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# The Economics of Open-Access Journals 

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#### Abstract

A new business model for scholarly journals, open access, has gained wide attention recently. An open-access journal's articles are available over the Internet free of charge to all readers; revenue to cover publication costs comes from authors' fees. In this paper, we present a model of the journals market. Drawing upon the emerging literature on two-sided markets, we highlight the features distinguishing journals from examples economists have previously studied (telephony, credit cards, etc.). We analyze the efficiency of equilibrium author and reader fee schedules for various industry structures and for various assumptions about journals' objective functions. We ask whether open-access journals are viable in these various economic environments.


Keywords: Open access, scholarly journal, two-sided market, competition

Journal of Economic Literature Codes: L14, L82, D40, L31

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## 1 Introduction

The typical scholarly journal earns most of its revenue from subscriber fees-fees charged to libraries and individual subscribers. Focus for the moment on library subscription fees since they constitute most of journal revenue, especially for journals published by commercial (for-profit) firms. Library subscription fees vary widely across journals and can be quite high. In economics, for example, yearly library subscription fees ranged from an average of 190 USD ( 156 EUR) for the ten top-cited journals published by non-profit publishers to 1,370 USD (1,125 EUR) for the ten top-cited journals published by commercial firms in 2001 (Bergstrom 2001). Across science and technology journals more generally, the average yearly library subscription fee, measured by the Blackwell Periodical Price Index, was 671 GBP (999 EUR) in 2000 (Wellcome Trust 2003). Recent developments in the market for journals have led to dissatisfaction among some scholars and librarians with this business model involving such high subscriber fees. ${ }^{1}$ The advent of the Internet offers the prospect of nearly zero marginal cost distribution of journals in electronic form, potentially much lower than the traditional method of mailing print copies. Yet while technological advances might be expected to result in lower journal prices, real journal prices in fact have risen substantially over the past decade. In his sample of biomedical journals published by commercial firms, McCabe (2002) found average library subscription fees more than doubled from the 1988-1994 period to the 1995-2001 period. The Blackwell Periodical Price Index for science and technology journals rose by a factor of 1.8 between 1990 and 2000 (Wellcome Trust 2003). The recent wave of mergers among commercial publishers has dramatically increased concentration in many fields: the market share of the dominant firm, Elsevier, exceeded 50 percent in biomedical journals according to some measures (McCabe 2002). McCabe (2002) provides evidence that this consolidation has directly contributed to the price increases.

This dissatisfaction with the traditional business model for journals has led to the proposal

[^0]of a new business model, the open-access model. An open-access journal's articles are available over the Internet free of charge to all readers. Revenue to cover publication costs (and generate a profit for commercial publishers) comes from fees charged to submitting authors. In June 2004, the Directory of Open Access Journals (www.doaj.org) listed over 1,100 open access titles across all fields. The most widely publicized open-access initiative is the Public Library of Science (PLoS), publishing the PLoS Biology and PLoS Medicine journals, founded by Nobel-prizewinning biologist Harold Varmus with a 9 million USD ( 7.4 million EUR) grant from the Moore Foundation, with the stated goal of competing with the top-tier journals in biomedicine. The PLoS journals charge 1,500 USD (1,230 EUR) to authors of accepted papers. This appears to be on the upper end of author fees: other notable open-access journals, for example, the BioMed Central journals, charge lower author fees, 500 USD (410 EUR) per accepted paper in the case of BioMed Central journals. In economics and business, open access has so far been limited to largely to niche publications. With one exception, the exhaustive list in of refereed journals in economics and business Table 1 all charge no author fees, so the journals operate on donated labor and computer facilities. ${ }^{2}$

The fee structure of journals has potentially important consequences for social welfare. Subscription prices have risen to the point where libraries have begun to cancel significant titles (Weiss 2003). This in turn harms both readers and authors, readers because their access to past research is limited, and authors because fewer readers will reduce their impact and citations at the margin. ${ }^{3}$

[^1]Table 1: Refereed Open-Access Journals in Business and Economics

| Economics Journals | Business Journals |
| :--- | :--- |
| African Population Stud.* | Academy of Marketing Sci. Rev. |
| Brazilian Elec. J. of Ec. | B Quest |
| Demographic Research* | Elec. J. of Bus. Ethics and Organization Stud. |
| Ec. Bulletin | J. of Elec. Commerce Research* |
| Elec. J. of Evolutionary Modeling and Ec. Dynamics | J. of Empirical Generalisations in Marketing Sci. |
| Finnish Ec. Papers | Public Administration and Management |
| Industrial Geographer | M@n@gement |
| Nova Economia | South African J. of Information Management* |

Source: June 30, 2004 download of economics or business journals from Directory of Open Access Journals (DOAJ, available on the web site www.doaj.org). Notes: From this initial set of 24 journals, the subset in this table stated positively on their web sites that journal was refereed. Journals marked with an asterisk were added to the DOAJ between March 28, 2004 and June 30, 2004, a 29 percent increase in titles in three months. The date of DOAJ listing does not necessarily correspond to the start of the journal.

Many questions surround the economics of open-access journals. First, it is not obvious that profit-maximizing journals would ever voluntarily choose to have open access. If such examples exist, they may depend on special conditions on market structure, demand, and costs. Second, it is not obvious that a journal with the objective of introducing open access would be competitively viable. If open access only leads to a slight increase in readership and impact, authors may choose to stay with traditional journals and avoid the open-access journal's higher author fees. Third, it is not obvious that social welfare is enhanced by open access. True, it reduces any deadweight loss on the reader side. But if author fees need to be raised to pay for publication costs and to provide a profit margin, it may increase deadweight loss on the author side, leading to the publication of less research.

In order to address these and other related questions, in this paper we seek to construct an elementary model of open access. Even though we seek to make the model as simple as possible, there is one complication relative to the rest of the emerging theoretical research on academic journals (McCabe 2003, Jeon and Menicucci 2003) that cannot be avoided. The rest of the
literature only considers one side of the market, focusing on library subscription fees alone. To study open access we need to model two sides of the market, author fees in addition to subscriber fees. There are bilateral benefits exerted by readers on authors and vice versa. Since authors typically cannot pay readers directly and vice versa, these bilateral benefits are externalities. The existence of these bilateral externalities prevents the full pass through of fees charged on one side of the market to the other. Thus the structure of individual fees charged to authors and readers will matter in equilibrium. The sources of these bilateral externalities are clear: on one side of the market, authors benefit from greater impact and citations and thus prefer a journal which has more readers; on the other side of the market, readers benefit from content and thus prefer journals with more articles (or, in another dimension, higher quality articles).

Our paper is part of a growing theoretical literature on two-sided markets as applied to such markets as telecommunications and payment-card systems. ${ }^{4}$ Perhaps the closest paper in this literature is Rochet and Tirole's (2003) general treatment of platform competition. Our paper differs on several formal dimensions from Rochet and Tirole (2003). In Rochet and Tirole (2003), both sides of the market can "multihome", that is, can simultaneously operate on two or more platforms. In our application, one side of the market, readers, can multihome since they can subscribe to multiple journals. The other side of the market, authors, cannot multihome. Authors cannot have the same paper published in multiple journals. Another unique feature of the journals market is that journals offer a bundle of articles/authors to readers. In Rochet and Tirole (2003), the platform mediates a single transaction between buyer and seller. These differences require new formal analysis in our paper.

Aside from the complication of two-sided markets, in other dimensions we seek to make the model as simple as possible. The model is static. Authors produce a single article of equal quality. Journals publish only one issue. The readers' benefit from additional articles

[^2]is heterogeneous across readers but is linear in the number of articles. A journal's quality is endogenously determined solely by the number of articles it publishes. Analogous to the readers' benefit from additional authors, the authors' benefit from additional readers is heterogeneous across authors but is linear in the number of readers. Costs have a simple affine structure. We leave aside the role of other market participants such as libraries, funding agencies, and editors. Still, the analysis is sufficiently complicated that we have to devote a number of sections to the general analysis of journal pricing before focusing on the questions about open-access journals of central interest. Section 2 lays out the model. Sections 3, 4, and 5 analyze in sequence the monopoly case, the social optimum, and the case of competing journals. We derive a number of general propositions in these sections, but the presence of demand discontinuities in even simple numerical examples prevents us from concentrating exclusively on results that require the existence of well-behaved interior solutions. In Section 6, we gain further insight by studying numerical examples. We step back in Section 7 and take stock of what our results imply for the questions about open access that are of central interest in this paper. Section 8 concludes.

## 2 Model

The model has three types of economic agents: journals, authors, and readers. Journals are intermediaries between authors and readers. Journals acquire articles from authors, bundle them into a journal issue, and distribute them to subscribing readers. Each article costs the journal $c^{A}$ to process, including the costs of refereeing, copy editing, typesetting, etc. The cost of distributing the articles to a single reader includes a fixed $\operatorname{cost} c^{R}$ for the bundle of articles in the journal plus a variable cost $c$ per article. The fixed cost $c^{R}$ includes the cost of servicing the reader's account and any fixed shipping and handling costs. The remaining (variable) shipping costs are embodied in $c$.

Each author produces a single article. ${ }^{5}$ Author $i$ obtains a benefit $b_{i}^{A} \in \mathbb{R}$ per reader. This term embodies a number of potential benefits. It embodies the pure enjoyment of being read by an additional reader. It embodies the benefit of being published and thus certified by a scholarly journal. Certification in this way is beneficial because it enhances the author's curriculum vitae and thus improves the author's career prospects (i.e., for tenure, promotion, outside offers, etc.). This certification benefit can be thought of as increasing with the number of readers since publication in a widely-read journal carries with it greater impact. The term $b_{i}^{A}$ also embodies the benefit from the expected number of citations by an additional reader. Citations benefit authors because they are used as a measure of impact that again affects the author's career prospects. Assume $b_{i}^{A}$ is a random variable with continuous cumulative distribution function $F^{A}$. Normalize the mass of authors to unity.

Reader $k$ obtains benefit $b_{k}^{R} \in \mathbb{R}$ per article read. This term embodies the benefit the reader obtains from the information contained in the article. The reader can read as many articles as he likes from the journals to which he subscribes. Assume $b_{i}^{R}$ is a random variable with cumulative distribution function $F^{R}$. Normalize the mass of readers to unity.

Note we have assumed a fair degree of homogeneity. There are no exogeneous differences among journals. They have identical costs. They may differ in quality but only to the extent they publish different numbers of articles, not in the quality of the articles published nor in the value added in selecting or editing them. Authors differ in the benefits they gain from publishing their articles, but their articles provide identical benefits to readers. That is, articles are of a similar quality. ${ }^{6}$ Readers differ in the benefits they gain from reading a given article, but having the

[^3]article read provides the same benefit to an author regardless of who is doing the reading. If the author benefits from the readers' citations, for example, the implicit assumption is that all readers are equally likely to cite a given author's work. In particular, it might be realistic in some settings to assume high $-b_{i}^{R}$ readers produce more citations, but for simplicity we do not pursue this extension here. We have also assumed a fair degree of linearity. An author's benefit from having his article read is linear in the number of readers. A reader's benefit is linear in the number of articles he reads.

The benefits reader provide authors and vice versa are externalities. That is, we assume there is no way for an author to pay readers for the benefit their reading confers to him. Similarly, there is no way for a reader to pay authors directly for the benefit of their articles. It may be possible for a reader to pay authors indirectly by passing subscription fees back to authors, but as will be seen we will impose an exogenous limit on these payments by assuming, as is consistent with industry practice, that journals cannot make positive payments to authors. Given that there are externalities flowing both ways in this market, it is a classic example of what the economic literature refers to as a two-sided market. See Rochet and Tirole (2002) for a discussion and review of the literature. In ordinary markets, as is taught in introductory microeconomics courses, the incidence of a tax is the same regardless of the side on which it is assessed (i.e., the seller or the buyer side). Because of the externalities, in two-sided markets, the side of the market on which a tax is assessed does have real economic effects. More to the point in our application, economic outcomes will depend on the level of author and reader fees individually, not just some

[^4]aggregation of them such as the sum.
Journal $j$ charges each author a submission fee $p_{j}^{A}$ and each reader a subscription fee $p_{j}^{R}$. Note that, following industry practice, these fees are taken to be fixed in the sense that $p_{j}^{A}$ is independent of the number of journal $j$ 's readers and $p_{j}^{R}$ is independent of the number of articles in journal $j$. Since all articles are of equal quality, it makes no difference whether $p_{j}^{A}$ is taken to be a submission fee or a fee paid conditional on acceptance since all submitted articles will be published in equilibrium. We will constrain prices $p_{j}^{A}$ and $p_{j}^{R}$ to be non-negative. Journals may subsidize authors and readers, in that prices may be set below marginal cost, but journals cannot make explicit cash transfers to authors or readers. The restriction of cash transfers appears to be nearly universal among scholarly journals. We suspect journals' strong motivation for this restriction is to avoid the appearance of corruption. It would be interesting to develop a broader model in which this restriction arises endogenously, but in this paper it is imposed exogenously.

A reader can read as many articles as he wants from a journal to which he subscribes. If $b_{k}^{R}>0$, indeed he will read all of the articles since there is a positive marginal benefit but no marginal fee to do so. Following industry practice, an author is assumed to be able to publish his article in only one journal, i.e., journals sign exclusive contracts with authors. On the other hand, readers may subscribe to multiple journals.

Next we will compute the surplus of the economic agents. Suppose journal $j$ has $n_{j}^{A}$ authors and $n_{j}^{R}$ readers. Its profit is

$$
\begin{equation*}
p_{j}^{A} n_{j}^{A}+p_{j}^{R} n_{j}^{R}-T C\left(n_{j}^{A}, n_{j}^{R}\right) \tag{1}
\end{equation*}
$$

where $T C\left(n_{j}^{A}, n_{j}^{R}\right)$ is the total cost function

$$
\begin{equation*}
T C\left(n_{j}^{A}, n_{j}^{R}\right)=c^{A} n_{j}^{A}+c^{R} n_{j}^{R}+c n_{j}^{A} n_{j}^{R} . \tag{2}
\end{equation*}
$$

If author $i$ submits his article to journal $j$, he obtains net surplus

$$
\begin{equation*}
n_{j}^{R} b_{i}^{A}-p_{j}^{A} \tag{3}
\end{equation*}
$$

If reader $k$ subscribes to journal $j$, he obtains net surplus

$$
\begin{equation*}
n_{j}^{A} b_{k}^{R}-p_{j}^{R} \tag{4}
\end{equation*}
$$

The existence of the infinitesimal players (authors and readers) generates a multiplicity of subgame-perfect, rational-expectations equilibria supported in many cases by "bizarre" coordination behavior. For example, with a monopoly journal there can exist a rational-expectations equilibrium with marginal-cost pricing. The equilibrium is supported by author and reader strategies of refusing to deal with the journal unless the journal prices at marginal cost. The journal cannot make positive profit so it may as well price at cost. There is no incentive for an author (respectively, a reader) to deviate unilaterally if the journal charges higher prices since it obtains no surplus from dealing with a journal with no readers (respectively, authors). Similarly, with competing journals, there are rational-expectations equilibria in which all submitters and subscribers deal with a journal even though it has higher submission and subscription prices. Again, there is no incentive for an author or a reader to deviate unilaterally since the other journal has no customers and thus provides no surplus. We say that such equilibria are supported by "bizarre" coordination behavior because the infinitesimal players are coordinating on an outcome that is Pareto dominated by another. We thus will strengthen our subgame-perfect, rational-expectations equilibrium concept to require the infinitesimal players to pursue strategies leading to Paretoundominated outcomes for the coalition of all infinitesimal players on any proper subgame and to require journals' strategies to be immune to deviations that would be profitable for some Pareto-undominated response by the infinitesimal players.

## 3 Monopoly Journal

In this section, we will analyze the case of a single, monopoly journal. We will drop subscript $j$ on journals for now. Author $i$ will submit his article to the journal if his surplus given in expression (3) is positive, or, upon rewriting, if $b_{i}^{A}>p^{A} / n^{R}$. Recalling the mass of authors has been normalized to one, the structural equation for authors' demand is

$$
\begin{equation*}
n^{A}=1-F^{A}\left(p^{A} / n^{R}\right) \tag{5}
\end{equation*}
$$

Reader $k$ will subscribe to the journal if his surplus in (4) is positive, or, upon rewriting, if $b_{k}^{R}>p^{R} / n^{A}$. Recalling the mass of authors has been normalized to one, the structural equation for readers' demand is

$$
\begin{equation*}
n^{R}=1-F^{R}\left(p^{R} / n^{A}\right) . \tag{6}
\end{equation*}
$$

For brevity, we will nest equations (5) and (6) as follows (and use a similar convention for the notation throughout the remainder of the paper):

$$
\begin{equation*}
n^{x}=1-F^{x}\left(p^{x} / n^{y}\right) \tag{7}
\end{equation*}
$$

for $x, y \in\{A, R\}, x \neq y$. Solving the system of equations in (7) simultaneously yields reducedform solutions for demand

$$
\begin{equation*}
\hat{n}^{x}\left(p^{x}, p^{y}\right)=\sup \left\{n \mid G^{x}\left(n, p^{x}, p^{y}\right)=0\right\} \tag{8}
\end{equation*}
$$

where

$$
\begin{equation*}
G^{x}\left(n, p^{x}, p^{y}\right)=1-F^{x}\left(\frac{p^{x}}{1-F^{y}\left(p^{y} / n\right)}\right)-n \tag{9}
\end{equation*}
$$

for $x, y \in\{A, R\}, x \neq y$.


Figure 1: Discontinuities exhibited by reduced-form author demand in numerical example with uniformly-distributed benefits.

The reduced-form demands have straightforward comparative static properties. For example, authors' demand $\hat{n}^{A}\left(p^{A}, p^{R}\right)$ is of course weakly decreasing in submission fees $p^{A}$. Authors' demand and also weakly decreasing in subscription fees $p^{R}$. This is because authors anticipate that high subscription fees reduce the number of readers and thus the benefit authors obtain from publishing in the journal. Deriving these comparative statics results is complicated by the fact that the equation $G^{x}\left(n, p^{x}, p^{y}\right)=0$ embedded in the definition of $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ in (8) may have multiple solutions for $n$, and these solutions may vary discontinuously with $p^{x}$ and $p^{y}$.

The possibility of discontinuous demands is demonstrated in Figure 1, which graphs author demand in a numerical example in which $F^{A}$ and $F^{R}$, the distributions of author and reader benefits, are taken to be uniform $[0,1]$. Increasing $p^{A}$ above a certain threshold causes author
demand to jump down to zero as the feedback between reductions in submitters and subscribers causes the market to unravel.

Comparative statics results can still be obtained in this setting using the results of Milgrom and Roberts (1994). The proof of Proposition 1 and all subsequent propositions are provided in the Appendix.

Proposition 1. Monopoly demand $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ is weakly decreasing in prices $p^{x}$ and $p^{y}$ for all $x, y \in\{A, R\}, x \neq y$.

The monopoly journal maximizes profit given by expression (1), substituting $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ for demands for both $x=A$ and $x=R$. Call this profit $\Pi^{m}\left(p^{A}, p^{R}\right)$. As mentioned above, demands $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ may not be continuous. To build intuition, however, for now suppose demands are continuous, indeed are differentiable, and the monopoly optimum is given by an interior solution. Suppress the arguments of the demand functions for brevity. Let $M C^{x}$ be the effective marginal cost of adding a customer on side $x \in\{A, R\}$ of the market. From (2), $M C^{x}=c^{x}+c \hat{n}^{y}$. The first-order conditions for the optimum are

$$
\begin{equation*}
\hat{n}^{x}+\left(p^{x}-M C^{x}\right) \frac{\partial \hat{n}^{x}}{\partial p^{x}}+\left(p^{y}-M C^{y}\right) \frac{\partial \hat{n}^{y}}{\partial p^{x}}=0 \tag{10}
\end{equation*}
$$

for all $x, y \in\{A, R\}, x \neq y$. The first-order conditions in (10) resemble the usual ones for a multiproduct monopolist with interdependent demands. They can be rewritten in the form of a Lerner index building on Tirole (1988, p. 70). Define the Lerner index $L^{x}=\left(p^{x}-M C^{x}\right) / p^{x}$ and demand elasticity $\epsilon^{x y}=\left(\partial \hat{n}^{x} / \partial p^{y}\right) /\left(\hat{n}^{x} / p^{y}\right)$ for $x, y \in\{A, R\}$. It follows that

$$
\begin{equation*}
L^{x}=\frac{1}{\left|\epsilon^{x x}\right|}\left[1+L^{y} \epsilon^{y x}\left(\frac{p^{y} \hat{n}^{y}}{p^{x} \hat{n}^{x}}\right)\right] \tag{11}
\end{equation*}
$$

Proposition 1 implies $\epsilon^{y x} \leq 0$ for all $x, y \in\{A, R\}$. This in turn implies our monopoly journal prices as would a multiproduct monopolist producing complementary goods, here, authors and readers. The journal shades the submission fee $p^{A}$ down somewhat from the single-product

Lerner index formula to take account of the effect that increasing the number of articles increases the number of readers. Similar reasoning holds for the subscription fee $p^{R}$. ${ }^{7}$

Equation (11) indicates that a monopoly journal will typically charge prices strictly above marginal cost for both authors and readers. The monopolist typically seeks to extract rent from both sides of the market. The exception are cases in which the demand on one side of the market, say readers, has a negative cross-price elasticity with respect to author fees, and the revenue from readers' fees is much less than from authors (note the revenue-ratio term in equation (11)). The monopolist would then subsidize readers in order to extract more rent from the "important" side of the market, authors.

## 4 Social Optimum

As a benchmark, we will analyze the second-best problem for a social planner. The second best maximizes the sum of consumer and producer surplus subject to a break-even constraint for the firm. Continue to suppose that demands $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ are differentiable and the social planner's problem has an interior optimum. The Lagrangian associated with this constrained optimization problem is

$$
\begin{equation*}
\int_{p^{A} / \hat{n}^{R}}^{\infty} \hat{n}^{R} b d F^{A}(b)+\int_{p^{R} / \hat{n}^{A}}^{\infty} \hat{n}^{A} b d F^{R}(b)-T C\left(\hat{n}^{A}, \hat{n}^{R}\right)+\lambda \Pi^{m}\left(p^{A}, p^{R}\right) \tag{12}
\end{equation*}
$$

where $\lambda \in \mathbb{R}^{+}$is the Lagrange multiplier, and where we have continued to suppress the arguments of the demand functions for brevity. Let $V^{x}\left(p^{x}, p^{y}\right)$ be the benefit from adding a customer on side $x \in\{A, R\}$ of the market averaged across the population of consumers on the other side of

[^5]the market, $y \in\{A, R\}, y \neq x$ :
\[

$$
\begin{equation*}
V^{x}\left(p^{x}, p^{y}\right)=\int_{p^{y} / \hat{n}^{x}}^{\infty} b d F^{y}(b) . \tag{13}
\end{equation*}
$$

\]

Then the first-order conditions associated with Lagrangian (12) are

$$
\begin{equation*}
\lambda \hat{n}^{x}+\left[(1+\lambda)\left(p^{x}-M C^{x}\right)+V^{x}\right] \frac{\partial \hat{n}^{y}}{\partial p^{x}}+\left[(1+\lambda)\left(p^{y}-M C^{y}\right)+V^{y}\right] \frac{\partial \hat{n}^{y}}{\partial p^{x}}=0 \tag{14}
\end{equation*}
$$

for $x, y \in\{A, R\}, x \neq y$. Equation (14) can be rearranged into a Lerner index formula:

$$
\begin{equation*}
L^{x}=\frac{1}{\left|\epsilon^{x x}\right|}\left\{\frac{\lambda}{1+\lambda}+\epsilon^{y x}\left[L^{y}+\frac{V^{y}}{(1+\lambda) p^{y}}\right]\left(\frac{p^{y} \hat{n}^{y}}{p^{x} \hat{n}^{x}}\right)\right\}-\frac{V^{x}}{(1+\lambda) p^{x}} . \tag{15}
\end{equation*}
$$

Equation (15) nests both the first best (by letting $\lambda \rightarrow 0$ ) and the monopoly problem (by letting $\lambda \rightarrow \infty$ ). Equation (15) is readily interpretable. If one were to ignore the terms $V^{A}$ and $V^{R}$, one would have the usual Ramsey pricing formula. The inclusion of $V^{A}$ and $V^{R}$ reflects the positive externalities exerted by each side of the market on the other. The higher is $V^{A}$, for example, the greater the externality exerted by authors on readers, and thus the higher the markup on subscription fees to pay for a reduced markup on submission fees. Because, as can be demonstrated from equation (2), the total cost function exhibits nondecreasing ray average cost, markups in equation (15) can be negative. Indeed, if the zero-profit constraint binds, at least one of the second-best markups $L^{A}$ or $L^{R}$ from (15) will be nonpositive.

## 5 Competing Journals

In this section, suppose there are two identical journals $j=1,2$ which choose prices $p_{j}^{A}$ and $p_{j}^{R}$ simultaneously prior to the submission and subscription decisions of authors and readers. Recall our equilibrium concept involves the refinement that the coalition of infinitesimal players (authors
and readers) cannot coordinate on a Pareto-dominated outcome given journal prices. We will also focus for the moment on symmetric equilibria. By symmetry we mean equal journal prices. The next proposition shows that our refinement is inconsistent with full symmetry in the sense of equal journal prices and equal quantities. The reason is that, rather than dividing themselves (in particular the authors) across two journals, the coalition can benefit by coordinating on one of the two. Our refinement thus requires that all submitters and subscribers coordinate on a single journal ex post.

Proposition 2. In the symmetric-price equilibrium of the duopoly journal game under the refinement we consider, submitters and subscribers coordinate on a single journal ex post, though they can randomize between the journals ex ante.

Our game resembles the standard Bertrand game in that we have two firms choosing prices simultaneously for homogeneous products. The difference is that here firms are intermediaries between two markets rather than serving a single one. Still, the usual undercutting arguments used to prove firms earn zero profits in the standard Bertrand game apply here, with one slight wrinkle involving demand discontinuities.

Proposition 3. In the symmetric-price equilibrium of the duopoly journal game under the refinement we consider, equilibrium prices $\left(p^{A *}, p^{R *}\right)$ satisfy

$$
\begin{equation*}
\Pi^{M}\left(p^{A *}, p^{R *}\right)=0 \tag{16}
\end{equation*}
$$

if monopoly demands $\hat{n}^{x}\left(p^{x}, p^{y}\right), x, y \in\{A, R\}, x \neq y$, are continuous at $\left(p^{A *}, p^{R *}\right)$. That is, equilibrium prices are such that a single journal serving market demand at those prices would earn zero profit. Ex post, one of the two journals serves all submitters and subscribers and both journals earn zero profit. If monopoly demands are discontinuous at $\left(p^{A *}, p^{R *}\right)$, journals may earn positive expected profit in equilibrium.

In the standard Bertrand game, there is only one equilibrium outcome, marginal-cost pricing for the single good, yielding zero profit. With two prices here, there may be a continuum of prices satisfying the zero-profit condition (16). Unlike the standard Bertrand game, therefore, here we potentially have a continuum of equilibria.

To characterize a subset of this continuum, some notation is in order. Let $Z$ be the set of prices providing a stand-alone journal with zero profit:

$$
Z=\left\{\left(p^{A}, p^{R}\right) \in \mathbb{R}_{+}^{2} \mid \Pi^{m}\left(p^{A}, p^{R}\right)=0\right\} .
$$

Define the "greater than" sign for vectors as follows: $\left(x_{i}^{\prime}\right)_{i=1}^{n}>\left(x_{i}^{\prime \prime}\right)_{i=1}^{n}$ implies $x_{i}^{\prime} \geq x_{i}^{\prime \prime}$ for all $i=1, \ldots, n$ with at least one inequality strict. Let $\underline{Z}$ be the following subset of $Z$ :

$$
\underline{Z}=\left\{\begin{array}{l|l}
\left(p^{A}, p^{R}\right) \in Z & \begin{array}{l}
\text { there exists no }\left(p^{A^{\prime}}, p^{R^{\prime}}\right) \in Z \text { such that } \\
\left(\hat{n}^{A}\left(p^{A^{\prime}}, p^{R^{\prime}}\right), \hat{n}^{R}\left(p^{R^{\prime}}, p^{A^{\prime}}\right)\right)>\left(\hat{n}^{A}\left(p^{A}, p^{R}\right), \hat{n}^{R}\left(p^{R}, p^{A}\right)\right)
\end{array}
\end{array}\right\},
$$

i.e., $\underline{Z}$ is the subset of $Z$ whose elements are associated with quantities that are not less than (in the vector sense) the quantities associated with some other element of $Z$. We have the following proposition.

Proposition 4. For all $\left(p^{A}, p^{R}\right) \in \underline{Z}$, there exists an equilibrium of the duopoly journal game satisfying the refinement we consider in which both journals charge $\left(p^{A}, p^{R}\right)$.

The next proposition shows the second best will typically be an equilibrium in our model with competing journals.

Proposition 5. Suppose the journal's zero-profit constraint binds in the second-best social optimum. There exists an equilibrium of the duopoly journal game satisfying the refinement we consider in which both firms charge the prices observed in the second best.

Thus far, we have restricted attention to equilibria in which the journals choose the same prices, i.e., symmetric equilibria. There also may exist many asymmetric equilibria as the next proposition shows.

Proposition 6. Consider two elements $\left(p^{A^{\prime}}, p^{R^{\prime}}\right),\left(p^{A^{\prime \prime}}, p^{R^{\prime \prime}}\right) \in \underline{Z}$ such that $\Pi^{M}\left(p^{A^{\prime}}, p^{R^{\prime}}\right)=$ $\Pi^{M}\left(p^{A^{\prime \prime}}, p^{R^{\prime \prime}}\right)$. There exists an equilibrium of the duopoly journal game satisfying the refinement we consider in which one journal charges $\left(p^{A^{\prime}}, p^{R^{\prime}}\right)$ and the other $\left(p^{A^{\prime \prime}}, p^{R^{\prime \prime}}\right)$. This equilibrium is asymmetric if $\left(p^{A^{\prime}}, p^{R^{\prime}}\right) \neq\left(p^{A^{\prime \prime}}, p^{R^{\prime \prime}}\right)$.

## 6 Numerical Examples

As demonstrated by the demand curves in Figure 1, there may be demand-curve discontinuities even in the simplest examples with uniformly-distributed benefits, so that the assumptions behind our Lerner index formulae (11) and (15) may not hold. In this section we analyze simple numerical examples in which we can account for any discontinuities to verify the previous results and derive additional intuition.

Start by assuming the distributions of author and reader benefits, $F^{x}, x \in\{A, R\}$, are symmetric, both being uniform distributions on $[0,1]$ (we will consider the case of asymmetric distributions of benefits below). Table 2 presents results from three different cost configurations for this example. We chose the configuration in Example $1\left(c^{A}=0.1, c^{R}=0.1, c=0\right)$ to make authors and readers completely symmetric in terms of benefits and costs. This is for pedagogical purposes, but may capture the print-journal case in which there is a fixed cost of producing an issue of a journal and of shipping it to a reader that does not depend much on the number of articles/pages it contains. Example $2\left(c^{A}=0.1, c^{R}=0.0, c=0.1\right)$ is meant to capture cost conditions in a print-journal environment where the cost of producing and shipping an issue to a reader depends linearly on the number of articles/pages. Example $3\left(c^{A}=0.1, c^{R}=0.0\right.$, $c=0.0$ ) is meant to capture cost conditions in an online-journal environment. Most costs in this environment have to do with processing the articles and posting them on the Internet. There are nearly zero marginal costs of serving readers. It is Example 3 that will be most useful in addressing the question of open access. In all examples, we have assumed the same author cost $c^{A}=0.1$. Details on the formulae and computations used in the examples is provided in the Appendix.

We see in each of Examples 1-3 that the monopoly journal prices significantly above marginal cost. Social welfare is only about half that in the first best.

There are a range of equilibria in the case of competing journals. The table exhibits the

Table 2: Numerical Examples with Symmetric Author and Reader Benefits

|  | Monopoly | Competitive Equilibria |  | Social Optimum |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Maximizing Authors | Maximizing Readers | Second Best | First <br> Best |
| Example 1 (Equal author and reader costs): $c^{A}=0.1, c^{R}=0.1, c=0.0$ |  |  |  |  |  |
| Submission Fee | 0.237 | 0.000 | 0.230 | 0.100 | 0.000 |
| Subscription Fee | 0.237 | 0.230 | 0.000 | 0.100 | 0.000 |
| Number Authors | 0.612 | 1.000 | 0.770 | 0.887 | 1.000 |
| Number Readers | 0.612 | 0.770 | 1.000 | 0.887 | 1.000 |
| Industry Profit | 0.168 | 0.000 | 0.000 | 0.000 | -0.200 |
| Consumer Surplus | 0.229 | 0.682 | 0.682 | 0.699 | 1.000 |
| Social Welfare | 0.398 | 0.682 | 0.682 | 0.699 | 0.800 |
| Example 2 (Print journals case): $c^{A}=0.1, c^{R}=0.0, c=0.1$ |  |  |  |  |  |
| Submission Fee | 0.317 | 0.000 | 0.200 | 0.172 | 0.000 |
| Subscription Fee | 0.170 | 0.230 | 0.000 | 0.022 | 0.000 |
| Number Authors | 0.536 | 1.000 | 0.800 | 0.824 | 1.000 |
| Number Readers | 0.682 | 0.770 | 1.000 | 0.974 | 1.000 |
| Industry Profit | 0.196 | 0.000 | 0.000 | 0.000 | -0.200 |
| Consumer Surplus | 0.222 | 0.682 | 0.720 | 0.721 | 1.000 |
| Social Welfare | 0.418 | 0.682 | 0.720 | 0.721 | 0.800 |
| Example 3 (Online journals case): $c^{A}=0.1, c^{R}=0.0, c=0.0$ |  |  |  |  |  |
| Submission Fee | 0.304 | 0.000 | 0.100 | 0.100 | 0.000 |
| Subscription Fee | 0.164 | 0.113 | 0.000 | 0.000 | 0.000 |
| Number Authors | 0.573 | 1.000 | 0.900 | 0.900 | 1.000 |
| Number Readers | 0.713 | 0.887 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.234 | 0.000 | 0.000 | 0.000 | -0.100 |
| Consumer Surplus | 0.263 | 0.837 | 0.885 | 0.855 | 1.000 |
| Social Welfare | 0.497 | 0.837 | 0.885 | 0.855 | 0.900 |

Note: Author and reader benefits are uniformly distributed on $[0,1]$.


Figure 2: Continuum of competitive equilibria in three numerical examples with uniformly-distributed benefits. In each example, A is the equilibrium maximizing authors' demand, R is the equilibrium maximizing readers' demand, and T is the equilibrium maximizing consumer (i.e., author plus reader) surplus.
two endpoints of the set. Figure 2 graphs the entire set for each of the three examples. The equilibrium maximizing the number of authors puts all the fees on the reader side and the equilibrium maximizing the number of readers puts all the fees on the author side. Recall that we have exogenously limited prices to be positive; it is conceivable that if we did not add this constraint, there would be additional equilibria in which yet larger reader fees went toward positive payments for authors and vice versa. The equilibrium maximizing the number of readers involves open access in all three examples. It tends to give higher social welfare than the equilibrium maximizing the number of authors and yields surplus close to that in the second best. Indeed,
the equilibrium maximizing the number of readers coincides with the second best in Example 3, the example capturing the online-journals case.

Several additional notes about the results are in order. Note that most of the subscription fees are seen to fall in Table 2 when the reader cost is reduced from $c^{R}=0.1$ in Example 1 to $c^{R}=0$ in Example 2 and 3. Subscription fees fall because the effective marginal cost of adding a reader, $M C^{R}$, falls with a reduction in $c^{R}$, and the lower cost is reflected in lower prices. For instance, in the monopoly case in Example 1, $M C^{R}=0.1$ compared to $M C^{R}=0.054$ in the monopoly case in Example 2. ${ }^{8}$

It comes as no surprise that the fees in the first best are less than marginal costs. The journal can be subsidized in the first best and does not need to cover costs. It is more surprising that fees in the second best can also be less than marginal costs. In the second best in Example 2, one can calculate $M C^{A}=0.197$ and $M C^{R}=0.082$, so both submission fee $(0.172)$ and the subscription fee ( 0.022 ) are less than the corresponding author and reader effective marginal costs. Recall from our discussion following equation (15) that the markup over marginal cost in the second best need not be positive because the cost function exhibits increasing ray average costs, and so price can be less than marginal cost and still have revenue cover total costs.

Next, we will consider numerical examples for the case of asymmetric author and reader benefits. Table 3 provides a set of examples in which author benefits exceed reader benefits. Specifically, the unit mass of authors all have benefit $b_{i}^{A}=1$ per reader. Readers have uniformly distributed benefits on $[0,1]$ per author/article as before. This is a particularly convenient specification because all authors turn out to submit articles in equilibrium, so only one side of the market (readers) has nontrivial demand, alleviating the need to solve a complicated fixed-point problem to compute demands. The cost configurations are the same as in Table 2. The Appendix

[^6]Table 3: Numerical Examples with Large Author Relative to Reader Benefits

|  |  | Social Optimum |  |
| :---: | :---: | :---: | :---: |
| Monopoly | Competitive Equilibrium | Second Best | First <br> Best |

Example 4 (Equal author and reader costs): $c^{A}=0.1, c^{R}=0.1, c=0.0$

| Submission Fee | 0.950 | 0.200 | 0.200 to 1.000 | 0.000 to 1.000 |
| :--- | :---: | :---: | :---: | :---: |
| Subscription Fee | 0.050 | 0.000 | 0.000 | 0.000 |
| Number Authors | 1.000 | 1.000 | 1.000 | 1.000 |
| Number Readers | 0.950 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.803 | 0.000 | 0.000 to 0.800 | -0.200 to 0.800 |
| Consumer Surplus | 0.451 | 1.300 | 1.300 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.254 | 1.300 | 1.300 | 1.300 |

Example 5 (Print journals case): $c^{A}=0.1, c^{R}=0.0, c=0.1$

| Submission Fee | 0.950 | 0.200 | 0.200 to 1.000 | 0.000 to 1.000 |
| :--- | :---: | :---: | :---: | :---: |
| Subscription Fee | 0.050 | 0.000 | 0.000 | 0.000 |
| Number Authors | 1.000 | 1.000 | 1.000 | 1.000 |
| Number Readers | 0.950 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.803 | 0.000 | 0.000 to 0.800 | -0.200 to 0.800 |
| Consumer Surplus | 0.451 | 1.300 | 1.300 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.254 | 1.300 | 1.300 | 1.300 |

Example 6 (Online journals case): $c^{A}=0.1, c^{R}=0.0, c=0.0$

| Submission Fee | 1.000 | 0.100 | 0.100 to 1.000 | 0.000 to 1.000 |
| :--- | :---: | :---: | :---: | :---: |
| Subscription Fee | 0.000 | 0.000 | 0.000 | 0.000 |
| Number Authors | 1.000 | 1.000 | 1.000 | 1.000 |
| Number Readers | 1.000 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.900 | 0.000 | 0.000 to 0.900 | -0.100 to 1.000 |
| Consumer Surplus | 0.500 | 1.400 | 1.400 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.400 | 1.400 | 1.400 | 1.400 |

Notes: Unit mass of authors have equal benefit, $b_{i}^{A}=1$ for all $i$, per reader. Readers' benefits are uniformly distributed on $[0,1]$. There are a continuum of first and second-best optima, as indicated by the intervals.
provides details on the formulae and computations used in these examples.
Relative to the case of symmetric author and reader benefits in Table 2, in Table 3 the monopoly journal raises the price charged the high-and-inelastic-demand side of the market (authors) and lowers the price charged to the other side of the market (readers). Indeed, in Example 6 the monopoly journal uses an open-access regime. Though reducing subscription fees lowers the revenue extracted from readers, readers exert such a large positive externality on authors that this decline in revenue is more than offset by the increase in submission fees the monopoly journal can charge when more readers are expected to subscribe. This result bears out what we saw in the Lerner index formula in (11). Equation (11) shows that the markup should be adjusted up for the side of the market with inelastic demand (c.f. $\left|\epsilon^{x x}\right|$ in the denominator of the first factor) and also should be adjusted up for the side of the market generating more revenue (c.f. $p^{y} \hat{n}^{y} / p^{x} \hat{n}^{x}$ in the second factor, which note is multiplied by the negative elasticity $\epsilon^{y x}$ ).

In each of Examples 4-6, the unique competitive equilibrium involves open access. Readers exert such a large positive externality on authors that only pricing schemes maximizing the number of readers can be competitively viable. The first- and second-best social optima also involve open access in all three examples. Note that there are a continuum of social optima in Examples 46. To see why there is this multiplicity, one can start from the optimum maximizing consumer surplus, raise the submission fee in a range, and not reduce the number of authors since author demand is inelastic. The increase in submission fee only transfers surplus from authors to the journal, a transfer that does not affect social welfare.

In Table 4 we take the mirror-image case in which readers have a larger benefit than authors. The unit mass of readers all have benefit $b_{k}^{R}=1$ per author/article; authors have uniformly distributed benefits on $[0,1]$. The notable result from the table is that open access does not emerge in a competitive equilibrium in any of Examples 7-9, nor is open access second-best efficient. That is, the unique competitive equilibrium in all three examples involves positive subscription fees, even in the online-journals example (Example 9). Though there are a range of

Table 4: Numerical Examples with Large Reader Relative to Author Benefits

|  |  |  | Social Optimum |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Monopoly | Competitive Equilibrium | Second Best | First <br> Best |
| Example 7 (Equal author and reader costs): $c^{A}=0.1, c^{R}=0.1, c=0.0$ |  |  |  |  |
| Submission Fee | 0.050 | 0.000 | 0.000 | 0.000 |
| Subscription Fee | 0.950 | 0.200 | 0.200 to 1.000 | 0.000 to 1.000 |
| Number Authors | 0.950 | 1.000 | 1.000 | 1.000 |
| Number Readers | 1.000 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.803 | 0.000 | 0.000 to 0.800 | -0.200,0.800 |
| Consumer Surplus | 0.451 | 1.300 | 1.300 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.254 | 1.300 | 1.300 | 1.300 |
| Example 8 (Print journals case): $c^{A}=0.1, c^{R}=0.0, c=0.1$ |  |  |  |  |
| Submission Fee | 0.050 | 0.000 | 0.000 | 0.000 |
| Subscription Fee | 0.950 | 0.200 | 0.200 to 1.000 | 0.000 to 1.000 |
| Number Authors | 0.950 | 1.000 | 1.000 | 1.000 |
| Number Readers | 1.000 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.803 | 0.000 | 0.000 to 0.800 | -0.200 to 0.800 |
| Consumer Surplus | 0.451 | 1.300 | 1.300 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.254 | 1.300 | 1.300 | 1.300 |
| Example 9 (Online journals case): $c^{A}=0.1, c^{R}=0.0, c=0.0$ |  |  |  |  |
| Submission Fee | 0.000 | 0.000 | 0.000 | 0.000 |
| Subscription Fee | 1.000 | 0.100 | 0.100 to 1.000 | 0.000 to 1.000 |
| Number Authors | 1.000 | 1.000 | 1.000 | 1.000 |
| Number Readers | 1.000 | 1.000 | 1.000 | 1.000 |
| Industry Profit | 0.900 | 0.000 | 0.000 to 0.900 | -0.100 to 0.900 |
| Consumer Surplus | 0.500 | 1.400 | 1.400 to 0.500 | 1.500 to 0.500 |
| Social Welfare | 1.400 | 1.400 | 1.400 | 1.400 |

Notes: Unit mass of readers have equal benefit, $b_{k}^{R}=1$ for all $k$, per author/article. Authors' benefits are uniformly distributed on $[0,1]$. There are a continuum of first and second-best optima, as indicated by the intervals.
second-best optima, the subscription fee is positive in all of them. Open access can be first-best efficient, but the journal earns strictly negative profit, so such an outcome would not be feasible without subsidies.

## 7 Open Access Journals

In this section, we will review what the results of our previous general analysis of journal pricing have to say about the questions surrounding open access posed in the Introduction.

The first question regards whether profit-maximizing journals would voluntarily choose open access. The theoretical results from Section 3, in particular the Lerner index formula (11), suggest that profit-maximizing monopoly journals will not voluntarily choose open access unless the elasticities line up in just the right way (presumably a rare case) or unless authors' benefits are much more important than readers'. In the numerical examples of Section 6, we saw open access never emerged with a profit-maximizing monopoly journal if authors' and readers' benefits were symmetric (Examples 1-3) or readers' benefits were higher than authors' (Examples 7-9). The monopolist charged readers substantial markups in an effort to extract revenue from all possible sources. The monopoly journal only pursued open access in Example 6, in which marginal reader costs were zero and authors' benefits were substantially higher than readers'.

Compared to the case of a profit-maximizing monopoly journal, open access emerged more often as an equilibrium with competitive journals (in essence perfectly competitive in our model). Referring to the numerical examples in Section 6, open access emerged in the equilibrium maximizing the number of readers in Examples 1-3 and emerged as the unique competitive equilibrium in Examples 4-6. Only when readers' benefits were so large relative to authors' that readers preferred authors to be subsidized to increase the number of articles published (Examples 7-9) was open access not observed in a competitive equilibrium.

In sum, if journals are profit-maximizing, we would predict open access would be more likely
to be observed the lower is journals' market power, the greater are author benefits relative to reader benefits, and the lower are the marginal cost of serving readers.

The next question regards whether journals with the objective of introducing open access can be viable in competition with profit-maximizing journals. Our numerical examples demonstrated that the answer is yes. In Examples 1-3, there was a stable equilibrium in which both firms chose open access. As Proposition 6 suggests, there may exist asymmetric equilibria in which an open-access journal competes alongside another journal that charges a different configuration of prices, involving possibly positive reader prices. To be more concrete, consider any of the three numerical examples of Section 6 and in particular any of the three equilibrium loci in Figure 2. Any outcome in which the open-access journal charges prices given by point R and the other (non-open-access) journal charges prices given by some other point on the locus of equilibria will be an equilibrium. In Examples 4-6 the unique competitive equilibrium involved open access. Authors' benefits were so high relative to readers' that non-open-access journals would not be viable in competition with open-access journals.

Our results that profit-maximizing journals with market power are less likely to choose open access than those without market power should not be construed to imply that market power prevents open access from being viable. It should be emphasized that the aforementioned result is for profit-maximizing journals only. Increasing a journal's market power increases the rents it could use to achieve objectives other than profit maximization if it so chose. In particular, if a journal were dedicated to maximizing readership, increasing its market power would facilitate its move to open access.

The final question regards the efficiency of open access. The examples indicate that open access is not universally efficient. If there are substantial costs of serving readers (Examples 1 and 2) or if readers' benefits are large relative to authors' (Examples 7-9), then the second best involves positive reader fees. However, if authors and readers have symmetric benefits and readers are costless to serve (Example 3) or authors' benefits are substantially larger than readers'
(Examples 4-6), open access is efficient. Are the conditions under which open access is secondbest efficient of practical relevance? We would argue yes, for two reasons. First, the case of symmetric author and reader benefits seems to be a reasonable benchmark; if benefits must be asymmetric, authors' benefits might plausibly be assumed to be higher than readers'. Second, the case in which readers are costless to serve corresponds to the case of online journals, precisely the environment in which open access has been advocated (open access was not a policy issue in the print-journal era). In sum, our results indicate that open access tends to be efficient in an environment in which journals are distributed over the Internet and in which readers' benefits do not swamp authors'.

We have in a sense been conservative in our assessment of both the social benefit and competitive potential of open access by ignoring an important technological advantage of open access to this point. The model assumed that the costs $c^{A}, c^{R}$, and $c$ were exogenous, independent of the journal's pricing scheme. In particular, if $c^{R}$ was assumed to be positive, it was assumed to be positive whether or not the journal was open access. One of the benefits of open access is that by posting articles on the Internet and allowing readers to access them freely, there is no need to administer reader accounts. This benefit could be modeled by supposing there is a discontinuous fall in the cost of administering a reader account from $c^{R}>0$ for a journal that charges a subscription fee, no matter how small, to $c^{R}=0$ for an open-access journal. Making this assumption on how costs change with the pricing scheme would lead open access to be socially optimal and for a wider set of parameters and to emerge as a competitive equilibrium for a wider set of parameters. For instance, the second best in Example 1 would switch from one involving positive submission and subscription fees ( 0.100 each) to an open-access regime with a submission fee of 0.100 and zero subscription fee (to see this, note the open-access cost structure would be identical to that in Example 3). Social welfare would rise from 0.699 to 0.855 .

## 8 Conclusion

There is currently an active debate between advocates of the traditional business model for scholarly journals and a new business model involving open access. Both sides have at times claimed that their preferred model is competitively more viable, and at times claimed that their preferred model is socially more efficient, than the alternative. In this paper, we provide the first attempt to bring formal economic theory to bear in the debate. We argued that a two-sided-market model is required to address questions regarding the economics of open-access journals properly. We constructed and analyzed what might be considered the most elemental version of such a model.

On a superficial level, our analysis suggests there is merit to both sides of the debate. Consider the "possibility results" derived from our numerical examples. We showed it is possible for open access to emerge in equilibrium with profit maximizing journals. This was true for various journal market structures ranging from monopoly to Bertrand competition. We showed it is possible for open access to be socially efficient. On the other hand, we demonstrated a range of cases in which open access did not emerge in equilibrium and a range of cases in which the second-best social optimum (second best in the sense journals are constrained to earn non-negative profit without external subsidy) did not involve open access.

On a deeper level, our interest is in characterizing the conditions under which open access is competitively viable and/or socially efficient. Consider the comparative statics results from our general analysis of the model assuming well-behaved interior optima, corroborated by our analysis of numerical examples which allowed for demand discontinuities and corner solutions. We found a profit-maximizing journal would be more likely to adopt open access in equilibrium

- the lower the journal's market power,
- the lower the marginal cost of serving a reader, and
- the higher the distribution of author benefits.

These comparative statics results are intuitive. The more market power the journal has, the freer it is to extract rent from both sides of the market, readers as well as authors, through high markups. Equilibrium prices at least partially reflect marginal costs for the usual reasons, so the subscription price tends to be low only if marginal reader costs are low. High author benefits are associated with low subscription prices because low subscription prices increase the quantity of readers, in turn increasing the demand of the high-value authors. For sufficiently high author relative to reader benefits, and sufficiently low marginal reader costs, there are cases in which even a monopoly journal would adopt open access, as we mentioned in the previous paragraph. Competing journals would adopt open access for a broader set of author/reader benefits and marginal reader costs.

Our second set of comparative statics results related to the conditions under which a non-profit journal which decided to adopt open access could be competitively viable. Obviously, it would be competitively viable in all the cases from the previous paragraph in which a profit-maximizing journal was found to adopt open access in equilibrium. It would also be more likely to be competitively viable the greater its market power. The journal can use the rents accruing from its market power to facilitate achieving its objectives, whether maximizing readership through open access or some other objective. Thus, while an increase in market power reduces the likelihood a profit-maximizing journal would choose open access in equilibrium, an increase in market power increases the likelihood a non-profit journal would find open access feasible.

Our last set of comparative statics results related to the conditions under which open access is socially efficient (in the sense of being part of a second-best social optimum). The set of cases in which open access is socially efficient is smaller than the set of cases in which open access emerged in a competitive equilibrium. Open access tended to be inefficient when readers' benefits were large relative to authors' or when the marginal cost of serving readers was high. The intuition again is clear. It is inefficient to have free reader access if readers are costly to
serve at the margin or if the positive externality authors exert on readers is so high that author demand should be subsidized by positive reader fees.

In the model with competing journals, our decision to have them be symmetric competitors rather than an entrant competing against an incumbent was deliberate. While it is true that most scholarly journals are not open access, and so expansion of open access will require entry, we wanted to separate pricing issues from entry issues. We recognize that there may be significant barriers to entry in the journal market, among other reasons because a journal's reputation may be based on its stock of publications and may only evolve slowly over time. Such barriers to entry are not specific to open-access journals, however; they apply to any new journal whether it use an open-access or traditional pricing scheme. Rather than positing some exogenous quality difference between journals, we were interested in a model in which any quality differences between journals emerged endogenously, in our model through the number of articles published.

In future work, it would be valuable to analyze how evolving reputations create potential barriers to entry. Although number of articles functioned somewhat as a proxy for journal quality in our model, it would also be useful to add an explicit quality dimension, since this would allow us to evaluate the claim that open-access journals will have an incentive to increase the number of articles published at the expense of quality to boost revenue. Such a model would be considerably more complicated than the present one because, to be economically interesting, it would require the reader not to be fully informed about a given article's quality, and to use the journal in which it is published as a quality signal.

## Appendix

Proof of Proposition 1: It is evident that $G^{x}\left(n, p^{x}, p^{y}\right)$ in expression (9) is weakly decreasing in $p^{x}$. Thus, by Lemma 1 of Milgrom and Roberts (1994),

$$
\sup \left\{n \mid G^{x}\left(n, p^{x}, p^{y}\right)=0\right\} \geq \sup \left\{n \mid G^{x}\left(n, p^{x}+\delta, p^{y}\right)\right\}
$$

for all $\delta \geq 0$. Therefore $\hat{n}^{x}\left(p^{x}, p^{y}\right) \geq \hat{n}^{x}\left(p^{x}+\delta, p^{y}\right)$. That is, $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ is weakly decreasing in $p^{x}$. The proof that $\hat{n}^{x}\left(p^{x}, p^{y}\right)$ is weakly decreasing in $p^{y}$ is similar.

Proof of Proposition 2: Consider a first outcome in which journals charge equal prices and both make some positive sales. Consider a move to a second outcome in which journals maintain the same prices as in the first outcome, the active submitters and subscribers from the first outcome coordinate on one of the two journals, say journal 1, and the inactive authors and readers remain out of the market. Inactive consumers are no worse off in the second outcome. Active consumers are no worse off since they pay the same prices but have at least as many consumers on the other side of the market from which to benefit. Indeed, since journal 2 made some positive sales in the first outcome, at least one side of the market will have strictly more consumers on the other side from which to benefit, and will strictly benefit from the move from the first to the second outcome.

Proof of Proposition 3: Consider the symmetric-price outcome $\left(p^{A *}, p^{R *}\right)$. Suppose demands $\hat{n}^{x}\left(p^{x}, p^{y}\right), x \in\{A, R\}, x \neq y$, are continuous at $\left(p^{A *}, p^{R *}\right)$. By Proposition 2, one of the two journals makes all the sales ex post at these prices. Thus, ex ante, there is some positive probability, $\alpha>0$, at least one of the journals, say journal 1 , makes all the sales at these prices. Journal 2's profit is thus at most $(1-\alpha) \Pi^{m}\left(p^{A *}, p^{R *}\right)$ from an ex-ante perspective.

If $\Pi^{m}\left(p^{A *}, p^{R *}\right)<0$, journal 1 can avoid the negative profit by deviating to higher prices, effectively exiting the market. Hence $\left(p^{A *}, p^{R *}\right)$ would not be an equilibrium.

If $\Pi^{m}\left(p^{A *}, p^{R *}\right)>0$, journal 1 must earn positive margins on at least one side of the market (authors or readers). Journal 2 can deviate by slightly undercutting the price on the side of the market on which journal 1 makes positive margins by $\epsilon>0$. The Pareto-optimal outcome for the coalition of authors and readers would be to all coordinate on journal 2. For small enough $\epsilon$, since monopoly demands and thus monopoly profit are continuous at ( $p^{A *}, p^{R *}$ ), journal 2 can guarantee itself a profit arbitrarily close to $\Pi^{m}\left(p^{A *}, p^{R *}\right)$, and can guarantee it earns this with probability one from an ex ante perspective. Its profit would be strictly higher than $(1-\alpha) \Pi^{m}\left(p^{A *}, p^{R *}\right)$, an upper bound on what it could earn in the outcome considered initially. Hence the proposed outcome is not an equilibrium.

Proof of Proposition 4: Suppose both journals charge $\left(p^{A}, p^{R}\right) \in \underline{Z}$; all participating customers (authors and readers) coordinate on one or the other journal if both charge $\left(p^{A}, p^{R}\right)$; and, if one journal deviates to another price vector $\left(p^{A^{\prime}}, p^{R^{\prime}}\right)$, all participating customers coordinate on the
non-deviating journal unless all participating customers' coordinating on the deviating journal Pareto dominates coordinating on the non-deviating journal for customers.

We will show these strategies form a subgame-perfect, rational-expectations equilibrium satisfying our refinement. We need to show there exists no strictly profitable deviation $\left(p^{A^{\prime}}, p^{R^{\prime}}\right)$ for a journal. Given customers' strategies, the deviation will generate zero demand, and thus not be strictly profitable, unless all participating customers coordinate on it. But if all participating customers coordinate on the deviation, it will be unprofitable if $\left(p^{A^{\prime}}, p^{R^{\prime}}\right) \notin Z$. So suppose $\left(p^{A^{\prime}}, p^{R^{\prime}}\right) \in Z$. Since $\left(p^{A}, p^{R}\right) \in \underline{Z}$, by definition of $\underline{Z}$, at least one of the following three conditions must hold regarding the relationship between $\left(p^{A}, p^{R}\right)$ and $\left(p^{A^{\prime}}, p^{R^{\prime}}\right)$ :

$$
\begin{align*}
\left(\hat{n}^{A}\left(p^{A}, p^{R}\right), \hat{n}^{R}\left(p^{R}, p^{A}\right)\right) & =\left(\hat{n}^{A}\left(p^{A^{\prime}}, p^{R^{\prime}}\right), \hat{n}^{R}\left(p^{R^{\prime}}, p^{A^{\prime}}\right)\right)  \tag{17}\\
\hat{n}^{A}\left(p^{A}, p^{R}\right) & >\hat{n}^{A}\left(p^{A^{\prime}}, p^{R^{\prime}}\right)  \tag{18}\\
\hat{n}^{R}\left(p^{R}, p^{A}\right) & >\hat{n}^{R}\left(p^{R^{\prime}}, p^{A^{\prime}}\right) . \tag{19}
\end{align*}
$$

If (17) holds, the participating customers obtain the same surplus whether coordinating on the deviating or non-deviating journal. If (18) holds, if all participating customers coordinate on the non-deviating journal, there exists an author whose private value $b_{i}^{A}$ is slightly greater than the marginal authors', and thus obtains strictly positive surplus. This author does not submit if all participating customers coordinate on the deviating journal, and obtains zero surplus then. Similarly, if (19) holds, there exists a reader who obtains positive surplus if all participating customers coordinate on the non-deviating journal but zero surplus if they coordinate on the deviating journal. In sum, if one of (17), (18), or (19) holds, all participating customers' coordinating on the deviating journal does not Pareto dominate their coordinating on the non-deviating journal. According to the strategies from the first paragraph of this proof, participating customers thus do not coordinate on the deviating journal, implying it obtains no customers, implying it earns zero profit from deviating, implying its deviation is not strictly profitable.

Proof of Proposition 5: Let $\left(p^{A *}, p^{R *}\right)$ be the price vector implementing the second best. Suppose the journal's zero profit constraint binds in this second best. There cannot exist $\left(p^{A^{\prime}}, p^{R^{\prime}}\right) \in Z$ such that

$$
\left(\hat{n}^{A}\left(p^{A^{\prime}}, p^{R^{\prime}}\right), \hat{n}^{R}\left(p^{R^{\prime}}, p^{A^{\prime}}\right)\right)=\left(\hat{n}^{A}\left(p^{A *}, p^{R *}\right), \hat{n}^{R}\left(p^{R *}, p^{A *}\right)\right)
$$

or else $\left(p^{A^{\prime}}, p^{R^{\prime}}\right)$ would provide participating customers with more surplus, and would generate more social (customers plus journal) surplus, than $\left(p^{A *}, p^{R *}\right)$, contradicting the fact that ( $p^{A *}, p^{R *}$ ) implements the second best. Hence $\left(p^{A *}, p^{R *}\right) \in \underline{Z}$. By Proposition 4, $\left(p^{A *}, p^{R *}\right)$ there exists an equilibrium satisfying our refinements in which both journals charge $\left(p^{A *}, p^{R *}\right)$.

Proof of Proposition 6: This proposition can be proved using arguments paralleling the proof of Proposition 4.

Details on Formulae and Computations for Numerical Examples: In Examples 1-3, author and reader benefits are uniformly distributed on $[0,1]$. In this case, it can be shown reduced-form demands are given by

$$
\hat{n}^{x}\left(p^{x}, p^{y}\right)= \begin{cases}\min \left(\frac{1}{2}\left[1-p^{x}+p^{y}+\sqrt{h\left(p^{x}, p^{y}\right)}\right], 1\right) & \text { if } h\left(p^{x}, p^{y}\right) \geq 0 \\ 0 & \text { if } h\left(p^{x}, p^{y}\right)<0\end{cases}
$$

where

$$
h\left(p^{x}, p^{y}\right)=1-2\left(p^{x}+p^{y}\right)+\left(p^{x}-p^{y}\right)^{2} .
$$

In terms of these reduced-form demands, industry profit in terms of is given by equation (1), net consumer surplus for authors is given by

$$
\frac{1}{2} \hat{n}^{R}\left(p^{R}, p^{A}\right)-\frac{1}{2} \hat{n}^{R}\left(p^{R}, p^{A}\right)\left[1-\hat{n}^{A}\left(p^{A}, p^{R}\right)\right]-p^{A} \hat{n}^{A}\left(p^{A}, p^{R}\right)
$$

and net consumer surplus for readers is given by an analogous expression. Consumer surplus is given by the sum of net author and reader consumer surpluses. Social welfare is given by the sum of industry profit and consumer surplus. The prices $p^{A}, p^{R}$ maximizing monopoly profit, social welfare in the second best and social welfare in the first best are found in each instance by numerical optimization methods.

In Examples 4-6, author benefits per reader equal one for the unit mass of authors and reader benefits are uniformly distributed on $[0,1]$. In this case, it can be shown reduced-form author demand is

$$
\hat{n}^{A}\left(p^{A}, p^{R}\right)= \begin{cases}1 & \text { if } p^{R} \leq 1 \text { and } p^{A}+p^{R} \leq 1 \\ 0 & \text { else }\end{cases}
$$

and reduced-form reader demand is

$$
\hat{n}^{R}\left(p^{R}, p^{A}\right)= \begin{cases}1-p^{R} & \text { if } p^{R} \leq 1 \text { and } p^{A}+p^{R} \leq 1 \\ 0 & \text { else }\end{cases}
$$

In terms of these reduced-form demands, net consumer surplus for authors is given by

$$
\hat{n}^{A}\left(p^{A}, p^{R}\right)\left[\hat{n}^{R}\left(p^{R}, p^{A}\right)-p^{A}\right]
$$

and for readers by

$$
\frac{1}{2} \hat{n}^{A}\left(p^{A}, p^{R}\right)\left[\frac{1}{2}-p^{R}+\left(\frac{p^{R}}{2}\right)^{2}\right]
$$

The rest of the calculations are as in the previous paragraph.
One issue with Examples 4-6 that deserves further discussion is the uniqueness of equilibrium. In each of Example 4-6, the equilibrium is the unique price vector that both maximizes the quantity of authors and readers (note the entire mass of authors and readers are served in the examples) and provides the stand-alone journal with zero profit. Hence the set $\underline{Z}$ is a single point
in each example.
Calculations for Examples 7-9 are analogous to those for Examples 4-6.

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[^0]:    ${ }^{1}$ For a newspaper account, see Weiss (2003).

[^1]:    ${ }^{2}$ The exception is the South African Journal of Information Management, which charges authors 75 Rand (10 EUR) per published page.
    ${ }^{3}$ The possibility that open access will offer more citations to authors is suggested by Lawrence's (2001) study of 1,500 computer conference "venues" that publish some of their content as open-access articles and some only in print. For 90 percent of the venues, the open-access articles were more highly cited. Within venues, open-access articles generated over three times the citations of print articles. The study does not fully account for the possible bias due to the selection of articles for open-access versus print publication. Walker (2004) discusses the example of an entomology society that has a hybrid model, allowing authors to choose open access for a fee. In 2001, about a year after introducing this model, about half of the authors paid for open access at a price of 90 USD ( 74 EUR) for an eight page article. As of February 2004, this percentage had grown to two-thirds of all authors at a price of $\$ 124$ for an eight page article.

[^2]:    ${ }^{4}$ This literature includes, among many other papers, Baye and Morgan (2001); Caillaud and Jullien (2003); Evans (2003); Hermalin and Katz (2004); Jeon, Laffont, and Tirole (2004); Laffont, et al. 2001; Rochet and Tirole (2002, 2003); Schmalensee (2002); and Wright (2003).

[^3]:    ${ }^{5}$ As we will see, the benefit per article is linear in the number of readers, so it would be straightforward to handle the case of multiple articles per author by treating the articles as being written by different authors.
    ${ }^{6}$ A natural question that arises in this simple model with homogeneous articles and with no exogenous differences among journals is why do journals exist in the first place? Why do authors not circumvent the intermediary and circulate their articles directly to readers? One answer provided by the model is that by bundling articles, journals economize on the fixed cost, $c^{R}$, of serving readers. If $c^{R}>0$, it would be prohibitively expensive for the infinitesimal authors to circulate their articles directly to the infinitesimal readers. By posting their articles on the Internet using the open-access model, however, it could be argued that authors cost force reader fixed costs $c^{R}$ to zero (see Section 7 for further discussion on this point). There would still be a role for journals in this case if one

[^4]:    were to add to the model a second type of article which is useless to our readers-qua-scholars (the articles may be useful in other regards, perhaps providing news or opinion about current events, but are useless to scholars in this particular field). Suppose the set of useless articles has a higher cardinality than the set of valuable articles. Readers must expend $\epsilon>0$ per article to determine its quality before reading it. The idea is that readers will have difficulty winnowing interesting scholarly articles from the abundant chaff on the Internet. Journals provide such a function. Journals have an advantage in sorting valuable from useless articles for two reasons. First, they can economize on the fixed $\operatorname{cost} \epsilon$ of search/selection, paying the cost once rather than each infinitesimal reader having to pay. Second, authors of useless articles would generally obtain no benefit from publishing in a scholarly journal and thus would not be willing to jump the hurdles involved in submitting to the journal (hurdles including submission fees and personal effort costs).

[^5]:    ${ }^{7}$ The equilibrium price for the multiproduct monopolist may be higher than for the single-product monopolist because the existence of the complementary good may raise a product's demand. Here we are comparing structural Lerner index formulae rather than equilibrium prices.

[^6]:    ${ }^{8}$ It might be thought that the increase in $c$ would offset the reduction in $c^{R}$ in moving from Example 1 to Example 2 to keep $M C^{R}$ constant. This is not true for two reasons. First, $c^{R}$ appears directly in $M C^{R}=c^{R}+c \hat{n}^{A}$, whereas $c$ is multiplied by $\hat{n}^{A} \leq 1$. Second, a simultaneous increase in $c$ and equal decrease in $c^{R}$ will cause $\hat{n}^{A}$ to fall. This is because the increase in $c$ has a direct effect on $n^{A}$, through its effect on $p^{A}$, whereas a decrease in $c^{R}$ only indirectly affects $n^{A}$ through its effect on $p^{R}$ and thus $n^{R}$.

