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Article

Asymmetric Information Flow between Exchange Rate, Oil, and Gold: New Evidence from Transfer Entropy Approach

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Abstract: The present study used transfer entropy and effective transfer entropy to examine the asymmetric information flow between exchange rates, oil, and gold. The dataset is composed of daily data covering the period of 1 January 2018 to 31 December 2021. Further, the dataset is bifurcated for analysis for before and during COVID. The bidirectional information flow is observed between EUR/USD and Oil for the whole study period unlike before COVID. However, during COVID, there was a unidirectional information flow from Oil→EUR/USD. The study finds a significant unidirectional information flow from Gold→EUR/USD. The study estimates also indicate that before COVID, the direction of information flow was from Oil→Gold. However, the direction of information flow reversed during COVID from Gold→Oil. Overall, the direction of information flow among these three variables is asymmetric. The highest transfer entropy was observed for Gold→EUR/USD among all the pairs under consideration.

Keywords: Shannon; Renyi; transfer entropy; COVID; Gold; Crude Oil; EUR/USD; Asymmetry



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1. Introduction

A common belief among policymakers and investors globally is that prices of the commodity move in unison as they are impacted by the various common macroeconomic variables (Le and Chang 2011). Crude Oil and Gold are listed among the most traded commodities in the world. Globally, Crude Oil is the most demanded commodity, and its prices are very volatile. Several studies have already been done on the asymmetry, uncertainty, volatility, and other aspects of Crude Oil prices in a global context, yet many studies are still ongoing (Li et al. 2022; Zhang et al. 2022a, 2022b). On the other hand, Gold is not just a precious metal that has an industrial value, but it is also considered a safe-haven asset (Ali et al. 2021; Janani et al. 2022; Vukovic et al. 2021b; Wen et al. 2022; Madani and Ftiti 2022). Due to this, investors both in the advanced and emerging markets generally use the combination of Gold and Oil to diversify their investment portfolios (Soytas et al. 2009). The exchange rates play a vital role in the global trading of commodities. Earlier and recent studies show that exchange rates strongly influence both Crude Oil and Gold prices (Jain and Biswal 2016; Bedoui et al. 2018; Chen et al. 2022).

As a consequence, a considerable number of studies are done on the dynamic linkages between Crude Oil, Gold, and exchange rates in the global context (Chang et al. 2013; Chen et al. 2022; Zhang and Qin 2022). The study findings are mixed because of different exchange rates, economic policies, consumption patterns, non-linear behavior and others. Hence, there is no ultimate consensus regarding the causal relationship among Crude Oil, Gold, and exchange rates. This provides theoretical support for the present study. The present study is diverse from the earlier studies in many contexts. First, the present study considers global indices over regional indices for Crude Oil and Gold, unlike the aforementioned studies. Second, the present study used EUR/USD currency pairs as the proxy for exchange rates instead of the regional exchange rates. The reason to choose

EUR/USD is that statistically, EUR/USD currency pairs in FOREX are the most traded currency pairs in the world. The information flow between the time series is of great interest to researchers and policymakers. As such, hidden information flow could reveal critical information on the risk, noise, and other associated dynamics (Kayal et al. 2021). However, quantifying such information flow between the time series is relatively difficult in reality. Most of the previous studies rely on VAR, VECM, GARCH, and other regular techniques for studying the causal relationship between the timeseries. These techniques are most useful for studying linear models based on several assumptions. However, the present study relies on the transfer entropy approach to overcome the above-mentioned issues.

The history of quantifying information has its roots in information theory. The study by Hartley (1928) quantifies the information as a logarithm of the number of all possible sequences of symbols based on a particular probability distribution. The concept of information entropy is introduced by Shannon (1948). The Kullback and Leibler (1951) distance and Shannon entropy concepts are combined to measure Shannon transfer entropy (Schreiber 2000). Similar to Shannon transfer entropy, a measure of Renyi transfer entropy is also derived (Rényi 2007; Beck and Schögl 1993; Jizba et al. 2012). Shannon and Renyi's transfer entropy are nonparametric-based measures that deal with the asymmetric information transfer between the time series. The assumptions and restrictions associated with these two methods are quite a few as compared to the other techniques. The study by Bossomaier et al. (2016) covered details on the background and applications of transfer entropy. However, transfer entropy-based measures are only used by a few studies in finance (Sensoy et al. 2014; Teng and Shang 2017; Benedetto et al. 2020; Huynh et al. 2020; Lahmiri and Bekiros 2020; Yao and Li 2020; Asafo-Adjei et al. 2021; Nyakurukwa 2021; Owusu Junior et al. 2021; and others).

The present study relies on the transfer entropy approach for the following reasons, as listed below.

- (i) Transfer entropy approach is well suited for studying asymmetric, nonlinear, and nonparametric causality.
- (ii) Transfer entropy approach can capture certain information that is beyond the scope of both the Diebold and Yilmaz (2012) and Baruník and Křehlík (2018) approaches [see Owusu Junior et al. (2021)].
- (iii) Transfer entropy approach ensures that the tail risk and leverage effects of asset returns are well captured [see Owusu Junior et al. (2021)].
- (iv) The present study also estimates effective transfer entropy to delineate low-risk assets from risky assets. In addition to it, effective transfer entropy measures are also useful in terms of accuracy, especially for small datasets.

Hence, the present study added value to the existing literature in the following ways:

- By providing rich asymmetric causality information among the exchange rate, Crude Oil, and Gold, especially during the COVID-19 period and non-COVID-19 period to the global policymakers and investors.
- By estimating effective transfer entropy values to outline low-risk assets from risky assets. It also helps to understand the integration between the various assets. All this information would be useful to the policymakers to design appropriate steps for domestic financial markets and investors in minimizing the overall investment risks and increasing returns, especially during crises.

The present study findings are interesting and have important implications for the policymakers. It investigates the asymmetric information flow among Oil, Gold, and EUR/USD, during and before the COVID period. All these variables have a direct link to the performance of European and global financial markets. Moreover, Gold is necessary for sovereign reserves. Similarly, Oil is a key petroleum product that is heavily imported by European and other nations as an energy resource. Furthermore, major trading currencies used globally for these Oil and Gold commodities are USD and EUR. These three assets' (Gold, Oil, and EUR/USD) widespread appeal has resulted in bivariate price co-movements

that have been the subject of growing research literature. Since a thorough understanding of price co-movements is essential for comprehending market integration and taking the proper action for portfolio diversification, it is critical to investigate the overall dynamics of information transmission among these assets. The study finds a strong one-way information flow from Gold→EUR/USD in both COVID and non-COVID periods. However, for the other pairs, the flow of information between the pairs varies significantly during COVID and non-COVID periods. This provides varied insights for decision making during the volatile (during COVID) and less volatile (before COVID) periods. It suggests that there is more to understanding market co-integration than only looking at the short- or long-term correlation between assets to develop an investing strategy. Our work looks into the diversification prospects in the form of quantifying information flows over the transmission of shocks. The transfer entropy and effective transfer entropy measures quantify the information flows. These values would help global researchers and policymakers to examine the informational efficiency of markets. Moreover, the findings suggest that depending on the state of the market, information flow may alter, which would have an effect on how the assets are integrated and, consequently, how their prices move. As a result, investors' diversification strategies should be flexible and depend on market integration and the direction of information flow.

The rest of the paper is structured as follows: A literature review (Section 2), Data and Methodology (Section 3), Results and Discussions (Section 4), and concludes with highlighting important policy implications (Section 5).

2. Literature Review

Gold and Oil are the two most actively traded commodities in the world (Baruník et al. 2016). Further, among all commodities, Gold is considered a means of exchange and a store of value and is also part of most of the central bank's major FOREX reserves (Kayal and Maheswaran 2021). Further, Oil is the most important commodity as it is the primary source of energy globally. Since it combines two of the largest economies and trading blocks in the world, the EUR/USD pairing has grown to be the most actively traded and thereby most liquid currency pair in the world. Further, USD and EUR are the top two most reserved foreign exchange currencies (Kayal and Maheswaran 2017). The global appeal of these three assets (Gold, Oil, and EUR/USD) has led to bivariate price co-movements, which have been the topic of developing scholarly literature. It is important to examine the general dynamics of information transmission among these assets since a detailed understanding of price co-movements is crucial for understanding market integration and taking the appropriate steps for portfolio diversification.

Economic theory makes it simple to explain the connection between the prices of Gold, Oil, and EUR/USD. For instance, a rise in the price of oil internationally pushes inflation higher. Investors commonly use major precious metals such as gold in this situation to hedge their portfolios from inflation (Baruník et al. 2016). Additionally, an important gauge of the state of the world economy is the Gold-Oil ratio. As mentioned earlier, the global trading of commodities is heavily reliant on exchange rates. Exchange rates have a significant impact on the prices of both Crude Oil and Gold, according to both earlier and recent studies (Jain and Biswal 2016; Bedoui et al. 2018; Chen et al. 2022). As a result, much research on the dynamic relationships between crude Oil, Gold, and exchange rates in a worldwide context have been conducted (Chang et al. 2013; Chen et al. 2022; Zhang and Qin 2022). Because of various exchange rates, economic policies, purchasing habits, and other factors, the study's findings are conflicting. As Gold and Oil both are denominated in US dollars, they are strongly connected. Among fiat currencies, EUR is the most important alternative to the USD and therefore a positive connection is generally observed between Gold and EUR or Oil and EUR. Consequently, EUR/USD is the single most suitable currency pair for this study.

Sometimes, generic economic intuition seems obvious while exploring directional or causative linkages among these three assets (Gold, Oil, and EUR/USD). Such theories might not, however, always offer sufficient justifications for actual linkages. The empirical finance literature is looking into these price dynamics using different advanced econometric or statistical models. We contribute to similar literature using the Transfer entropy (TE) approach. Prior research on the co-movements and spill-over of Gold, Oil and currency is inadequate and conflicting. To the best of our knowledge, a study specifically examining the direction and dominance of information transfer between pairs of Gold, Oil, and EUR/USD is few and far between. Through this work, we try to shed light on the same. We first discuss the studies that explore the relationship between Gold and Oil, the studies on Oil and EUR/USD and, lastly, the studies on Gold and EUR/USD.

The relationship between Gold and Oil prices is generally found to be momentous. For instance, some studies observe a stable correlation between Gold and Oil prices (Sari et al. 2010; Shafiee and Topal 2010; Gil-Alana et al. 2017), whereas others find that the same correlation is weak and inconsequential (Mensi et al. 2020a; Wen et al. 2020). Further, an asymmetric and nonlinear long-term relationship between Oil and Gold was observed (Churchill et al. 2019). Among many different commodities, Gold is found to be a net information transmitter for other significant commodities (Kang et al. 2017), whereas one study (Yildirim et al. 2020) demonstrates a one-way information flow from Oil to Gold prices. Another study (Yaya et al. 2016) observes a bidirectional relationship between them explicitly prior to the financial crisis and the unidirectional relationship (Gold to Oil) following it.

The evidence of the dynamic relationship between Oil prices and the EUR/USD exchange rate in academic studies is inconsistent. For example, there is evidence of a one-way causal relationship between EUR/USD to Oil prices (EUR/USD→Oil) (Houcine et al. 2020). However, Youssef and Mokni (2020) observe no significant relationship between them. In the context of volatility spillover, there is an existence of a positive relationship between EUR/USD and Oil prices (Jawadi et al. 2016; Zolfaghari et al. 2020). Further, a recent study offers significant evidence for a nonlinear and asymmetric relationship between these two assets, especially during periods of oil crashes (Ming et al. 2022). Many other studies offer different insights into the dynamic relationship between Oil prices and exchange rates (see Jammazi and Nguyen 2017; Li et al. 2017; Kočenda and Moravcová 2019; Bagheri and Ebrahimi 2020; Wen et al. 2020; Karatas and Unal 2021; Shang and Hamori 2021; etc.).

Earlier studies that explore specifically the dynamic relationship between Gold prices and the EUR/USD currency pair are rare and generally studied in the context of other aspects such as hedging, portfolio diversification, etc. Therefore, drawing precise conclusions related to the relationship between EUR/USD currency pair and Gold prices could be challenging. However, many studies provide various perspectives on the dynamic connection between Gold prices and exchange rates (for example, Antonakakis and Kizys 2015; Bagheri and Ebrahimi 2020; Mensi et al. 2021; Abdullah et al. 2022). Unlike all these studies, this study specifically explores the price dynamics between Gold and the EUR/USD currency pair.

Empirical academic literature on price co-movements, spillovers, interdependence, contagion, and information transfer is vast. All these studies use different financial assets such as equity, exchange rates, energy, cryptocurrency, and commodities in different settings (for example, Antonakakis 2012; Hameed et al. 2015; Corbet et al. 2020; Mensi et al. 2020b; Al-Yahyaee et al. 2020). The recent development of new statistical/econometrics methods suitable for quantifying these dynamics and advancement in computational power has resulted in a rapid expansion of the empirical finance literature in this area. Most of this research makes use of different time series models such as VAR-SVAR (Luu Duc Huynh 2019); nonlinear model (Zhang and Wu 2019; Maiti et al. 2020b; Peng et al. 2020; Li et al. 2020); multi-quantile VaR (Deng et al. 2021); time-varying robust model (Pham and Cepni 2022); copula-based models (Dastgir et al. 2019; Jang et al. 2022; Kim et al. 2020; She et al.

2019); wavelet-based (Maiti et al. 2020a; Maiti 2021; Vukovic et al. 2021a; Li et al. 2021; Maiti et al. 2022; Adebayo 2022), etc. Compared to all these methods, we use a completely different approach in this study. To accurately estimate the granger causality, we do not use traditional/advanced model-dependent cointegration methodologies. We explore a model-free TE method that allows nonlinear, nonparametric, and asymmetric interactions. Application of the nonlinear nonparametric technique is crucial since structural changes, volatility variations, and nonlinearities may all be used to characterize the prices of financial assets. By using the proper conditional density, TE may also be able to separate information that originates from shared information because of shared history. As a result, TE is a desirable metric for locating conditional dependencies (Diks and Fang 2017).

Further, due to its resistance to the issue of missing data and small variance Gaussian noise, TE is an effective method for estimating real-world bivariate causal connections (Edinburgh et al. 2021). In the context of directional causality of bivariate variables, the empirical finance literature has only recently begun to recognize the value and benefits of TE (see, He and Shang 2017; Adam 2020; Benedetto et al. 2020; Huynh 2020; Osei and Adam 2020; Behrendt and Schmidt 2021; Maghyereh et al. 2021). This is one of few first studies, to the best of the authors' knowledge, to utilize TE to analyze the information flow between bivariate pairs of different financial assets.

3. Data and Methodology

3.1. Data

The daily closing price data for EUR/USD, Crude Oil, and Gold is obtained from Yahoo. Daily returns are calculated from the closing price. The total data period of the study is between 3 January 2018 and 30 December 2021. Furthermore, the study divided the total sample into two as follows: (i) Before COVID (3 January 2018 to 31 December 2019) and (ii) During COVID (1 January 2020 to 30 December 2021).

3.2. Methodology

The study by Shannon (1948) estimates entropy of the discrete random variable as shown in Equation (1).

$$H_J = - \sum_j p(j) \cdot \log(p(j)) \tag{1}$$

The above formula uses the log base of 2 and the random variable is denoted by J. All the possible outcomes are denoted by j_1, j_2, j_n , whereas probabilities of the outcomes are denoted by $p(j_1), \dots, p(j_n)$. Thus, the above Equation (1) measures the average level of uncertainty or randomness or information gain in the units of bits. However, to quantify the information transfer between the two-time series, the concept of Shannon's (1948) entropy needed to be tied with the concept of Kullback and Leibler (1951) distance under the assumption that the underlying process follows a Markov process (Schreiber 2000). Accordingly, the Shannon transfer entropy is derived as follows (Schreiber 2000):

$$T_{J \rightarrow I}(k, l) = \sum_{i,j} p(i_{t+1}, i_t^{(k)}, j_t^{(k)}) \cdot \log \left(\frac{p(i_{t+1} | i_t^{(k)}, j_t^{(k)})}{p(i_{t+1} | i_t^{(k)})} \right) \tag{2}$$

where $T_{J \rightarrow I}$ measures the transfer entropy or information flow from J to I.

In a similar line, the transfer entropy could also be estimated by using the Rényi (2007) entropy. Rényi (2007) estimated entropy of the discrete random variable as shown in Equation (3).

$$H_J^q = \frac{1}{1-q} \log \sum_j p^q(j) \tag{3}$$

where q represents the weighting parameters and $p(j)$ represents the individual probabilities. The weighting parameters distribution could be normalized by using the escort distribution (Beck and Schögl 1993). Consequently, the Renyi transfer entropy is derived as follows (Jizba et al. 2012):

$$RT_{J \rightarrow I}(k, l) = \frac{1}{1 - q} \log \left(\frac{\sum_i \varnothing_q(i_t^{(k)}) p^q(i_{t+1} | i_t^{(k)})}{\sum_{i,j} \varnothing_q(i_t^{(k)}, j_t^{(l)}) p^q(i_{t+1} | i_t^{(k)}, j_t^{(l)})} \right) \tag{4}$$

where $RT_{J \rightarrow I}$ measures the transfer entropy or information flow from J to I. The Renyi entropy approaches the Shannon entropy for $q \rightarrow 1$.

From the application point of view, in the smaller samples, the above transfer entropy estimates are often biased. Such biases are addressed by estimating the effective transfer entropy (Marschinski and Kantz 2002). The statistical significance of the Shannon transfer entropy function (Equation (2)) is determined by the Markov block bootstrap (Dimpfl and Peter 2013). A discrete and stationary dataset is required for estimating both the Shannon and Renyi transfer entropy. In this study, the Shannon and Renyi transfer entropy are tested and estimated as outlined by Behrendt et al. (2019).

4. Results and Discussion

Both the Augmented Dickey Fuller (ADF) and Kwiatkowski–Phillips–Schmidt–Shin (KPSS) tests confirm that all the time series under consideration are stationary and at level (See Table 1).

Table 1. Stationarity test results.

	EUR/USD	Oil	Gold
ADF	−32.176	−23.14	−32.406
<i>p</i> value	0.01	0.01	0.01
KPSS	0.29341	0.068584	0.10441
<i>p</i> value	0.1	0.1	0.1

The descriptive statistics of EUR/USD, Oil, and Gold for the whole study period is shown in Table 2. The oil return series is more volatile as compared to the EUR/USD and Gold. The Skewness and Kurtosis values are extremely high for Oil.

Table 2. Descriptive Statistics.

	EUR/USD	Oil	Gold
Mean	-2.18×10^{-5}	−0.00288	0.000381
Median	0.00017	0.002286	0.000584
Maximum	0.014509	0.376623	0.059477
Minimum	−0.02782	−3.05966	−0.04979
Std. Dev.	0.004055	0.110553	0.009629
Skewness	−0.3731	−22.6229	−0.15439
Kurtosis	5.792471	603.6905	8.969453

The daily returns of Oil, Gold, and EUR/USD series are shown in Figure 1. Please also note that the EUR/USD series is represented in the secondary axis in Figure 1.

The following observations are common for all the Shannon transfer estimates tables. Under the column direction, X represents the first series and Y represents the second series. It indicates the direction of information flow from one series to another. For example, $X \rightarrow Y$ represents directional information flow from X to Y. The effective transfer entropy is shown under the heading “Eff. TE”. The Standard errors and p -values are based on the bootstrap samples whose quantiles are depicted at the end of the table.

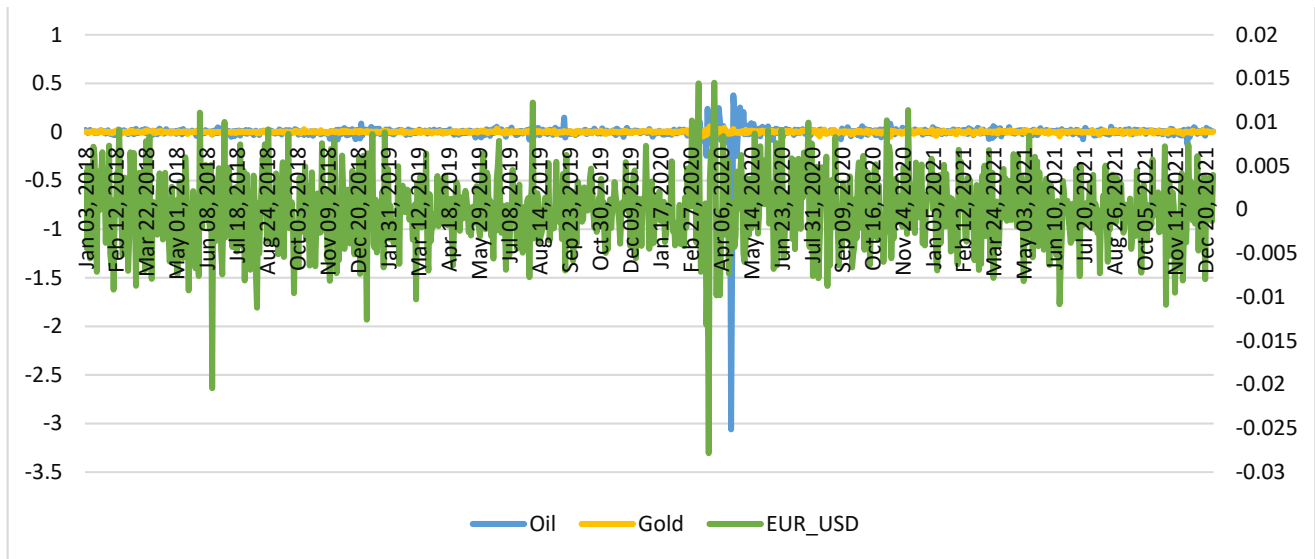


Figure 1. Oil, Gold, and EUR/USD daily returns plots between 3 January 2018 to 30 December 2021.

4.1. EUR/USD and Oil

The Shannon transfer entropy estimates between the two-time series namely EUR/USD and Oil are shown in Table 3a,b.

Table 3. (a) and (b): Shannon entropy estimates for EUR/USD and Oil.

(a) Total											
Direction	TE	Eff. TE	Std. Err.	p value							
X->Y	0.0154	0.007	0.0036	0.05							*
Y->X	0.0183	0.0108	0.0033	0.0033							**
Bootstrapped TE Quantiles (300 replications):											
Direction	0%	25%	50%	75%	100%	75%	100%				
X->Y	0.0017	0.0045	0.0065	0.0094	0.0194						
Y->X	0.001	0.0064	0.0089	0.0113	0.0217						
(b)											
Before COVID					During COVID						
Direction	TE	Eff. TE	Std. Err.	p value	TE	Eff. TE	Std. Err.	p value			
X->Y	0.0141	0	0.0057	0.3467	0.018	0.0033	0.0058	0.28			
Y->X	0.0048	0	0.0049	0.86	0.0232	0.0103	0.0051	0.0133	*		
Bootstrapped TE Quantiles (300 replications)											
Direction	0%	25%	50%	75%	100%	0%	25%	50%	75%	100%	
X->Y	0.0006	0.0064	0.0091	0.0131	0.028	0.0007	0.0071	0.0099	0.0141	0.0315	
Y->X	0.0013	0.0086	0.0119	0.0162	0.0382	0.0035	0.0114	0.014	0.0186	0.0407	

Note: p -values: 0.001 ‘***’, 0.01 ‘**’, 0.05 ‘*’; X: EUR/USD & Y: Oil.

The obtained Shannon entropy transfer estimates (Table 3a) confirm that there is a significant information flow between the two series for the entire study period in both ways (EUR/USD→Oil and Oil→ EUR/USD). This means that knowledge of either variable will even indicate a correspondingly higher level of risk. A part of this result is similar to the observation made by Houcine et al. (2020). They find a one-way causal relationship

between the EUR/USD to oil prices (EUR/USD→Oil). However, before COVID, there was no statistically significant information flow observed between the two series (EUR/USD and Oil), consistent with the findings of [Youssef and Mokni \(2020\)](#). This indicates that both the two series, namely EUR/USD and Oil, are highly unpredictable and risky. Interestingly, during COVID, a statistically significant information flow is observed between Oil→EUR/USD but not in the other direction (See [Table 3b](#)). The possible reason for this could be crude oil prices were more volatile and have a statistically significant impact on EUR/USD during COVID. It indicates that during an extraordinary situation, major financial assets become more integrated and generally move in similar fashion. Therefore, it becomes challenging for the investors to appropriately diversify their financial portfolio across asset classes. A diversification strategy that performs well in normal times might not perform similarly in a crisis.

4.2. EUR/USD and Gold

The Shannon transfer entropy estimates between EUR/USD and Gold are shown in [Table 4a,b](#).

Table 4. (a) and (b): Shannon entropy estimates for EUR/USD and Gold.

(a) Total										
Direction	TE	Eff. TE	Std. Err.	p value						
X->Y	0.011	0.0039	0.0032	0.11						
Y->X	0.0319	0.0244	0.0037	0 ***						
Bootstrapped TE Quantiles (300 replications)										
Direction	0%	25%	50%	75%	100%					
X->Y	0.0013	0.0048	0.0068	0.0092	0.0248					
Y->X	0.0012	0.0044	0.0067	0.0088	0.0174					
(b)										
Before COVID					During COVID					
Direction	TE	Eff. TE	Std. Err.	p value	TE	Eff. TE	Std. Err.	p value		
X->Y	0.0037	0	0.0049	0.8833	0.0185	0.0058	0.0056	0.1233		
Y->X	0.0514	0.0415	0.0046	0 ***	0.0428	0.0321	0.0056	0 ***		
Bootstrapped TE Quantiles (300 replications):										
Direction	0%	25%	50%	75%	100%	0%	25%	50%	75%	100%
X->Y	0.0015	0.0066	0.0095	0.0129	0.0315	0.001	0.0073	0.011	0.0153	0.032
Y->X	0.0006	0.0056	0.0086	0.0116	0.0269	0.0019	0.0081	0.0114	0.0158	0.0334

Note: p-values: 0.001 '***', 0.01 '**', 0.05 '*'; X: EUR/USD & Y: Gold.

The obtained Shannon entropy transfer estimates ([Table 4a,b](#)) confirm that there is a statistically significant unidirectional information flow observed between Gold→EUR/USD in all the cases. This indicates that EUR/USD series movement is predictable to a certain extent by perceiving the varying GOLD returns. Although there is numerous research that offer varied viewpoints on the dynamic relationship between gold prices and exchange rates (see [Bagheri and Ebrahimi 2020](#); [Mensi et al. 2021](#); [Abdullah et al. 2022](#), etc.), our observation is a bit different. Significant presence of unidirectional information flow between Gold→EUR/USD in all scenarios considered in this work implies gold price should be used to predict currency rates, especially EUR/USD. The possible reason behind our findings is the large share of gold among all the traded commodities in the world and significance of EUR and USD as the major traded currency.

4.3. Oil and Gold

The Shannon transfer entropy estimates between Oil and Gold are shown in Table 5a,b.

The obtained Shannon entropy transfer estimates (Table 5a,b) indicate that there is a significant unidirectional information flow between Gold→Oil during COVID and for the whole sample, similar to the findings of Yaya et al. (2016). However, before COVID, there was a significant reverse directional flow of information from Oil→Gold. This observation is in line with the findings of Yıldırım et al. (2020). The possible reason for this reverse trend could be the significant excessive asymmetric multifractality and fat tails characteristics of oil and gold prices (Mensi et al. 2020a). These different findings imply that understanding cointegration for investing strategy and portfolio diversification requires more than simply examining the short- or long-term correlation between assets. Information flow could change based on the market situation and that would impact the integration between the assets and hence their price movements. Therefore, diversification strategies for investors should be dynamic and must be based on market integration and the directional information flow.

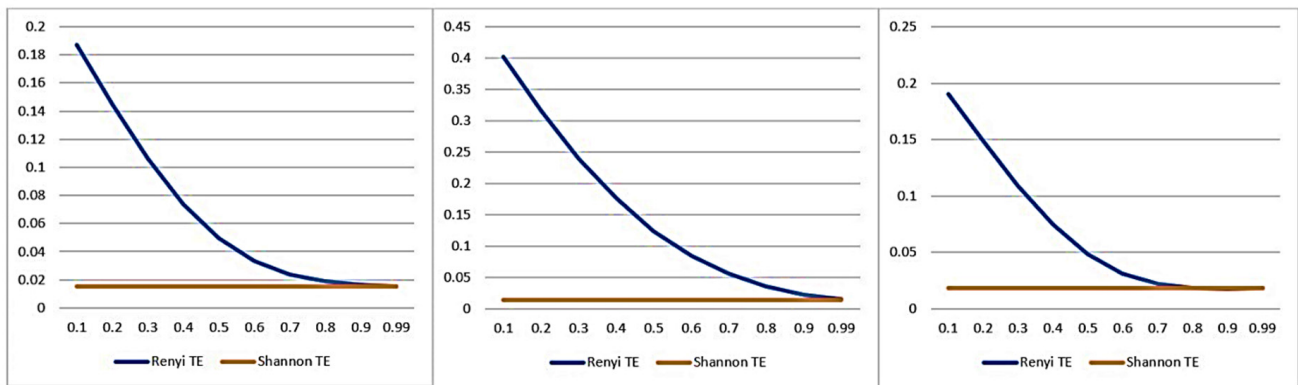
Table 5. (a) and (b): Shannon entropy estimates for Oil and Gold.

(a) Total										
Direction	TE	Eff. TE	Std. Err.	p value						
X->Y	0.0118	0.0045	0.0033	0.1133						
Y->X	0.0149	0.0056	0.0032	0.04						*
Bootstrapped TE Quantiles (300 replications)										
Direction	0%	25%	50%	75%	100%					
X->Y	0.0028	0.0065	0.0085	0.0108	0.0226					
Y->X	0.0018	0.0052	0.0072	0.0096	0.0175					
(b)										
Before COVID						During COVID				
Direction	TE	Eff. TE	Std. Err.	p value		TE	Eff. TE	Std. Err.	p value	
X->Y	0.0212	0.0124	0.0046	0.01	**	0.0191	0.0058	0.0061	0.1467	
Y->X	0.011	0	0.006	0.52		0.0265	0.0102	0.0061	0.03	*
Bootstrapped TE Quantiles (300 replications)										
Direction	0%	25%	50%	75%	100%	0%	25%	50%	75%	100%
X->Y	0.0004	0.0079	0.0112	0.0158	0.0345	0.0029	0.0104	0.0134	0.0175	0.0434
Y->X	0.0004	0.0056	0.0087	0.012	0.0253	0.0013	0.0081	0.0118	0.0166	0.0348

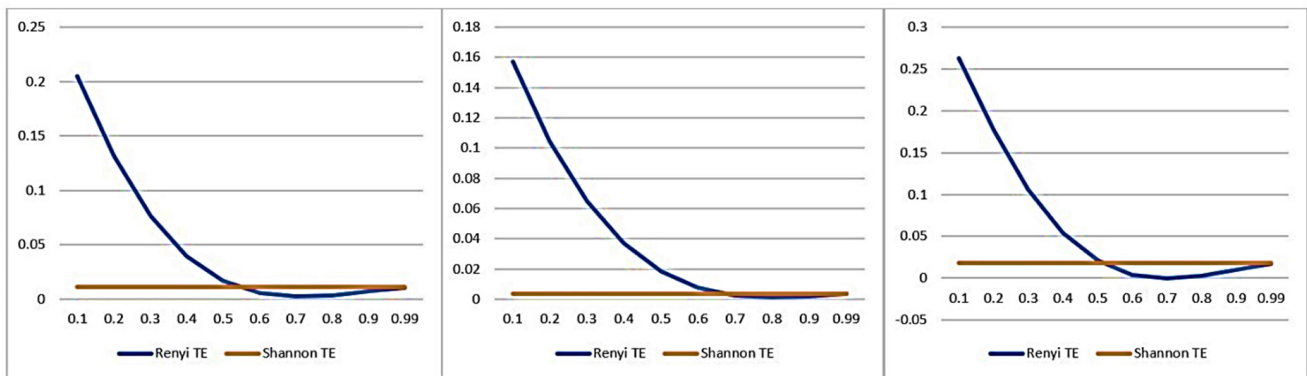
Note: p-values: 0.001 '***', 0.01 '**', 0.05 '*'; X: Oil & Y: Gold.

4.4. Robustness Checks

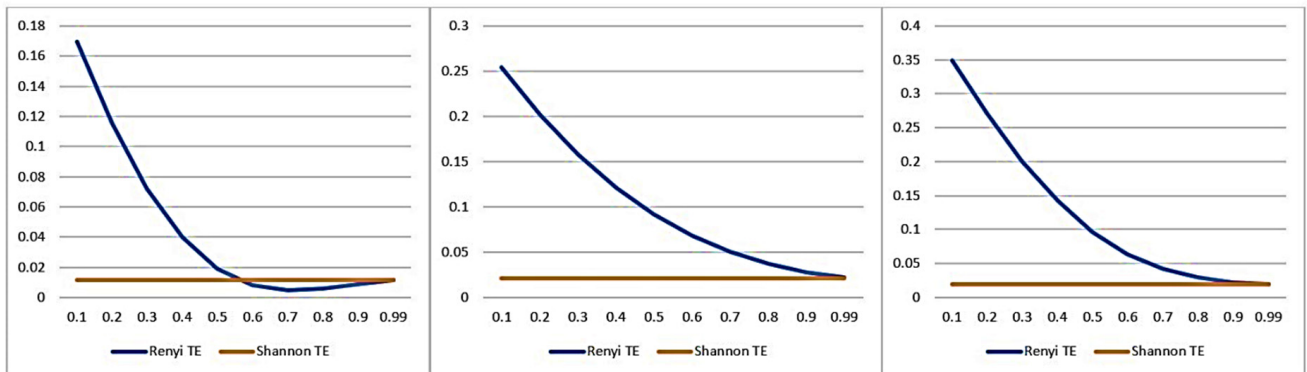
The quantiles are important because they affect the order of magnitude of the transfer entropy. Renyi transfer entropy allows for reweighting the probabilities associated with the different areas under the distributions. Hence, the Shannon transfer entropy estimates are comparable to the Renyi transfer entropy only when using the same bins. The Renyi transfer entropy for different weighting(q) are shown in the Figure 2a–c. It is clear from all the figures that the value of Renyi transfer entropy is highest at the lower values of q and it decreases subsequently with the increasing values of q , and as the value of q approaches 1 ($q \rightarrow 1$), it converges with the Shannon entropy. All these estimates confirm that the analysis is robust.



(a) EUR/USD and Oil (Total, Before COVID, and During COVID)



(b) EUR/USD and Gold (Total, Before COVID, and During COVID)



(c) Oil and Gold (Total, Before COVID, and During COVID)

Figure 2. (a–c): Renyi transfer entropy for different values of q .

5. Conclusions

The present study used transfer entropy and effective transfer entropy to examine the information flow between the different time series (exchange rate, oil, and gold). For a comprehensive analysis, the present study divides the period into three periods as total, before COVID, and during COVID. Information flow from series X to series Y is the amount of uncertainty reduced in future values of Y by knowing the past values of X given past values of Y. The transfer entropy and effective transfer entropy values quantify the amount of information flow from one series to another time series. Hence, knowing these values would certainly help global policymakers to design appropriate steps for domestic financial markets and investors in portfolio diversification to maximize risk-adjusted returns. The study finds a significant bidirectional information flow between EUR/USD and Oil pairs for the whole sample, partly similar to the observation made by [Houcine et al. \(2020\)](#). However, it becomes unidirectional during COVID (Oil→EUR/USD), and insignificant for

the before COVID sample. The study estimates also indicate a significant unidirectional transfer of entropy from Gold to EUR/USD (Gold→EUR/USD) for all samples. Our results offer a different insight into the dynamic relationship between gold prices and the exchange rates relationship literature (see Bagheri and Ebrahimi 2020; Mensi et al. 2021; Abdullah et al. 2022, etc. for varied viewpoints). Before COVID, there was a significant information flow from Oil to Gold (Oil→Gold), similar to the observation made by Yıldırım et al. (2020). However, the direction of information flow reversed during COVID (Gold→Oil). Among all these pairs, the information flow from Gold to EUR/USD is higher for all the samples. The findings show strong one-way information flow from gold→EUR/USD during both COVID and non-COVID periods. However, for other couples, the information flow between pairs differs significantly during COVID and non-COVID times. Based on the estimated transfer entropy and effective transfer entropy values, global investors and policymakers should make their decision in the selection of the assets in the portfolio to diversify the risk and improve returns.

For robustness checks, the present study plotted Renyi transfer entropy for different values of q against Shannon transfer entropy estimates. The plotted Figure 2a–c indicates that the value of Renyi transfer entropy is highest at the lower values of q , and when the value of q approaches 1 ($q \rightarrow 1$), it converges with the Shannon entropy. This means that knowledge of any of the two variables will even reveal a correspondingly higher level of risk. Certainly, it also does not mean there is no information flow. The major limitation of this work is that it does not consider multi-variate information transfer. Future research could replicate the current study utilizing real-time tick data, other important characteristics, possibly in a multi-variate framework.

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