$$

where  $\bar{F}_{NT}$  is the average of the  $N$  cross-section ADF( $p_i$ )  $F$ -statistics,  $E\{F_{iT}(p_i) | \pi_{3i} = \pi_{4i} = 0\}$  and  $Var\{F_{iT}(p_i) | \pi_{3i} = \pi_{4i} = 0\}$  are the mean and variance respectively of the average  $F(p_i)$  statistics under the null for the annual frequency.

### 3 Simulation

#### 3.1 Simulation experiments

In this section we use Monte Carlo experiments to examine finite sample properties of the panel-based seasonal unit root tests. The experiment adopts that of Im et al. (2002). The first set focuses on the benchmark model

$$y_{it} = (1 - \phi_i)\mu_i + \phi_i y_{i,t-4} + \epsilon_{it}, \quad t = 1, \dots, T; \quad i = 1, \dots, N, \quad (7)$$

where  $\epsilon_{it} \sim N(0, \sigma_i^2)$ . The second set of experiments allows for the presence of positive (heterogeneous) AR(1) serial correlations in  $\epsilon_{it}$ ,

$$\epsilon_{it} = \rho_i \epsilon_{i,t-1} + e_{it}, \quad t = 1, \dots, T; \quad i = 1, \dots, N, \quad (8)$$

where  $e_{it} \sim N(0, \sigma_i^2)$ ,  $\rho_i \sim U[0.2, 0.4]$ ,  $U$  denotes a uniform distribution and  $\rho_i$ 's are generated independently of  $e_{it}$ . The next sets of experiments allow for seasonal dummies, a linear trend and seasonal dummies as well as a linear trend in estimation of the HEGY regressions using the same data generating process employed in the first two sets of experiments.

In all of the experiments  $e_{it}$  (or  $\epsilon_{it}$ ) are generated as *iid* normal variates with zero means and heterogeneous variances,  $\sigma_i^2$ . The parameters  $\mu_i$  and  $\sigma_i^2$  are generated according to

$$\mu_i \sim N(0, 1), \quad \sigma_i^2 \sim U[0.5, 1.5], \quad i = 1, \dots, N, \quad (9)$$

Under the null  $\phi_i = 1$  for all  $i$  (denoted as set 1), while  $\phi_i = 0.8$  for all  $i$  under the alternative hypothesis (denoted as set 2, the case with AR-errors is denoted set 3). All of the parameter values such as  $\mu_i$ ,  $\sigma_i^2$  or  $\rho_i$  are generated independently of  $\epsilon_{it}$  once and the fixed throughout replications. The first set of experiments are carried out for  $N = 5, 10, 20, 40, 100$  and  $T = 20, 32, 40, 60, 100$ . The other experiments (sets 2 and 3) are conducted for  $N = 5, 10, 20, 40, 100$ ,  $T = 20, 32, 40, 60, 100$  and  $p = 0, 1, 2, 3, 4, 5$ . We used 2000 replications to compute empirical size and power of the tests at the 5% nominal level.

### 3.2 Simulation results

The simulated critical values at the 5 percent significance level are given in the tables 1 to 5. Table 1 shows that the critical values for  $\Gamma_1$ ,  $\Gamma_2$  and  $\Gamma_3$  decrease with an increasing sample size  $T$  independent of the deterministic specification. The critical values of  $\Gamma_1$  are different from  $\Gamma_2$  if the regression equation includes an intercept or an intercept and a linear trend. They are more or less the same if an intercept and seasonal dummies are included. Accounting for a linear trend decreases the critical values for  $\Gamma_1$ . The specification of seasonal dummies does not influence the values of  $\Gamma_1$ . It affects the values of  $\Gamma_2$ . Moreover, if the panel dimension is increased (see Tables 2 to 5) it does not change these observations. If the critical values of a higher panel dimension are compared with the critical values for  $N = 5$ , where the deterministic specification is identical, it is apparent that the critical values are higher (lower) for  $\Gamma_1$  and  $\Gamma_2$  ( $\Gamma_3$ ).

In Tables 6 to 10 the means and standard deviations of the corresponding distributions are presented. For example in Table 6 the panel dimension is  $N = 5$ . In the first cell the sample size is  $T = 20$ , such that the mean is -1.3498 and the standard deviation is in parentheses (.3912). These results correspond to the distribution of  $\Gamma_1$ , where the critical

value of -1.9898 is given in Table 1 first cell. The values in Tables 6 to 10 are used to test for seasonal unit roots.

The next step is to analyze the nominal values of the tests if the data generating processes have different covariances. The covariances are drawn from a uniform distribution in the range of 0.5 to 1.5. The nominal value of the tests is the 5 percent level, hence, the critical value is -1.64486. In this experiment the number of cases is counted, where the test value is lower than the critical value. The Tables 11 to 15 gives these frequencies, where the number should be close to the 5 percent. Table 11 presents the results for the panel dimension  $N = 5$ . The first block of Table 11 exhibits the specification, which corresponds to the regression that is used to generate the critical values. The next block includes the result if the test regression contains one lag of the endogenous variable. In other words these equations are overfitted. The limits of the values to be in line with the nominal value can be determined by  $\sqrt{p(1-p)/2000}$ , where  $p$  indicates the nominal significance level. The two error bounds are 4 and 6 for  $p = 5$ . At first, if the test regression includes an intercept, the test statistic  $\Gamma_1$  is well sized.  $\Gamma_2$  is to some extent undersized whereas  $\Gamma_3$  is oversized for the different sample sizes. The small overfitting (lag = 1 or 2) does not destroy this evidence. Turning to the trend specification the evidence for the  $\Gamma_1$  or  $\Gamma_2$  test statistic do not change. However, the  $\Gamma_3$  test statistic is undersized for sample sizes of from  $T = 20$  to  $T = 60$  and a lag length of one or two.

If the panel dimension is increased (see Table 12 to 15) the results for  $\Gamma_1$ ,  $\Gamma_2$  and  $\Gamma_3$  become better if the test regression only includes an intercept and no lags. If a lag of unity is specified the test statistics  $\Gamma_1$  and  $\Gamma_2$  are undersized for  $N = 100$  and  $T = 100$ . The same is found if seasonal dummies and a linear trend are specified. In general if the test regression is well specified the tests work good. A misspecification of test regression destroy the nominal size of the tests.

The power results are given in Tables 16 to 25. For  $N = 5$  the null hypothesis of no unit root at the null frequency is rarely rejected for small sample sizes (first row in Table 16) if the test regression only includes an intercept. The two other tests have a higher power in such situation. It is nearly 100 percent for  $T = 100$  (see also Figure 1 upper left panel). A lag specification reduces the power. If the test regression additionally contains a linear trend results of the  $\Gamma_1$  and  $\Gamma_2$  test do not change substantially. The  $\Gamma_3$  test looses power. Specifying seasonally dummies reduces the power of  $\Gamma_1$  and  $\Gamma_2$  (see Figure 1 middle right panel).

It is worth noting that the power of the tests grows if the panel dimension increases for the cases of no linear trend and no seasonal dummies. The power of the tests is high if the correct specification is selected (see Figure 1 upper row and middle left panel). However, in cases of a linear trend and seasonal dummies and lags the power of the tests is low as long as the dimension is small ( $T \leq 40$ ) (see Table 20). This evidence is also found

if the autoregressive errors are considered (see Table 21 to 25, Figure 1 lower row). An underfitting of the test equation (lag = 0) substantially reduces the power of the  $\Gamma_1$  test. In such cases the test has no power even if the panel dimension is  $N = 100$  and the time dimension less than 60. For  $\Gamma_2$  and  $\Gamma_3$  better results are presented (see Table 21 for example).

#### 4 Application

According to the insider-outsider theory of the labour market, hysteresis may arise as a consequence of the division between insiders, who are employed, and outsiders, who are unemployed (Blanchard and Summers 1986). If union's expectations depend on past employment autoregressive components are included. Provided that former employment fully affects the expectations, the employment series contain a random walk. Under the assumption that labour supply is stationary unemployment will include a random walk. Leon-Ledesma (2000) tests this hypothesis for the unemployment rate of 51 US states and 12 EU countries for the period 1985-1999 with quarterly data. He uses the IPS-tests and finds mixed results for the US states and EU countries. For the EU countries the null hypothesis of nonstationary unemployment series is not rejected. For the US states he presents evidence of nonstationarity if he do not control for correlation in the series. For the adjusted series the null hypothesis is rejected. Moreover, Smyth (2003) presents evidence in favour of hysteresis for Australia performing panel unit root tests based on data of Australian regions.

In this paper the nonstationarity hypothesis is tested for zero frequency and for the seasonal frequencies for the unemployment rate in member countries of the European Union which are at least 9 nine years member of the EU except of Greece. Additionally, Japan and the United States are considered. We use original data, which is not seasonally adjusted. The data are from the OECD data base of the period 1983.1 to 2003.4.

The HEGY approach is adopted to test for individual seasonal unit roots and unit roots at the zero frequency. To control for autocorrelation in the equations at most a lag of 5 is considered. Following the general-to-specific approach significant lags are selected. The specification of the test equations are given in Table 26. It is apparent that in some countries the null hypothesis of no unit root is rejected. In most countries the sample includes seasonal unit roots. Turning to the panel the evidence of seasonal unit roots vanish. Overall, we find no evidence of seasonal unit roots. It is worth noting that the evidence is same if seasonal dummies are specified in the test regression, However, we present strong evidence of a unit roots at the zero frequency. This result is in favour of the hypothesis that hysteresis exist in industrial countries.

## 5 Conclusion

In this paper the seasonal unit root of Hylleberg et al. (1990) is generalized for to cover a heterogenous panel. The procedure is along the lines of Im, Pesaran and Shin (2002). Test statistics are proposed and critical values are obtained by simulations. The properties of the tests are analyzed for different deterministic and dynamic specifications. Evidence is presented that for a small time dimension the power is slow even for increasing cross section dimension. Therefore, it seems necessary to have a higher time dimension than cross section dimension. This result is in line with Phillips and Moon (1999) who require that the ratio  $N/T$  converges to zero for  $N$  and  $T$  go to infinity. Moreover, a misspecification of the test regression, either due to an inappropriate lag order or deterministic component, reduces the power of the test.

At the end of paper the new test is applied to analyze unemployment behaviour in industrialized countries. In some countries seasonal unit roots are detected. However, the null hypotheses of panel seasonal unit roots are rejected. The null hypothesis of a unit root at the zero frequency is not rejected, thereby supporting the presence of hysteresis effects.

## References

- Blanchard, O.J. and L.H. Summers (1986):** "Hysteresis and the European Unemployment problem. In: S. Fischer (ed.) *NBER Macroeconomics Annual*, MIT Press Cambridge, Massachussets. of 1990-1991 (USA)", American Economic Review, Papers and Proceedings, vol. 87, p. 270-274.
- Hylleberg, S., R.F. Engle, C.W.J. Granger, and B.S. Yoo (1990):** "Seasonal Integration and Cointegration", *Journal of Econometrics*, vol. 69, pp. 5–25.
- Engle, R.F., C.W.J. Granger, S. Hylleberg, and H.S. Lee (1993):** "Seasonal Cointegration: The Japanese Consumption Function", *Journal of Econometrics*, vol. 55, p.275–298.
- Hylleberg, S., R.F. Engle, C.W.J. Granger and B.S. Yoo (1990):** "Seasonal Integration and Cointegration", *Journal of Econometrics*, vol. 44, p. 215-238.
- Im, K.S., M.H. Pesaran and Y. Shin (2002):** "Testing for Unit Roots in Heterogeneous Panels", Discussion paper, Trinity College, Cambridge.
- Leon-Ledesma, M.A. (2000):** Unemployment Hysteresis in the US and the EU: A Panel Data Approach, Discussion paper Department of Economics, University of Kent, Kent.
- Phillips, P.C.B. and Moon, H.R. (1999):** "Linear Regression Limit Theory for Non-stationary Panel Data", *Econometrica* 67, 1057–1111.
- Smyth, R. (2003):** "Unemployment Hysteresis in Australian States and Regions", The Australian Economic Reviews, vol. 19,2, pp. 181-192.

**Table 1:** Simulated critical values for the panel dimension of  $N = 5$ .

Specification	Statistic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.9898	-2.0467	-2.0694	-2.0900	-2.1156
	$\Gamma_2$	-1.0087	-1.0537	-1.0660	-1.0883	-1.1065
	$\Gamma_3$	1.9424	1.8586	1.8712	1.8627	1.8894
c,t	$\Gamma_1$	-2.5519	-2.6189	-2.6429	-2.6707	-2.7038
	$\Gamma_2$	-1.0014	-1.0554	-1.0714	-1.0938	-1.1112
	$\Gamma_3$	2.6822	2.2032	2.1342	2.0220	1.9798
c,S	$\Gamma_1$	-1.9436	-2.0140	-2.0415	-2.0654	-2.0996
	$\Gamma_2$	-1.9523	-2.0203	-2.0444	-2.0708	-2.0934
	$\Gamma_3$	7.5251	5.9055	5.5410	5.1279	4.8635
c,S,t	$\Gamma_1$	-2.5103	-2.5843	-2.6197	-2.6491	-2.6886
	$\Gamma_2$	-1.9509	-2.0221	-2.0462	-2.0740	-2.0938
	$\Gamma_3$	8.1211	6.0798	5.6642	5.1864	4.8948

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 2:** Simulated critical values for the panel dimension of  $N = 10$ .

Specification	Statistic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.8031	-1.8669	-1.8879	-1.9185	-1.9353
	$\Gamma_2$	-0.8044	-0.8499	-0.8644	-0.8875	-0.9043
	$\Gamma_3$	1.6417	1.5998	1.5967	1.5995	1.6151
c,t	$\Gamma_1$	-2.3696	-2.4456	-2.4722	-2.5077	-2.5353
	$\Gamma_2$	-0.8069	-0.8559	-0.8704	-0.8947	-0.9089
	$\Gamma_3$	2.2703	1.8961	1.8246	1.7387	1.6982
c,S	$\Gamma_1$	-1.7633	-1.8376	-1.8644	-1.8992	-1.9218
	$\Gamma_2$	-1.7611	-1.8411	-1.8611	-1.8964	-1.9229
	$\Gamma_3$	6.5892	5.2184	4.9210	4.5743	4.3513
c,S,t	$\Gamma_1$	-2.3198	-2.4106	-2.4473	-2.4898	-2.5212
	$\Gamma_2$	-1.7662	-1.8441	-1.8656	-1.9017	-1.9247
	$\Gamma_3$	7.1012	5.2789	5.0266	4.6323	4.3817

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 3:** Simulated critical values for the panel dimension of  $N = 20$ .

Specification	Statistic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.6707	-1.7401	-1.7609	-1.7921	-1.8122
	$\Gamma_2$	-0.6585	-0.7038	-0.7183	-0.7432	-0.7543
	$\Gamma_3$	1.4411	1.4114	1.4154	1.4241	1.4363
c,t	$\Gamma_1$	-2.2398	-2.3250	-2.3534	-2.3898	-2.4197
	$\Gamma_2$	-0.6652	-0.7138	-0.7279	-0.7509	-0.7613
	$\Gamma_3$	1.9924	1.6758	1.6160	1.5479	1.5056
c,S	$\Gamma_1$	-1.6335	-1.7108	-1.7400	-1.7754	-1.8000
	$\Gamma_2$	-1.6306	-1.7125	-1.7376	-1.7731	-1.7996
	$\Gamma_3$	5.9098	4.7420	4.4945	4.1991	4.0076
c,S,t	$\Gamma_1$	-2.1877	-2.2933	-2.3267	-2.3714	-2.4064
	$\Gamma_2$	-1.6338	-1.7171	-1.7413	-1.7775	-1.8017
	$\Gamma_3$	6.3594	4.8973	4.5892	4.2483	4.0334

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 4:** Simulated critical values for the panel dimension of  $N = 40$ .

Specification	Statistic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.5758	-1.6480	-1.6691	-1.6996	-1.7191
	$\Gamma_2$	-0.5577	-0.6036	-0.6153	-0.6387	-0.6561
	$\Gamma_3$	1.3035	1.2866	1.2923	1.3012	1.3139
c,t	$\Gamma_1$	-2.1461	-2.2378	-2.2687	-2.3087	-2.3386
	$\Gamma_2$	-0.5684	-0.6147	-0.6268	-0.6479	-0.6626
	$\Gamma_3$	1.7973	1.5243	1.4720	1.4121	1.3776
c,S	$\Gamma_1$	-1.5372	-1.6216	-1.6487	-1.6846	-1.7088
	$\Gamma_2$	-1.5403	-1.6245	-1.6479	-1.6848	-1.7110
	$\Gamma_3$	5.4549	4.4168	4.2042	3.9360	3.7552
c,S,t	$\Gamma_1$	-2.0912	-2.2084	-2.2429	-2.2907	-2.3253
	$\Gamma_2$	-1.5422	-1.6298	-1.6549	-1.6896	-1.7136
	$\Gamma_3$	5.8545	4.5578	4.2898	3.9836	3.7803

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 5:** Simulated critical values for the panel dimension of  $N = 100$ .

Specifi- cation	Statistic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.4931	-1.5653	-1.5884	-1.6191	-1.6416
	$\Gamma_2$	-0.4663	-0.5113	-0.5263	-0.5480	-0.5651
	$\Gamma_3$	1.1854	1.1787	1.1838	1.1940	1.2079
c,t	$\Gamma_1$	-2.0652	-2.1624	-2.1945	-2.2360	-2.2661
	$\Gamma_2$	-0.4813	-0.5254	-0.5391	-0.5583	-0.5728
	$\Gamma_3$	1.6363	1.3982	1.3489	1.2976	1.2665
c,S	$\Gamma_1$	-1.4571	-1.5441	-1.5704	-1.6051	-1.6323
	$\Gamma_2$	-1.4584	-1.5437	-1.5703	-1.6067	-1.6327
	$\Gamma_3$	5.0491	4.1425	3.9399	3.7037	3.5472
c,S,t	$\Gamma_1$	-2.0072	-2.1321	-2.1698	-2.2178	-2.2531
	$\Gamma_2$	-1.4605	-1.5512	-1.5771	-1.6118	-1.6356
	$\Gamma_3$	5.4121	4.2670	4.0234	3.7487	3.5715

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 6:** Mean and standard deviations for the panel test statistics of panel dimension  $N = 5$ .

Specifi- cation	Stati- tic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.3498 (.3912)	-1.4262 (.3813)	-1.4524 (.3802)	-1.4793 (.3780)	-1.5032 (.3762)
	$\Gamma_2$	-0.3091 (.4312)	-0.3531 (.4329)	-0.3685 (.4311)	-0.3894 (.4333)	-0.4022 (.4337)
	$\Gamma_3$	0.9953 (.5042)	0.9950 (.4672)	1.0092 (.4646)	1.0170 (.4557)	1.0328 (.4607)
c,t	$\Gamma_1$	-1.9253 (.3750)	-2.0309 (.3545)	-2.0662 (.3498)	-2.1092 (.3433)	-2.1420 (.3411)
	$\Gamma_2$	-0.3299 (.4140)	-0.3705 (.4223)	-0.3839 (.4232)	-0.4014 (.4281)	-0.4107 (.4309)
	$\Gamma_3$	1.3698 (.7008)	1.1791 (.5545)	1.1490 (.5299)	1.1037 (.4945)	1.0826 (.4829)
c,S	$\Gamma_1$	-1.3167 (.3819)	-1.4071 (.3698)	-1.4374 (.3704)	-1.4681 (.3706)	-1.4954 (.3711)
	$\Gamma_2$	-1.3181 (.3821)	-1.4079 (.3745)	-1.4349 (.3710)	-1.4678 (.3724)	-1.4942 (.3695)
	$\Gamma_3$	4.3976 (1.700)	3.6813 (1.227)	3.5195 (1.123)	3.3238 (1.018)	3.1885 (.9537)
c,S,t	$\Gamma_1$	-1.8678 (.3815)	-2.0018 (.3515)	-2.0435 (.3464)	-2.0928 (.3390)	-2.1303 (.3380)
	$\Gamma_2$	-1.3219 (.3767)	-1.4161 (.3701)	-1.4426 (.3673)	-1.4740 (.3695)	-1.4984 (.3677)
	$\Gamma_3$	4.6967 (1.870)	3.7909 (1.270)	3.5950 (1.148)	3.3662 (1.028)	3.2102 (.9572)

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 7:** Mean and standard deviations for the panel test statistics of panel dimension  $N = 10$ .

Specifi- cation	Stati- tic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.3503 (.2764)	-1.4265 (.2699)	-1.4512 (.2696)	-1.4807 (.2680)	-1.5032 (.2652)
	$\Gamma_2$	-0.3091 (.3043)	-0.3535 (.3051)	-0.3675 (.3049)	-0.3896 (.3073)	-0.4023 (.3073)
	$\Gamma_3$	0.9925 (.3549)	.9972 (.3308)	1.0074 (.3277)	1.0172 (.3234)	1.0322 (.3254)
c,t	$\Gamma_1$	-1.9262 (.2654)	-2.0313 (.2505)	-2.0669 (.2464)	-2.1093 (.2428)	-2.1405 (.2413)
	$\Gamma_2$	-0.3302 (.2923)	-0.3709 (.2976)	-0.3828 (.2992)	-0.4017 (.3036)	-0.4108 (.3054)
	$\Gamma_3$	1.3668 (.4930)	1.1816 (.3925)	1.1470 (.3736)	1.1044 (.3515)	1.0825 (.3414)
c,S	$\Gamma_1$	-1.3173 (.2703)	-1.4076 (.2618)	-1.4361 (.2628)	-1.4695 (.2628)	-1.4954 (.2615)
	$\Gamma_2$	-1.3163 (.2705)	-1.4082 (.2646)	-1.4338 (.2617)	-1.4684 (.2636)	-1.4949 (.2624)
	$\Gamma_3$	4.4009 (1.212)	3.6819 (.8688)	3.5164 (.7952)	3.3211 (.7195)	3.1862 (.6711)
c,S,t	$\Gamma_1$	-1.8684 (.2694)	-2.0019 (.2480)	-2.0441 (.2442)	-2.0930 (.2403)	-2.1289 (.2391)
	$\Gamma_2$	-1.3206 (.2672)	-1.4164 (.2612)	-1.4416 (.2590)	-1.4747 (.2616)	-1.4989 (.2611)
	$\Gamma_3$	4.6981 (1.329)	3.7901 (.8978)	3.5925 (.8136)	3.3641 (.7268)	3.2084 (.6738)

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 8:** Mean and standard deviations for the panel test statistics of panel dimension  $N = 20$ .

Specifi- cation	Stati- tic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.3507 (.1948)	-1.4262 (.1912)	-1.4492 (.1911)	-1.4816 (.1894)	-1.5026 (.1883)
	$\Gamma_2$	-0.3079 (.2152)	-0.3528 (.2155)	-0.3676 (.2149)	-0.3887 (.2174)	-0.4038 (.2168)
	$\Gamma_3$	0.9910 (.2515)	0.9974 (.2344)	1.0050 (.2324)	1.0167 (.2295)	1.0326 (.2303)
c,t	$\Gamma_1$	-1.9263 (.1881)	-2.0318 (.1775)	-2.0664 (.1747)	-2.1087 (.1720)	-2.1406 (.1699)
	$\Gamma_2$	-0.3290 (.2067)	-0.3702 (.2103)	-0.3831 (.2109)	-0.4008 (.2149)	-0.4122 (.2154)
	$\Gamma_3$	1.3644 (.3496)	1.1820 (.2786)	1.1442 (.2650)	1.1039 (.2494)	1.0830 (.2416)
c,S	$\Gamma_1$	-1.3175 (.1908)	-1.4075 (.1854)	-1.4339 (.1861)	-1.4703 (.1856)	-1.4947 (.1857)
	$\Gamma_2$	-1.3162 (.1918)	-1.4072 (.1865)	-1.4336 (.1854)	-1.4685 (.1864)	-1.4953 (.1863)
	$\Gamma_3$	4.4002 (.8517)	3.6827 (.6157)	3.5163 (.5642)	3.3224 (.5078)	3.1866 (.4738)
c,S,t	$\Gamma_1$	-1.8676 (.1912)	-2.0027 (.1758)	-2.0430 (.1726)	-2.0921 (.1702)	-2.1291 (.1683)
	$\Gamma_2$	-1.3204 (.1895)	-1.4155 (.1844)	-1.4413 (.1835)	-1.4747 (.1851)	-1.4993 (.1854)
	$\Gamma_3$	4.6946 (.9355)	3.7912 (.6355)	3.5918 (.5766)	3.3651 (.5126)	3.2090 (.4758)

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 9:** Mean and standard deviations for the panel test statistics of panel dimension  $N = 40$ .

Specifi- cation	Stati- stic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.3496 (.1377)	-1.4256 (.1352)	-1.4488 (.1345)	-1.4812 (.1336)	-1.5026 (.1329)
	$\Gamma_2$	-0.3081 (.1524)	-0.3530 (.1525)	-0.3679 (.1521)	-0.3889 (.1536)	-0.4046 (.1545)
	$\Gamma_3$	0.9915 (.1770)	0.9971 (.1658)	1.0047 (.1650)	1.0174 (.1631)	1.0336 (.1630)
c,t	$\Gamma_1$	-1.9253 (.1330)	-2.0318 (.1254)	-2.0651 (.1225)	-2.1089 (.1220)	-2.1411 (.1201)
	$\Gamma_2$	-0.3294 (.1463)	-0.3705 (.1488)	-0.3835 (.1494)	-0.4010 (.1518)	-0.4130 (.1535)
	$\Gamma_3$	1.3646 (.2463)	1.1819 (.1970)	1.1439 (.1882)	1.1046 (.1772)	1.0840 (.1710)
c,S	$\Gamma_1$	-1.3166 (.1348)	-1.4069 (.1310)	-1.4335 (.1310)	-1.4698 (.1311)	-1.4947 (.1311)
	$\Gamma_2$	-1.3168 (.1358)	-1.4075 (.1312)	-1.4343 (.1311)	-1.4694 (.1314)	-1.4965 (.1316)
	$\Gamma_3$	4.4015 (.6005)	3.6832 (.4329)	3.5147 (.4011)	3.3223 (.3595)	3.1893 (.3349)
c,S,t	$\Gamma_1$	-1.8668 (.1347)	-2.0024 (.1242)	-2.0418 (.1212)	-2.0923 (.1207)	-2.1296 (.1191)
	$\Gamma_2$	-1.3211 (.1341)	-1.4158 (.1298)	-1.4420 (.1299)	-1.4756 (.1304)	-1.5006 (.1310)
	$\Gamma_3$	4.6961 (.6593)	3.7909 (.4475)	3.5898 (.4093)	3.3650 (.3627)	3.2117 (.3363)

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 10:** Mean and standard deviations for the panel test statistics of panel dimension  $N = 100$ .

Specifi- cation	Stati- stic	Number of observations				
		$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	$\Gamma_1$	-1.3503 (.0872)	-1.4261 (.0856)	-1.4493 (.0848)	-1.4810 (.0845)	-1.5039 (.0840)
	$\Gamma_2$	-0.3091 (.0960)	-0.3536 (.0964)	-0.3683 (.0965)	-0.3886 (.0971)	-0.4045 (.0978)
	$\Gamma_3$	0.9924 (.1127)	0.9976 (.1052)	1.0052 (.1045)	1.0185 (.1032)	1.0342 (.1029)
c,t	$\Gamma_1$	-1.9258 (.0844)	-2.0318 (.0794)	-2.0656 (.0782)	-2.1090 (.0772)	-2.1409 (.0760)
	$\Gamma_2$	-0.3303 (.0922)	-0.3713 (.0941)	-0.3839 (.0947)	-0.4007 (.0959)	-0.4130 (.0972)
	$\Gamma_3$	1.3654 (.1571)	1.1825 (.1250)	1.1447 (.1191)	1.1058 (.1123)	1.0847 (.1080)
c,S	$\Gamma_1$	-1.3169 (.0853)	-1.4075 (.0832)	-1.4340 (.0826)	-1.4696 (.0829)	-1.4960 (.0829)
	$\Gamma_2$	-1.3167 (.0858)	-1.4073 (.0832)	-1.4342 (.0831)	-1.4693 (.0830)	-1.4960 (.0836)
	$\Gamma_3$	4.4014 (.3805)	3.6845 (.2733)	3.5135 (.2525)	3.3207 (.2279)	3.1914 (.2130)
c,S,t	$\Gamma_1$	-1.8663 (.0850)	-2.0025 (.0787)	-2.0423 (.0772)	-2.0923 (.0764)	-2.1295 (.0754)
	$\Gamma_2$	-1.3210 (.0846)	-1.4156 (.0823)	-1.4420 (.0823)	-1.4755 (.0824)	-1.5001 (.0832)
	$\Gamma_3$	4.6934 (.4187)	3.7925 (.2829)	3.5889 (.2574)	3.3633 (.2300)	3.2140 (.2138)

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 11:** Rejection frequency under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 5$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	5.20	5.30	4.90	4.75	4.65
		$\Gamma_2$	3.50	4.85	4.25	4.50	4.45
		$\Gamma_3$	7.35	5.15	6.60	6.00	7.35
c	1	$\Gamma_1$	4.95	4.75	4.55	4.75	4.60
		$\Gamma_2$	3.55	3.75	4.10	4.45	4.50
		$\Gamma_3$	7.05	5.20	6.90	5.70	7.35
c	2	$\Gamma_1$	5.30	5.30	4.75	5.35	4.65
		$\Gamma_2$	4.40	5.30	4.75	4.85	4.80
		$\Gamma_3$	6.75	5.70	6.60	5.90	7.70
c,t	0	$\Gamma_1$	5.30	5.10	5.15	4.60	4.40
		$\Gamma_2$	4.05	4.75	4.20	4.85	4.65
		$\Gamma_3$	7.40	5.80	6.55	5.90	7.80
c,t	1	$\Gamma_1$	4.20	4.50	4.80	4.45	4.50
		$\Gamma_2$	2.90	3.30	3.50	3.95	4.15
		$\Gamma_3$	1.50	2.35	3.65	3.30	6.05
c,t	2	$\Gamma_1$	6.15	5.25	5.25	4.70	4.65
		$\Gamma_2$	4.65	5.05	5.15	5.15	4.80
		$\Gamma_3$	2.20	3.55	4.25	4.25	6.65
c,S	0	$\Gamma_1$	5.55	5.20	4.90	4.50	4.75
		$\Gamma_2$	5.25	4.80	5.20	4.70	4.35
		$\Gamma_3$	6.00	6.30	6.60	6.80	6.65
c,S	1	$\Gamma_1$	3.20	3.60	3.80	3.90	4.40
		$\Gamma_2$	3.05	3.10	3.35	3.95	3.75
		$\Gamma_3$	6.50	1.35	1.70	2.75	4.25
c,S	2	$\Gamma_1$	2.90	4.05	3.60	4.55	4.55
		$\Gamma_2$	3.15	3.45	3.35	4.45	3.75
		$\Gamma_3$	0.95	1.30	1.25	2.30	3.75
c,S,t	0	$\Gamma_1$	5.30	5.00	5.55	4.45	4.50
		$\Gamma_2$	5.00	4.50	4.95	4.75	4.25
		$\Gamma_3$	6.65	6.40	5.85	7.10	6.70
c,S,t	1	$\Gamma_1$	3.00	2.85	3.25	3.45	3.75
		$\Gamma_2$	1.55	1.65	2.00	3.50	3.10
		$\Gamma_3$	1.35	1.35	1.60	2.60	4.00
c,S,t	2	$\Gamma_1$	3.20	3.40	3.00	3.60	3.55
		$\Gamma_2$	2.85	3.30	2.90	4.35	3.75
		$\Gamma_3$	1.00	0.95	1.05	1.85	3.40

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 12:** Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 10$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	4.70	4.95	4.50	5.20	4.70
		$\Gamma_2$	4.45	4.55	4.50	4.30	4.75
		$\Gamma_3$	6.30	5.85	5.95	5.85	7.30
c	1	$\Gamma_1$	4.75	5.20	4.20	5.10	5.05
		$\Gamma_2$	3.85	3.35	3.90	3.65	4.15
		$\Gamma_3$	6.60	6.05	5.90	5.60	6.85
c	2	$\Gamma_1$	4.30	5.00	4.25	4.95	4.80
		$\Gamma_2$	4.85	4.70	4.65	4.50	4.55
		$\Gamma_3$	7.05	5.60	6.75	6.10	7.60
c,t	0	$\Gamma_1$	4.95	5.45	4.70	5.30	5.00
		$\Gamma_2$	4.25	4.55	4.60	4.40	4.85
		$\Gamma_3$	6.80	6.00	6.15	5.90	7.40
c,t	1	$\Gamma_1$	4.15	4.90	4.10	5.00	4.70
		$\Gamma_2$	2.80	2.75	2.80	2.75	3.60
		$\Gamma_3$	0.70	1.45	2.05	3.00	5.15
c,t	2	$\Gamma_1$	4.95	5.10	4.20	5.50	5.15
		$\Gamma_2$	5.10	4.80	4.65	4.50	4.70
		$\Gamma_3$	1.35	2.55	2.85	3.75	5.85
c,S	0	$\Gamma_1$	4.70	5.20	4.40	4.70	5.10
		$\Gamma_2$	5.10	5.55	4.95	4.05	4.70
		$\Gamma_3$	6.45	6.10	5.70	5.80	6.30
c,S	1	$\Gamma_1$	2.10	2.90	3.00	3.90	4.55
		$\Gamma_2$	2.30	2.80	3.05	2.85	3.95
		$\Gamma_3$	0.30	0.80	0.80	2.10	2.65
c,S	2	$\Gamma_1$	1.80	3.05	2.75	3.85	4.25
		$\Gamma_2$	2.10	3.05	2.80	2.80	4.35
		$\Gamma_3$	0.40	0.60	0.70	1.65	2.00
c,S,t	0	$\Gamma_1$	5.45	5.40	4.80	5.15	5.25
		$\Gamma_2$	5.10	5.70	5.25	3.95	4.45
		$\Gamma_3$	6.95	6.10	5.95	5.40	5.80
c,S,t	1	$\Gamma_1$	2.05	2.60	2.60	3.75	3.55
		$\Gamma_2$	0.85	1.45	1.85	1.90	3.15
		$\Gamma_3$	0.60	0.50	0.85	2.05	2.85
c,S,t	2	$\Gamma_1$	2.05	2.50	2.25	3.30	4.15
		$\Gamma_2$	2.25	2.60	2.90	2.65	4.20
		$\Gamma_3$	0.55	0.55	0.50	1.25	1.75

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 13:** Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 20$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	5.05	5.35	5.10	4.70	6.05
		$\Gamma_2$	4.40	4.70	4.80	4.95	4.95
		$\Gamma_3$	5.95	5.65	6.45	5.60	6.95
c	1	$\Gamma_1$	4.70	4.90	4.80	4.65	5.40
		$\Gamma_2$	3.20	3.40	3.85	4.10	4.20
		$\Gamma_3$	5.85	5.70	6.25	5.75	6.45
c	2	$\Gamma_1$	5.45	4.90	5.40	4.35	5.80
		$\Gamma_2$	5.30	5.60	5.30	5.00	5.20
		$\Gamma_3$	6.70	6.50	6.45	6.10	7.00
c,t	0	$\Gamma_1$	4.80	5.50	4.35	4.55	5.30
		$\Gamma_2$	4.45	4.80	4.80	4.90	4.90
		$\Gamma_3$	6.45	5.80	6.35	5.90	7.00
c,t	1	$\Gamma_1$	3.60	4.30	4.00	4.85	4.75
		$\Gamma_2$	2.05	2.45	2.65	2.80	3.70
		$\Gamma_3$	0.05	0.85	1.10	1.90	4.35
c,t	2	$\Gamma_1$	3.95	4.80	4.85	5.70	5.35
		$\Gamma_2$	5.25	5.70	5.25	4.95	4.95
		$\Gamma_3$	0.70	1.35	1.55	2.50	4.70
c,S	0	$\Gamma_1$	5.65	5.40	5.55	4.95	5.95
		$\Gamma_2$	5.85	5.05	4.50	5.15	4.50
		$\Gamma_3$	6.55	6.00	6.50	6.05	5.70
c,S	1	$\Gamma_1$	1.50	2.50	3.25	3.80	4.55
		$\Gamma_2$	2.00	1.70	2.30	3.20	3.70
		$\Gamma_3$	0.15	0.10	0.25	1.15	2.35
c,S	2	$\Gamma_1$	1.55	2.75	3.10	3.40	4.75
		$\Gamma_2$	1.35	1.60	2.30	3.10	3.70
		$\Gamma_3$	0.05	0.25	0.30	0.75	1.70
c,S,t	0	$\Gamma_1$	5.10	5.30	4.75	5.05	5.15
		$\Gamma_2$	5.30	4.80	4.55	5.00	4.30
		$\Gamma_3$	6.60	5.55	6.35	5.60	5.50
c,S,t	1	$\Gamma_1$	0.70	1.60	1.95	2.55	3.70
		$\Gamma_2$	0.40	0.65	1.30	1.90	2.65
		$\Gamma_3$	0.25	0.20	0.45	1.10	2.40
c,S,t	2	$\Gamma_1$	0.90	1.75	2.15	3.00	3.45
		$\Gamma_2$	1.25	1.40	2.30	2.70	3.60
		$\Gamma_3$	0.00	0.20	0.05	0.55	1.35

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 14:** Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 40$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	4.60	5.20	4.85	4.65	6.15
		$\Gamma_2$	4.00	4.45	4.80	4.75	5.00
		$\Gamma_3$	5.90	5.80	5.90	5.90	6.15
c	1	$\Gamma_1$	4.90	4.30	4.20	4.15	5.60
		$\Gamma_2$	2.40	3.50	3.15	3.95	3.80
		$\Gamma_3$	5.90	6.15	6.05	5.40	5.95
c	2	$\Gamma_1$	4.30	4.25	4.90	4.60	6.15
		$\Gamma_2$	4.85	5.40	4.60	4.95	4.70
		$\Gamma_3$	7.45	7.05	5.70	5.90	6.30
c,t	0	$\Gamma_1$	5.40	4.75	4.95	4.60	4.85
		$\Gamma_2$	4.05	4.75	4.90	4.80	5.00
		$\Gamma_3$	5.45	5.45	6.05	5.95	6.15
c,t	1	$\Gamma_1$	4.35	3.55	4.30	3.50	4.30
		$\Gamma_2$	1.30	2.00	1.85	2.70	3.05
		$\Gamma_3$	0.00	0.40	0.55	1.30	3.35
c,t	2	$\Gamma_1$	3.65	4.05	4.90	4.30	4.30
		$\Gamma_2$	5.50	5.50	5.25	5.10	4.75
		$\Gamma_3$	0.25	0.80	0.70	1.85	3.50
c,S	0	$\Gamma_1$	5.15	5.20	4.85	4.95	5.90
		$\Gamma_2$	5.00	4.40	4.20	4.65	5.45
		$\Gamma_3$	6.00	5.90	6.30	6.15	5.40
c,S	1	$\Gamma_1$	0.55	1.80	2.10	2.65	4.60
		$\Gamma_2$	0.95	1.45	1.70	2.85	4.35
		$\Gamma_3$	0.00	0.00	0.10	0.65	1.15
c,S	2	$\Gamma_1$	0.60	1.50	2.15	2.95	4.10
		$\Gamma_2$	0.80	1.10	1.70	2.65	4.10
		$\Gamma_3$	0.00	0.00	0.00	0.35	0.55
c,S,t	0	$\Gamma_1$	5.15	5.10	5.20	4.10	5.00
		$\Gamma_2$	4.90	4.55	4.40	4.75	5.30
		$\Gamma_3$	5.55	4.85	6.00	6.35	5.20
c,S,t	1	$\Gamma_1$	0.30	0.60	1.50	2.15	2.75
		$\Gamma_2$	0.30	0.35	0.30	1.30	2.90
		$\Gamma_3$	0.00	0.00	0.05	0.80	1.00
c,S,t	2	$\Gamma_1$	0.20	0.65	1.15	2.20	2.80
		$\Gamma_2$	0.55	0.90	1.40	2.40	4.00
		$\Gamma_3$	0.05	0.00	0.00	0.15	0.50

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 15:** Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 100$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	4.95	5.10	5.90	4.65	4.90
		$\Gamma_2$	4.90	4.55	5.40	5.65	4.80
		$\Gamma_3$	6.20	5.95	5.20	5.80	5.75
c	1	$\Gamma_1$	4.75	3.95	5.05	3.75	3.95
		$\Gamma_2$	1.85	2.55	3.10	3.50	3.30
		$\Gamma_3$	6.60	5.60	5.00	5.50	5.35
c	2	$\Gamma_1$	3.80	3.40	4.65	3.80	3.75
		$\Gamma_2$	7.15	5.45	6.50	6.05	5.45
		$\Gamma_3$	8.20	6.80	5.85	5.90	5.80
c,t	0	$\Gamma_1$	4.85	4.30	4.90	4.55	4.95
		$\Gamma_2$	4.90	4.80	5.20	5.25	4.75
		$\Gamma_3$	6.00	5.85	5.20	5.90	5.65
c,t	1	$\Gamma_1$	2.95	3.25	3.30	3.65	4.15
		$\Gamma_2$	0.50	0.90	0.75	2.00	2.35
		$\Gamma_3$	0.00	0.05	0.10	6.50	1.45
c,t	2	$\Gamma_1$	2.90	3.20	4.45	4.50	4.75
		$\Gamma_2$	7.80	6.00	6.70	6.00	5.35
		$\Gamma_3$	0.00	0.20	0.15	1.00	2.35
c,S	0	$\Gamma_1$	5.70	4.95	5.95	4.90	4.85
		$\Gamma_2$	5.40	4.55	5.40	5.00	3.95
		$\Gamma_3$	3.95	5.20	5.00	5.00	5.15
c,S	1	$\Gamma_1$	0.15	0.70	1.70	1.80	2.60
		$\Gamma_2$	0.40	0.70	1.50	1.55	2.05
		$\Gamma_3$	0.00	0.00	0.00	0.05	0.05
c,S	2	$\Gamma_1$	0.20	0.35	1.15	1.65	2.45
		$\Gamma_2$	0.20	0.40	1.10	1.60	1.90
		$\Gamma_3$	0.00	0.00	0.00	0.00	0.25
c,S,t	0	$\Gamma_1$	5.25	4.30	4.85	4.55	4.70
		$\Gamma_2$	5.05	4.55	5.65	5.20	3.90
		$\Gamma_3$	4.40	5.15	5.45	5.30	5.20
c,S,t	1	$\Gamma_1$	0.00	0.30	0.50	1.40	2.20
		$\Gamma_2$	0.00	0.00	0.15	0.50	0.90
		$\Gamma_3$	0.00	0.00	0.00	0.05	0.50
c,S,t	2	$\Gamma_1$	0.00	0.30	0.60	1.15	1.80
		$\Gamma_2$	0.10	0.45	1.05	1.35	2.00
		$\Gamma_3$	0.00	0.00	0.00	0.00	0.20

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 16:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 5$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	8.85	11.35	13.75	22.60	54.65
		$\Gamma_2$	36.90	57.40	70.35	90.60	99.75
		$\Gamma_3$	22.40	44.25	60.70	89.50	99.90
c	1	$\Gamma_1$	7.75	10.15	11.25	20.65	49.65
		$\Gamma_2$	28.45	46.90	60.15	85.80	99.35
		$\Gamma_3$	19.35	38.80	55.35	87.35	99.90
c	2	$\Gamma_1$	8.30	10.30	10.75	20.60	48.55
		$\Gamma_2$	32.45	50.45	62.85	86.30	99.25
		$\Gamma_3$	17.25	33.25	47.05	78.55	99.35
c,t	0	$\Gamma_1$	7.50	8.15	8.80	9.60	23.05
		$\Gamma_2$	37.70	57.20	69.75	90.55	99.75
		$\Gamma_3$	22.90	47.00	62.10	90.50	99.90
c,t	1	$\Gamma_1$	5.45	6.30	6.95	8.90	20.50
		$\Gamma_2$	23.65	41.60	56.45	86.25	99.25
		$\Gamma_3$	5.70	24.70	41.35	70.50	99.90
c,t	2	$\Gamma_1$	6.60	6.90	6.90	7.20	20.95
		$\Gamma_2$	32.80	50.25	63.35	78.75	99.15
		$\Gamma_3$	5.30	18.65	31.25	66.45	99.00
c,S	0	$\Gamma_1$	9.45	12.40	15.60	24.00	56.60
		$\Gamma_2$	9.70	12.35	15.95	24.95	55.00
		$\Gamma_3$	10.55	16.85	22.90	38.60	77.65
c,S	1	$\Gamma_1$	5.20	7.65	9.20	18.95	48.35
		$\Gamma_2$	4.20	7.35	9.50	17.70	45.80
		$\Gamma_3$	2.00	4.10	8.55	22.05	65.60
c,S	2	$\Gamma_1$	3.95	7.05	8.00	16.75	45.40
		$\Gamma_2$	3.45	6.50	8.40	16.80	42.00
		$\Gamma_3$	1.15	1.80	4.55	12.75	49.20
c,S,t	0	$\Gamma_1$	7.65	9.20	9.45	10.30	24.90
		$\Gamma_2$	9.45	12.30	15.50	24.85	54.80
		$\Gamma_3$	35.85	17.05	22.45	39.80	78.10
c,S,t	1	$\Gamma_1$	3.25	4.15	5.35	7.20	18.80
		$\Gamma_2$	2.45	4.90	7.05	15.20	42.80
		$\Gamma_3$	9.65	4.45	8.60	22.80	66.00
c,S,t	2	$\Gamma_1$	3.30	3.20	4.20	6.10	17.80
		$\Gamma_2$	3.20	6.05	8.70	16.65	41.25
		$\Gamma_3$	5.85	1.65	3.65	11.55	46.95

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 17:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 10$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	12.65	18.15	23.75	44.15	85.30
		$\Gamma_2$	67.55	88.69	96.40	99.80	100.00
		$\Gamma_3$	34.35	68.15	85.20	99.30	100.00
c	1	$\Gamma_1$	9.15	14.95	19.20	38.30	81.35
		$\Gamma_2$	54.15	80.65	91.25	99.30	100.00
		$\Gamma_3$	26.80	62.20	80.65	98.80	100.00
c	2	$\Gamma_1$	8.95	14.75	19.20	36.20	79.35
		$\Gamma_2$	58.50	83.10	92.25	99.20	100.00
		$\Gamma_3$	22.85	52.55	69.65	97.40	100.00
c,t	0	$\Gamma_1$	8.70	9.40	10.25	16.00	41.10
		$\Gamma_2$	67.65	88.75	96.15	99.80	100.00
		$\Gamma_3$	34.10	70.60	86.70	99.50	100.00
c,t	1	$\Gamma_1$	5.15	7.35	8.05	11.95	35.05
		$\Gamma_2$	45.30	74.80	87.75	99.30	100.00
		$\Gamma_3$	6.05	39.90	65.50	97.85	100.00
c,t	2	$\Gamma_1$	5.75	6.80	7.55	11.90	33.35
		$\Gamma_2$	57.65	82.50	92.30	99.25	100.00
		$\Gamma_3$	4.95	27.60	51.10	92.45	100.00
c,S	0	$\Gamma_1$	12.70	19.50	26.25	46.75	87.05
		$\Gamma_2$	12.40	19.45	26.35	45.80	85.85
		$\Gamma_3$	13.40	25.55	34.95	61.80	95.70
c,S	1	$\Gamma_1$	4.40	10.25	14.35	34.55	79.85
		$\Gamma_2$	4.20	9.45	14.40	33.30	76.55
		$\Gamma_3$	0.75	4.20	10.55	35.95	90.70
c,S	2	$\Gamma_1$	3.40	8.70	13.35	28.45	75.35
		$\Gamma_2$	3.05	6.35	12.75	28.80	71.90
		$\Gamma_3$	0.35	1.15	3.85	19.10	76.45
c,S,t	0	$\Gamma_1$	8.55	11.20	11.65	17.20	43.70
		$\Gamma_2$	12.70	19.65	25.65	45.00	85.85
		$\Gamma_3$	13.25	25.80	34.90	62.90	96.00
c,S,t	1	$\Gamma_1$	2.40	3.90	4.65	9.85	32.75
		$\Gamma_2$	1.50	5.05	9.60	26.55	72.65
		$\Gamma_3$	1.40	4.45	10.55	36.15	91.40
c,S,t	2	$\Gamma_1$	2.45	3.15	3.65	7.80	27.70
		$\Gamma_2$	2.90	6.25	11.35	28.25	72.00
		$\Gamma_3$	0.60	1.25	2.70	16.35	73.60

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 18:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 20$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	18.35	29.75	39.80	70.90	98.90
		$\Gamma_2$	93.70	99.70	99.95	100.00	100.00
		$\Gamma_3$	50.45	91.30	98.40	100.00	100.00
c	1	$\Gamma_1$	13.70	23.20	34.50	63.50	97.65
		$\Gamma_2$	83.55	98.60	99.80	100.00	100.00
		$\Gamma_3$	41.75	86.00	97.15	100.00	100.00
c	2	$\Gamma_1$	12.95	22.50	31.60	60.80	97.05
		$\Gamma_2$	87.55	99.00	99.80	100.00	100.00
		$\Gamma_3$	35.35	76.25	92.25	100.00	100.00
c,t	0	$\Gamma_1$	11.65	12.55	14.65	24.55	65.05
		$\Gamma_2$	94.05	99.75	99.95	100.00	100.00
		$\Gamma_3$	50.40	92.65	99.75	100.00	100.00
c,t	1	$\Gamma_1$	6.05	8.95	10.00	18.05	57.10
		$\Gamma_2$	73.70	97.35	99.55	100.00	100.00
		$\Gamma_3$	6.70	61.70	89.50	100.00	100.00
c,t	2	$\Gamma_1$	5.60	9.40	9.20	17.15	53.35
		$\Gamma_2$	87.10	99.00	99.70	100.00	100.00
		$\Gamma_3$	5.50	43.45	75.85	99.75	100.00
c,S	0	$\Gamma_1$	19.65	33.65	43.90	74.55	99.15
		$\Gamma_2$	20.15	33.65	45.75	74.15	99.00
		$\Gamma_3$	20.75	40.75	54.30	86.15	100.00
c,S	1	$\Gamma_1$	4.90	14.85	24.75	57.80	97.60
		$\Gamma_2$	4.40	12.95	24.60	56.40	97.90
		$\Gamma_3$	0.60	3.95	13.65	57.80	99.40
c,S	2	$\Gamma_1$	3.40	11.00	19.10	49.85	95.35
		$\Gamma_2$	3.10	10.15	19.40	47.95	95.95
		$\Gamma_3$	0.05	0.35	2.85	28.25	96.80
c,S,t	0	$\Gamma_1$	11.00	15.10	17.30	27.70	67.65
		$\Gamma_2$	19.05	32.70	45.05	74.25	99.05
		$\Gamma_3$	19.35	41.05	54.70	87.10	100.00
c,S,t	1	$\Gamma_1$	1.55	3.55	5.10	12.85	53.10
		$\Gamma_2$	0.85	5.95	14.80	46.75	96.75
		$\Gamma_3$	0.85	4.40	14.25	58.65	99.50
c,S,t	2	$\Gamma_1$	1.05	3.50	3.70	9.45	44.20
		$\Gamma_2$	2.80	8.50	18.35	47.00	95.60
		$\Gamma_3$	0.25	0.35	2.15	22.60	96.05

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 19:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 40$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	29.90	53.30	68.80	95.00	100.00
		$\Gamma_2$	99.85	100.00	100.00	100.00	100.00
		$\Gamma_3$	76.25	99.60	100.00	100.00	100.00
c	1	$\Gamma_1$	19.25	40.95	55.90	90.25	100.00
		$\Gamma_2$	98.80	100.00	100.00	100.00	100.00
		$\Gamma_3$	63.95	98.60	100.00	100.00	100.00
c	2	$\Gamma_1$	17.75	36.90	52.90	87.90	100.00
		$\Gamma_2$	99.10	100.00	100.00	100.00	100.00
		$\Gamma_3$	53.40	96.30	99.75	100.00	91.15
c,t	0	$\Gamma_1$	14.10	17.80	21.85	41.20	100.00
		$\Gamma_2$	99.80	100.00	100.00	100.00	100.00
		$\Gamma_3$	77.05	99.60	100.00	100.00	83.60
c,t	1	$\Gamma_1$	6.45	9.50	12.50	27.95	100.00
		$\Gamma_2$	95.90	100.00	100.00	100.00	100.00
		$\Gamma_3$	7.10	88.65	99.35	100.00	80.20
c,t	2	$\Gamma_1$	5.15	9.50	12.30	26.45	100.00
		$\Gamma_2$	99.15	100.00	100.00	100.00	100.00
		$\Gamma_3$	5.00	68.00	95.70	100.00	100.00
c,S	0	$\Gamma_1$	29.40	57.15	73.35	96.20	100.00
		$\Gamma_2$	32.30	56.80	74.60	95.75	100.00
		$\Gamma_3$	29.80	64.10	81.55	98.95	99.95
c,S	1	$\Gamma_1$	5.65	23.00	42.00	86.15	100.00
		$\Gamma_2$	4.95	22.95	41.90	85.85	100.00
		$\Gamma_3$	0.30	3.95	19.10	83.90	99.95
c,S	2	$\Gamma_1$	2.80	15.40	32.55	78.75	99.95
		$\Gamma_2$	2.60	15.15	31.65	77.40	99.95
		$\Gamma_3$	0.00	0.15	2.65	48.10	92.85
c,S,t	0	$\Gamma_1$	13.90	21.00	24.95	46.30	100.00
		$\Gamma_2$	30.35	56.00	73.35	95.60	100.00
		$\Gamma_3$	26.70	63.25	81.50	99.05	79.90
c,S,t	1	$\Gamma_1$	0.85	2.30	5.20	19.55	99.95
		$\Gamma_2$	0.80	7.40	23.90	75.55	99.95
		$\Gamma_3$	0.55	3.85	20.75	84.15	100.00
c,S,t	2	$\Gamma_1$	0.35	1.00	3.00	12.45	70.65
		$\Gamma_2$	2.20	12.40	29.00	75.80	99.95
		$\Gamma_3$	0.20	0.10	1.30	38.05	99.95

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 20:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 100$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	56.70	87.95	96.85	100.00	100.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	97.65	100.00	100.00	100.00	100.00
c	1	$\Gamma_1$	35.95	73.30	90.90	100.00	100.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	92.20	100.00	100.00	100.00	100.00
c	2	$\Gamma_1$	30.95	68.95	87.90	99.85	100.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	83.55	100.00	100.00	100.00	100.00
c,t	0	$\Gamma_1$	22.70	32.15	41.55	76.20	99.90
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	98.00	100.00	100.00	100.00	100.00
c,t	1	$\Gamma_1$	6.45	13.45	21.75	56.05	99.45
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	8.70	99.70	100.00	100.00	100.00
c,t	2	$\Gamma_1$	5.05	10.95	20.00	52.20	99.35
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	4.25	94.50	100.00	100.00	100.00
c,S	0	$\Gamma_1$	59.35	91.05	98.10	100.00	100.00
		$\Gamma_2$	62.30	90.85	98.05	100.00	100.00
		$\Gamma_3$	55.95	93.35	99.50	100.00	100.00
c,S	1	$\Gamma_1$	6.00	44.85	77.10	99.95	100.00
		$\Gamma_2$	5.50	47.45	79.35	99.85	100.00
		$\Gamma_3$	0.00	4.90	37.75	99.80	100.00
c,S	2	$\Gamma_1$	2.10	27.50	62.60	99.10	100.00
		$\Gamma_2$	2.10	28.85	63.65	99.10	100.00
		$\Gamma_3$	0.00	0.05	2.10	82.95	100.00
c,S,t	0	$\Gamma_1$	22.60	37.40	48.25	81.35	100.00
		$\Gamma_2$	59.45	90.35	97.60	100.00	100.00
		$\Gamma_3$	52.20	92.60	99.45	100.00	100.00
c,S,t	1	$\Gamma_1$	0.10	1.95	5.45	37.90	98.90
		$\Gamma_2$	0.45	14.25	49.95	98.95	100.00
		$\Gamma_3$	0.10	5.30	40.95	99.80	100.00
c,S,t	2	$\Gamma_1$	0.10	0.40	2.70	24.40	96.50
		$\Gamma_2$	1.10	22.75	58.10	98.95	100.00
		$\Gamma_3$	0.00	0.05	0.70	71.00	100.00

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 21:** Power simulation approach 2 Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 5$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	2.65	1.85	2.15	2.40	6.20
		$\Gamma_2$	61.75	84.90	93.55	99.60	100.00
		$\Gamma_3$	33.70	66.60	82.25	97.65	100.00
c	1	$\Gamma_1$	9.65	11.35	11.20	19.05	48.60
		$\Gamma_2$	29.10	46.90	60.90	86.20	99.45
		$\Gamma_3$	18.65	38.80	53.80	86.65	99.90
c	2	$\Gamma_1$	9.60	10.50	11.60	20.05	46.20
		$\Gamma_2$	33.25	50.05	63.35	86.40	99.50
		$\Gamma_3$	16.55	31.45	44.80	80.45	99.50
c,t	0	$\Gamma_1$	1.30	0.55	0.45	0.30	0.60
		$\Gamma_2$	58.70	82.90	92.65	99.25	100.00
		$\Gamma_3$	33.30	66.85	81.85	97.80	100.00
c,t	1	$\Gamma_1$	7.85	7.70	7.10	9.20	20.55
		$\Gamma_2$	24.20	41.70	56.85	84.05	99.45
		$\Gamma_3$	5.65	23.50	39.00	80.85	99.85
c,t	2	$\Gamma_1$	7.40	7.50	7.55	9.00	19.85
		$\Gamma_2$	33.45	49.45	62.90	86.55	99.50
		$\Gamma_3$	4.90	17.15	30.25	70.10	99.25
c,S	0	$\Gamma_1$	4.45	3.10	2.75	3.15	7.95
		$\Gamma_2$	22.60	39.30	53.75	77.25	96.55
		$\Gamma_3$	19.80	40.40	51.80	78.25	97.90
c,S	1	$\Gamma_1$	4.80	7.35	8.15	16.25	45.15
		$\Gamma_2$	5.00	7.25	10.90	19.15	48.80
		$\Gamma_3$	1.40	4.20	8.40	21.25	64.40
c,S	2	$\Gamma_1$	4.80	6.80	8.25	14.95	41.45
		$\Gamma_2$	4.20	5.85	9.40	17.95	44.80
		$\Gamma_3$	0.85	1.70	4.40	13.40	51.45
c,S,t	0	$\Gamma_1$	3.05	1.10	1.00	0.45	1.10
		$\Gamma_2$	19.70	36.65	50.85	75.20	96.35
		$\Gamma_3$	18.55	37.50	50.35	76.95	97.95
c,S,t	1	$\Gamma_1$	3.10	3.30	4.30	6.75	17.15
		$\Gamma_2$	2.35	4.50	7.90	16.60	44.35
		$\Gamma_3$	1.90	4.45	7.95	20.60	63.60
c,S,t	2	$\Gamma_1$	3.30	3.75	3.70	6.15	15.85
		$\Gamma_2$	3.95	5.45	8.60	17.80	44.25
		$\Gamma_3$	1.45	1.25	3.45	10.95	47.90

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 22:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 10$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	2.25	1.50	1.25	1.95	8.85
		$\Gamma_2$	91.05	99.50	99.95	100.00	100.00
		$\Gamma_3$	53.15	91.30	97.15	99.95	100.00
c	1	$\Gamma_1$	12.15	17.05	20.05	36.00	79.25
		$\Gamma_2$	53.55	81.60	93.05	99.20	100.00
		$\Gamma_3$	26.25	61.60	79.80	98.75	100.00
c	2	$\Gamma_1$	11.65	16.70	19.70	32.90	75.95
		$\Gamma_2$	58.30	83.10	93.05	99.30	100.00
		$\Gamma_3$	21.90	51.30	69.50	96.20	100.00
c,t	0	$\Gamma_1$	0.60	0.10	0.15	0.00	0.15
		$\Gamma_2$	89.25	99.30	99.95	100.00	100.00
		$\Gamma_3$	50.80	90.75	97.25	99.95	100.00
c,t	1	$\Gamma_1$	8.55	8.10	7.75	13.40	32.85
		$\Gamma_2$	44.95	75.15	89.30	98.90	100.00
		$\Gamma_3$	5.90	37.75	63.40	96.70	100.00
c,t	2	$\Gamma_1$	7.10	8.55	8.40	12.25	31.95
		$\Gamma_2$	57.90	83.00	92.85	99.20	100.00
		$\Gamma_3$	4.55	24.90	48.75	92.55	100.00
c,S	0	$\Gamma_1$	4.30	2.80	2.35	3.65	12.40
		$\Gamma_2$	36.80	65.90	81.45	96.25	100.00
		$\Gamma_3$	29.55	61.40	76.00	96.60	100.00
c,S	1	$\Gamma_1$	4.40	9.55	12.10	28.75	75.05
		$\Gamma_2$	6.05	10.80	16.30	34.05	80.35
		$\Gamma_3$	0.90	3.50	10.25	35.40	90.80
c,S	2	$\Gamma_1$	3.50	9.20	11.25	25.05	71.35
		$\Gamma_2$	4.35	9.05	13.95	30.30	76.40
		$\Gamma_3$	0.65	1.10	3.90	18.75	78.90
c,S,t	0	$\Gamma_1$	2.35	0.55	0.45	0.10	0.20
		$\Gamma_2$	30.85	60.90	78.45	95.05	100.00
		$\Gamma_3$	27.10	58.10	74.30	95.95	100.00
c,S,t	1	$\Gamma_1$	1.95	3.10	3.75	8.50	28.05
		$\Gamma_2$	2.25	6.05	10.90	27.85	76.15
		$\Gamma_3$	1.30	3.50	9.75	33.60	90.50
c,S,t	2	$\Gamma_1$	1.90	2.50	3.20	7.40	24.50
		$\Gamma_2$	3.90	7.70	13.10	28.75	76.35
		$\Gamma_3$	0.55	0.55	2.65	14.40	75.35

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 23:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 20$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	1.95	1.05	1.35	3.05	20.00
		$\Gamma_2$	99.85	100.00	100.00	100.00	100.00
		$\Gamma_3$	73.25	99.10	99.95	100.00	100.00
c	1	$\Gamma_1$	17.10	25.30	33.55	61.05	97.85
		$\Gamma_2$	86.25	99.05	99.90	100.00	100.00
		$\Gamma_3$	38.45	86.45	97.00	100.00	100.00
c	2	$\Gamma_1$	15.00	23.40	32.10	58.20	96.95
		$\Gamma_2$	89.15	99.00	99.95	100.00	100.00
		$\Gamma_3$	32.25	76.00	92.80	99.90	100.00
c,t	0	$\Gamma_1$	0.15	0.05	0.00	0.00	0.35
		$\Gamma_2$	99.30	100.00	100.00	100.00	100.00
		$\Gamma_3$	71.25	99.15	99.95	100.00	100.00
c,t	1	$\Gamma_1$	8.50	9.60	11.60	18.90	55.35
		$\Gamma_2$	76.70	97.60	99.85	100.00	100.00
		$\Gamma_3$	5.75	59.20	89.00	99.90	100.00
c,t	2	$\Gamma_1$	7.15	9.65	10.35	18.55	52.25
		$\Gamma_2$	88.55	99.00	99.90	100.00	100.00
		$\Gamma_3$	4.00	40.70	73.60	99.65	100.00
c,S	0	$\Gamma_1$	4.85	2.90	3.15	5.95	28.95
		$\Gamma_2$	56.95	88.20	96.85	100.00	100.00
		$\Gamma_3$	40.00	80.40	93.95	99.80	100.00
c,S	1	$\Gamma_1$	5.00	12.05	21.30	50.15	96.70
		$\Gamma_2$	5.90	15.95	26.15	61.45	97.55
		$\Gamma_3$	0.40	4.25	13.55	56.60	99.65
c,S	2	$\Gamma_1$	3.80	10.15	18.15	43.85	95.15
		$\Gamma_2$	3.50	11.85	21.45	54.75	96.55
		$\Gamma_3$	0.10	0.65	3.85	30.25	97.20
c,S,t	0	$\Gamma_1$	1.85	0.40	0.05	0.05	0.40
		$\Gamma_2$	48.85	85.05	95.85	100.00	100.00
		$\Gamma_3$	38.15	77.60	92.45	99.80	100.00
c,S,t	1	$\Gamma_1$	1.40	2.75	3.80	10.75	46.85
		$\Gamma_2$	1.25	7.95	16.40	51.30	96.70
		$\Gamma_3$	0.60	3.90	12.90	54.80	99.70
c,S,t	2	$\Gamma_1$	1.05	1.80	2.80	8.90	40.45
		$\Gamma_2$	2.50	10.80	19.70	53.45	96.55
		$\Gamma_3$	0.30	0.40	2.10	23.20	95.80

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 24:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 40$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	1.10	0.40	0.90	2.35	33.95
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	94.40	100.00	100.00	100.00	100.00
c	1	$\Gamma_1$	23.75	39.15	57.05	88.75	99.95
		$\Gamma_2$	98.70	100.00	100.00	100.00	100.00
		$\Gamma_3$	61.30	98.70	100.00	100.00	100.00
c	2	$\Gamma_1$	20.10	35.95	53.10	86.45	99.95
		$\Gamma_2$	99.15	100.00	100.00	100.00	100.00
		$\Gamma_3$	51.95	95.70	99.70	100.00	100.00
c,t	0	$\Gamma_1$	0.00	0.00	0.00	0.00	0.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	93.95	100.00	100.00	100.00	100.00
c,t	1	$\Gamma_1$	9.45	11.65	15.50	28.25	82.20
		$\Gamma_2$	96.50	100.00	100.00	100.00	100.00
		$\Gamma_3$	7.25	84.55	99.15	100.00	100.00
c,t	2	$\Gamma_1$	8.30	10.65	13.80	27.80	79.00
		$\Gamma_2$	99.05	100.00	100.00	100.00	100.00
		$\Gamma_3$	4.95	65.25	94.35	100.00	100.00
c,S	0	$\Gamma_1$	4.15	2.30	3.35	6.45	47.75
		$\Gamma_2$	83.10	99.15	99.95	100.00	100.00
		$\Gamma_3$	67.00	97.95	99.85	100.00	100.00
c,S	1	$\Gamma_1$	4.25	16.45	34.80	79.25	99.95
		$\Gamma_2$	6.15	27.05	46.40	89.25	100.00
		$\Gamma_3$	0.05	4.10	16.60	82.65	99.95
c,S	2	$\Gamma_1$	3.10	13.85	28.80	74.55	99.95
		$\Gamma_2$	3.30	20.30	37.65	84.20	100.00
		$\Gamma_3$	0.05	0.30	2.15	50.30	99.95
c,S,t	0	$\Gamma_1$	0.35	0.05	0.05	0.00	0.05
		$\Gamma_2$	74.70	98.25	99.95	100.00	100.00
		$\Gamma_3$	61.70	97.05	99.85	100.00	100.00
c,S,t	1	$\Gamma_1$	0.65	1.95	4.05	15.45	73.25
		$\Gamma_2$	0.75	12.45	28.60	80.35	100.00
		$\Gamma_3$	0.35	3.25	15.45	81.50	99.95
c,S,t	2	$\Gamma_1$	0.40	1.40	3.05	12.35	66.45
		$\Gamma_2$	2.25	16.95	34.20	82.55	100.00
		$\Gamma_3$	0.05	0.10	0.90	38.50	99.90

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 25:** Power simulation Rejection frequency in percent under the assumption of a nominal significance level of 5 percent for the panel dimension  $N = 100$ .

Specification	Lag	Statistic	Number of observations				
			$T = 20$	$T = 32$	$T = 40$	$T = 60$	$T = 100$
c	0	$\Gamma_1$	0.10	0.10	0.10	2.10	71.75
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	100.00	100.00	100.00	100.00	100.00
c	1	$\Gamma_1$	41.40	74.15	90.95	99.85	100.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	92.30	100.00	100.00	100.00	100.00
c	2	$\Gamma_1$	33.70	67.20	87.60	99.90	100.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	82.95	100.00	100.00	100.00	100.00
c,t	0	$\Gamma_1$	0.00	0.00	0.00	0.00	0.00
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	99.95	100.00	100.00	100.00	100.00
c,t	1	$\Gamma_1$	11.30	16.80	24.50	57.35	99.30
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	8.40	99.70	100.00	100.00	100.00
c,t	2	$\Gamma_1$	7.65	15.20	22.40	52.20	98.85
		$\Gamma_2$	100.00	100.00	100.00	100.00	100.00
		$\Gamma_3$	4.00	93.90	100.00	100.00	100.00
c,S	0	$\Gamma_1$	3.25	1.00	2.45	11.70	88.00
		$\Gamma_2$	99.45	100.00	100.00	100.00	100.00
		$\Gamma_3$	94.50	100.00	100.00	100.00	100.00
c,S	1	$\Gamma_1$	3.05	29.80	67.15	99.15	100.00
		$\Gamma_2$	8.70	51.45	83.70	99.95	100.00
		$\Gamma_3$	0.00	3.35	35.35	99.75	100.00
c,S	2	$\Gamma_1$	2.20	21.20	56.80	98.10	100.00
		$\Gamma_2$	3.35	38.35	73.45	99.70	100.00
		$\Gamma_3$	0.00	0.05	2.65	87.00	100.00
c,S,t	0	$\Gamma_1$	0.10	0.00	0.00	0.00	0.00
		$\Gamma_2$	98.55	100.00	100.00	100.00	100.00
		$\Gamma_3$	91.40	100.00	100.00	100.00	100.00
c,S,t	1	$\Gamma_1$	0.00	1.35	2.65	27.00	97.70
		$\Gamma_2$	0.20	18.70	59.15	99.30	100.00
		$\Gamma_3$	0.00	3.15	32.10	99.60	100.00
c,S,t	2	$\Gamma_1$	0.00	0.50	1.60	18.90	95.45
		$\Gamma_2$	0.15	30.20	67.60	99.60	100.00
		$\Gamma_3$	0.00	0.00	0.40	72.20	100.00

c: Test regression includes an intercept; t: Test regression includes a linear trend; S: Test regression includes three seasonal dummies.

**Table 26:** Results of the individual HEGY-tests and panel seasonal unit root tests.

Country	Specification	$\Gamma_1^i$	$\Gamma_2^i$	$\Gamma_3^i$	DW
Austria	$c, D_1, D_2, 1, 2, 4$	0.326	-2.949*	0.750	1.418
Belgium	$c, 1, 2, 4$	-2.796	-0.279	1.587	2.122
Denmark	$c, 1, 2, 4$	-2.637	0.624	1.072	2.011
Finland	$c, 1, 3$	-1.959	-0.850	0.136	2.154
France	$c, 1, 2$	-1.703	-0.941	0.941	2.043
Germany	$c, 1, 2$	-1.846	-0.239	0.551	2.046
Ireland	$c, 1, 2$	-0.221	-0.622	7.946*	1.794
Italy	$c, 1$	-2.141	-3.685*	2.598	1.854
Japan	$c, 1, 4$	0.517	-2.042*	0.733	1.933
Luxembourg	$c, 1, 3, 4$	-1.717	-5.137*	1.623	2.207
Netherlands	$c, 1, 3, 4$	-1.048	-1.323	3.565*	1.666
Portugal	$c, 1$	-3.775*	-2.948*	3.918*	1.939
Spain	$c, 1, 3$	-1.562	-3.321*	3.008	1.859
Sweden	$c, 1, 2$	-1.660	-0.833	2.397	1.999
United Kingdom	$c, 1, 2$	-1.045	-0.219	3.671*	1.866
United States	$c, 1, 2$	-1.713	-0.528	1.622	1.963
Averages		-1.561	-1.581	2.257	
Panel test	$c$	-0.296	-3.893*	3.633*	

Specification describes the choice of the deterministic terms and the lag numbers for the year-on-year-changes;  $c$ : Test regression includes an intercept;  $D_1$  Dummy-variable with unity at and zeros elsewhere,  $D_2$  Dummy-variable with unity at and zeros elsewhere. Critical values for the individual tests of HEGY. \* significant at the 5 percent level.

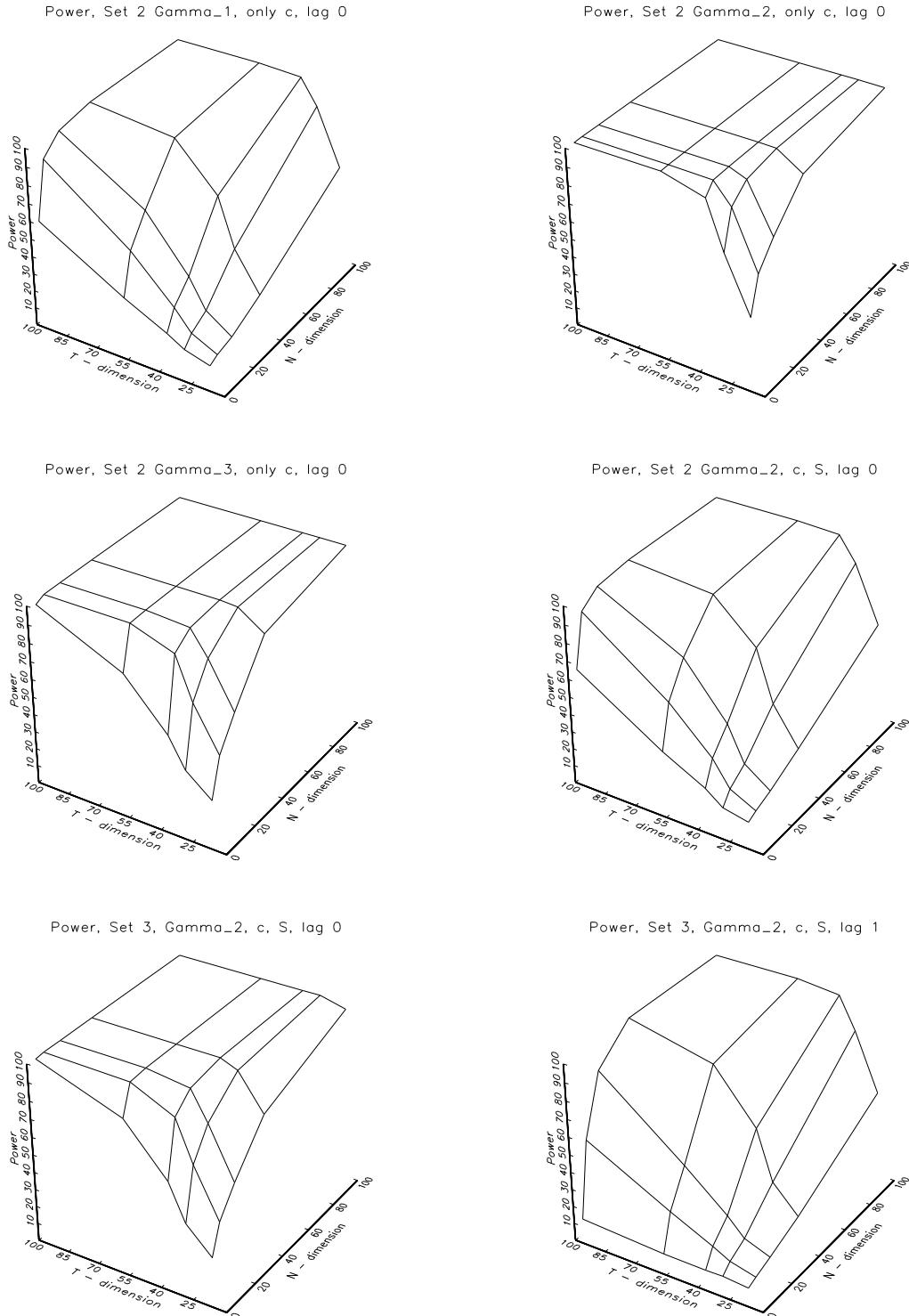


Figure 1: Power of set 2 and set 3 approaches for different cases.