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**Article**

## Modeling which factors impact interest rates

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## Modeling which Factors Impact Interest Rates

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**Abstract:** The Taylor (1993) rule for determining interest rates is generalized to account for three additional variables: The money supply, money velocity, and the unemployment rate. Thus, five parameters, i.e. weights assigned to the deviation in the inflation rate, the deviation in real GDP (Gross Domestic Product), the deviation in money supply, the deviation in the money velocity, and the deviation in unemployment rate, are introduced and estimated. The article explores and tests various combinations of the Taylor rule, the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve. The monthly US January 1, 1959 to March 31, 2022 data are adopted to test the optimal parameter values. Estimating the parameters with the least squares method gives better results than the Taylor rule. The optimal parameter values involve a relatively high weight to the deviation in unemployment rate, and moderate weights are assigned to the deviation in the inflation rate, the deviation in real GDP, the deviation in money supply, and the deviation in the money velocity. The corresponding sum of squares decreases by 42.95% when compared with the Taylor rule.

**Keywords:** Monetary policy, Taylor rule, Quantity Equation, Phillips curve, interest rates, inflation rate, GDP, money supply, money velocity, unemployment rate.

**JEL classification:** C6, E24, E50, E47, E52, E58.

## 1. Introduction

### 1.1. Background

Central banks are traditionally mandated to achieve certain objectives such as economic growth, low unemployment, price stability, stability of financial markets, etc. The Taylor rule (1993) accounts for some objectives. It predicts interest rates based on five variables: the equilibrium real interest rate, inflation rate, target inflation rate, real GDP (Gross Domestic Product), and the potential real GDP which can be sustained over the long term. Central banks often apply monetary policies including setting interest rates to manage the macroeconomy. Taylor's analysis (1993) has substantial impact on how the interest rate is determined. According to the Taylor rule, the interest rate is adjusted in response to the deviation in GDP and the deviation in the inflation rate. Taylor believes that his rule is a good tool to interpret historical monetary policy. This article questions that belief.

The Taylor rule relies on the deviation in real GDP and the deviation in the inflation rate to obtain the recommended central bank interest rate. It does not account for other variables which may be relevant for the conduct of monetary policy in economic and financial systems, such as money supply, money velocity, unemployment rate, financial market conditions, etc. Thus, the Taylor rule fails to reflect the state of the economy in real time. Another challenge is to precisely estimate the real potential GDP. In addition, the Taylor rule is a backward looking approach. This is also a critique of the current article since it ignores that central banks may be forward looking in setting the interest rates.

The Taylor rule is a well-known technique for central banks to set interest rates. The rule recommends that central banks increase the interest rate when the inflation rate is higher than the target inflation rate and the real GDP is higher than the real potential GDP. It gives equal 0.5 weight to the gap in real GDP and the gap in the inflation rate. It faces criticism because too few variables are incorporated. Other known variables such as money supply, money velocity and unemployment rate, captured by the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve, respectively, may additionally impact the interest rates. Specifically, a lower unemployment rate is one essential objective for central banks. Hence, it is interesting to incorporate these variables into the Taylor rule and explore the associated weights. Other unknown factors not considered in this article, such as economic crisis, fiscal deficit, global interest rates, etc. may also impact the interest rates.

How a central bank determines its interest rate is of particular interest in times of economic turmoil, common through history and, for example, during and in the aftermath of the 2020-2021 pandemic crisis when many countries first decreased and thereafter increased the interest rate to suppress high inflation above the target inflation rate. Changes in money supply impact economies substantially. Central banks commonly adjust the money supply through open market operations. That is, a central bank may increase the money supply by buying government bonds, either from commercial banks or other actors, or new bonds created by the government. The money velocity may also impact monetary policy. For example, a decline in the money velocity may offset an increase in the money supply. The Quantity Equation (Friedman, 1970) shows the relationship between the money supply and the money velocity. Two important objectives of central banks are low unemployment rate, and low inflation commonly preferred at 2%. However, the Taylor rule does not include the money supply, the money velocity and the unemployment rate.

## 1.2. Contribution

The article generalizes the Taylor rule by introducing the money supply and the money velocity as presented in the Quantity Equation (Friedman, 1970), and the unemployment rate as presented in the Phillips (1958) curve. The monthly US January 1, 1959 to March 31, 2022 data is adopted for empirical analysis. The least squares method is applied to estimate the optimal weights.

In his article, Taylor (1993, p. 202) points out that “this policy rule has the same coefficient on the deviation in the real GDP from trend and the inflation rate.” Inspired by this, this article tests different weights assigned to the deviation in real GDP, the deviation in the inflation rate, and three additional variables. The research questions are: How can the Taylor (1993) rule be improved to better account for the money supply, the money velocity and the unemployment rate? What are the optimal weights assigned to the deviations in inflation, real GDP, money supply, money velocity, and unemployment rate?

The theoretical contribution of this research is as follows: First, the article expands the Taylor rule by introducing additional variables, i.e. money supply, money velocity and unemployment rate. Second, the article explores various weights assigned to the deviations in inflation, real GDP, money supply, money velocity, and unemployment rate. Third, the article shows that incorporating the money supply, money velocity and the unemployment rate is more accurate than

the Taylor rule. The article provides a better framework for central banks to determine interest rates.

### 1.3. Literature

The Taylor rule has received substantial interest, with theoretical assessments and empirical testing, earning 12,681 citations in Google Scholar. Taylor (1993) assumes the same 0.5 weight to the deviation in real GDP and the deviation in the inflation rate. These parameter values fit the actual path during the 1987-1992 period very well. Judd and Rudebusch (1998) explore the Federal Reserve's response function to economic development. They point out that the Taylor rule framework helps to summarize the key elements of monetary policy. In his following research, Taylor (1999) updates the weights for the deviation in real GDP and the deviation in the inflation rate at 1 and 0.5, respectively. The reason is that the monetary policy rules have changed considerably over the different periods.

The Quantity Equation (Friedman, 1970) presents an analytical framework to explore the relationship between the money supply, money velocity, price level, and the real GDP. Although the money supply is widely assumed to impact interest rates, it is absent in the Taylor rule, perhaps because it is assumed to impact inflation and consequently may impact interest rates indirectly. The money supply plays an important role in monetary policy. The McCallum (1988) rule is an alternative to the Taylor rule. It recommends a target money supply  $M_0$  for the central banks. The McCallum rule is closely related to the Quantity Equation (Friedman, 1970), and recommends the central bank to set the target money supply  $M_0$  based on five variables: These are the money supply  $M_0$  in the previous period, the average quarterly increase of the money velocity of  $M_0$ , the desired inflation rate, the long-run average quarterly increase of real GDP, and the quarterly increase of nominal GDP. The McCallum rule performs better than the Taylor rule during crisis periods (Benchimol & Fourçans, 2012). Krušković (2022) investigates the role of central banks in maintaining price stability and achieving their inflation targets through various policy instruments, e.g. interest rate changes, foreign exchange interventions, and asset purchases.

The unemployment rate is also absent in the Taylor rule, but Prag (1994) finds a linkage from the unemployment rate to interest rates. Phillips (1958) also omits analyzing interest rates. Instead he analyzes the relationship between the unemployment rate and inflation. Azam, Khan, and Khan (2022) investigate the validity of the Phillips (1958) curve for eight countries in the Middle East and North Africa region. They find a negative but insignificant trade-off between the infla-

tion and unemployment rates in the short run. Gocer and Ongan (2020) examine the relationship between the inflation and interest rates in the United Kingdom using a nonlinear Autoregressive Distributed Lag model. They show that the nominal interest rate reacts more strongly to increases in inflation than to decreases in inflation. Wang and Hausken (2022b, 2022c) combine the Taylor (1993) rule, the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve, applying different tools and generating results different from the current article.

The literature more commonly compares how interest rate rules compare with money supply rules (Ascari & Ropele, 2013; Auray & Fève, 2003; Minford, Perugini, & Srinivasan, 2003), with solvency rules (Brancaccio & Fontana, 2013), and with the Friedman rule (Srinivasan, 2000). The literature also links the money supply to interest rate targets (Schabert, 2005, 2009) or to exchange rates (Tervala, 2012). The literature furthermore links monetary rules to macroeconomics more generally (Clarida, Gali, & Gertler, 2000), or applies the Taylor rule to build decision models for central bank digital currency (Wang & Hausken, 2022d).

Modified monetary rules appear after the Taylor rule. For example, Orphanides (2003) proposes a first difference rule, relating the current interest rate to its historical value and a year ahead forecast. As an alternative, Bullard (2017) and Kliesen (2019) adjust the Taylor rule, and propose an inertial rule. The rule prescribes a response of the interest rate to the economic developments over time.

## 1.4. Article organization

Section 2 presents the model. Section 3 analyzes the model with data sources, parameter estimation, and illustrations. Section 4 discusses the results. Section 5 presents limitations and future research. Section 6 provides policy implications. Section 7 concludes.

## 2. The model

Appendix A shows the nomenclature. This article tests and generalizes the well-known Taylor (1993) rule by incorporating the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve. Thus, we include three additional terms: money supply  $m_t$ ,  $m_t > 0$ , money velocity  $v_t$ ,  $v_t > 0$ , and the unemployment rate  $u_t$ ,  $u_t \geq 0$ , at time  $t$ ,  $t \geq 0$ , i.e.

$$i_t = \pi_t + r_t^* \pm a_\pi(\pi_t - \pi_t^*) \pm a_y \text{Log} \left( \frac{y_t}{\bar{y}_t} \right) \pm a_m \text{Log} \left( \frac{m_t}{\bar{m}_t} \right) \pm a_v \text{Log} \left( \frac{v_t}{\bar{v}_t} \right) \\ \pm a_u(\bar{u}_t - u_t), a_\pi + a_y + a_m + a_v + a_u = 1 \quad (1)$$

where  $i_t, i_t \in \mathbb{R}$  is the interest rate at time  $t$ ,  $\mathbb{R}$  is the set of all real numbers. The right hand side of (1) contains  $\pi_t + r_t^*$ , as in the Taylor rule, where  $\pi_t, \pi_t \in \mathbb{R}$ , is the inflation rate and  $r_t^*, r_t^* \in \mathbb{R}$ , is the equilibrium real interest rate. The subsequent five terms in (1) are preceded with  $\pm$  where  $+$  is the plausible default positive impact on the interest rate  $i_t$ , and  $-$  is the alternative negative impact on  $i_t$  analyzed in section 3. These five terms are expressed as follows: The deviation  $\pi_t - \pi_t^*$  in inflation rate, where  $\pi_t^*, \pi_t^* \in \mathbb{R}$ , is the target inflation rate. The deviation  $\text{Log} \left( \frac{y_t}{\bar{y}_t} \right)$  in real GDP, where  $y_t, y_t \geq 0$ , is the real GDP, and  $\bar{y}_t, \bar{y}_t \geq 0$ , is the potential real GDP that can be sustained over the long term. The deviation  $\text{Log} \left( \frac{m_t}{\bar{m}_t} \right)$  in money supply, where  $m_t, m_t \geq 0$ , is the money supply, and  $\bar{m}_t, \bar{m}_t \geq 0$ , is the potential money supply. The deviation  $\text{Log} \left( \frac{v_t}{\bar{v}_t} \right)$  in money velocity, where  $v_t, v_t \geq 0$ , is the money velocity, and  $\bar{v}_t, \bar{v}_t \geq 0$ , is the potential money velocity. The deviation  $\bar{u}_t - u_t$  in the unemployment rate, where  $\bar{u}_t, \bar{u}_t \geq 0$  is the natural unemployment rate, and  $u_t, u_t \geq 0$  is the unemployment rate. The five nonnegative parameters  $a_\pi, a_y, a_m, a_v, a_u$  are the weights assigned to the deviations in inflation  $\pi_t$ , real GDP  $y_t$ , money supply  $m_t$ , money velocity  $v_t$ , and unemployment rate  $u_t$ , respectively.  $\text{Log}$  is the logarithm with a base ten. The sum of the five parameters is assumed to be one, corresponding to Taylor (1993) assuming that  $a_\pi + a_y = 0.5 + 0.5 = 1$  when considering only the first two of the five terms.

The deviation  $\pi_t - \pi_t^*$  in the inflation rate and the deviation  $\text{Log} \left( \frac{y_t}{\bar{y}_t} \right)$  in real GDP are the two terms originally included in the Taylor (1993) rule. For the new term, the deviation  $\text{Log} \left( \frac{m_t}{\bar{m}_t} \right)$  in money supply in (1), the new variable money supply  $m_t, m_t \geq 0$  is introduced, as present in the Quantity Equation (Friedman, 1970). The potential money supply  $\bar{m}_t$  is estimated using the standard HP filter (Hodrick & Prescott, 1997), which is commonly used in economics to estimate potential real GDP (Michalek, 2010). Regarding the impact of the money supply  $m_t$  on the interest rate  $i_t$ , on the one hand, Ascari and Ropele (2013) suggest that an increase of money supply  $m_t$  will cause the interest rate  $i_t$  to increase. Thus, when the money supply  $m_t$  increases, central banks may increase the interest rate  $i_t$  to prevent savers' extensive withdrawals. On the other hand, the interest rate  $i_t$  is the price of the money supply  $m_t$  from the supply and demand perspective. Accordingly, C. A. Conrad (2021) suggest that the interest rate  $i_t$  decreases when the money supply  $m_t$  increases. This article explores both suggestions. The plus sign in (1) assumes a positive relationship between the interest rate  $i_t$  and the deviation

$\text{Log} \left( \frac{m_t}{\bar{m}_t} \right)$  in the money supply, while the minus sign assumes a negative relationship.

For the new term the deviation  $\text{Log} \left( \frac{v_t}{\bar{v}_t} \right)$  in money velocity in (1), the new variable money velocity  $v_t$ ,  $v_t \geq 0$ , is introduced. This term is also captured by the Quantity Equation (Friedman, 1970). The Keynesian theory of money demand (Keynes, Moggridge, & Johnson, 1971) suggests that the money velocity  $v_t$  needs to increase when the money supply  $m_t$  decreases, to keep the balance within the monetary market. Mendizabal (2006) suggests the money velocity  $v_t$  has a positive impact on the inflation rate  $\pi_t$ . Taylor (1993) suggests that the inflation rate  $\pi_t$  impacts the interest rate  $i_t$  positively. Therefore, we assume a positive relationship between the money velocity  $v_t$  and the interest rate  $i_t$ . Money velocity  $v_t$  is defined as the ratio of nominal GDP to the money supply stock (Federal Reserve Bank of St. Louis, 2022). Similarly, we define the potential money velocity  $\bar{v}_t$ ,  $\bar{v}_t \geq 0$  as the ratio of nominal potential GDP to the potential money supply. Thus, in (1) the deviation  $\text{Log} \left( \frac{v_t}{\bar{v}_t} \right)$  in the money velocity is presented on the same structure as the deviation  $\text{Log} \left( \frac{y_t}{\bar{y}_t} \right)$  in real GDP.

The new variable unemployment rate  $u_t$  is introduced for the new term the deviation  $\bar{u}_t - u_t$  in the unemployment rate in (1). A low unemployment rate  $u_t$  is one of the most important objectives of a central bank. Thus, central banks may take into account the unemployment rate  $u_t$  when setting the interest rate  $i_t$ . Phillips (1958) originally investigates the relationship between the unemployment rate  $u_t$  and wage growth. Thereafter, Samuelson and Solow (1960) connect the employment rate with the inflation rate. The Phillips (1958) curve illustrates an inverse relationship between the unemployment rate  $u_t$  and the inflation rate  $\pi_t$  in the short term. Specifically, the Phillips (1958) curve is divided into a short run Phillips (1958) curve and a long run Phillips (1958) curve (Granger & Jeon, 2011). The unemployment rate  $u_t$  and the inflation rate  $\pi_t$  are inversely related in the short run. This relationship breaks down in the long run (Russell & Banerjee, 2008). Since Taylor (1993) assumes a positive correlation between the inflation rate  $\pi_t$  and the interest rate  $i_t$ , an inverse relationship is assumed between the interest rate  $i_t$  and the unemployment rate  $u_t$ , as also suggested by Prag (1994). The deviation  $\bar{u}_t - u_t$  in the unemployment rate indicates an inverse relationship between the interest rate  $i_t$  and the unemployment rate  $u_t$ . Finally, for generality, the article also tests the plus versus minus signs for the five terms, i.e. the deviation  $\pi_t - \pi_t^*$  in the inflation rate, the deviation  $\text{Log} \left( \frac{y_t}{\bar{y}_t} \right)$  in real GDP, the deviation  $\text{Log} \left( \frac{v_t}{\bar{v}_t} \right)$  in money velocity, and the deviation  $\bar{u}_t - u_t$  in the unemployment rate.



### 3. Analyzing the model

#### 3.1. Data sources

Monthly US January 1, 1959 to March 31, 2022 data is collected and compiled from the following sources: The real GDP  $y_t$  is estimated from the U.S. Bureau of Economic Analysis (2022). The real potential GDP  $\bar{y}_t$  is derived from the U.S. Congressional Budget Office (2022b). The quadratic interpolation method is applied to convert quarterly data to monthly data for the real GDP  $y_t$  and the real potential GDP  $\bar{y}_t$ . The M2 money supply  $m_t$  is estimated from the Board of Governors of the Federal Reserve System (US) (2022b). The money velocity  $v_t$  is estimated from the Federal Reserve Bank of St. Louis (2022). The unemployment rate  $u_t$  is derived from the U.S. Bureau of Labor Statistics (2022b). The natural unemployment rate  $\bar{u}_t$  is estimated from the U.S. Congressional Budget Office (2022a). The quadratic interpolation method is used to convert quarterly data to monthly data for  $\bar{u}_t$ . The inflation rate  $\pi_t$  is derived from the U.S. Bureau of Labor Statistics (2022a). The target inflation rate  $\pi_t^* = 1.5\%$  is estimated from Shapiro and Wilson (2019) from January 1, 2000 to December 30, 2007. The common  $\pi_t^* = 2\%$  is assumed for the remaining January 1, 1959 to March 31, 2022 period, as Taylor (1993) assumes for January 1, 1984 to September 31, 1992. The common equilibrium real interest rate  $r_t^* = 2\%$  is assumed throughout January 1, 1959 to March 31, 2022, used also by Taylor (1993) for January 1, 1984 to September 31, 1992, and consistently with Kiley's (2020) estimation and the long run inflation target specified by the Federal Open Market Committee (The Federal Reserve, 2022). The empirical interest rate  $i_t$  is derived from the Board of Governors of the Federal Reserve System (US) (2022a).

#### 3.2. Estimating the parameters and illustrating the solution

Table 1 shows the estimations of the five parameter values  $a_\pi, a_y, a_m, a_v, a_u$  with different combinations of parameter values in (1), obtained using Mathematica 13.1 (<https://www.wolfram.com>).

Table 1. Curve number, estimated parameter values  $a_\pi, a_y, a_m, a_v, a_u$ , parameter specifics, the number  $N$  of free choice variables, and the sum  $S$  of the squared differences between the empirical interest rate  $i_t$  and the theoretical interest rate  $i_t$  in (1). A superscript star \* after a number means that the corresponding sign in (1) is changed from plus to minus.

Curve	$a_\pi, a_y, a_m, a_v, a_u$	Parameter specifics	N	S
1	0.5, 0.5, 0, 0, 0	Taylor (1993) rule	0	0.830774
2	0.2, 0.2, 0.2, 0.2, 0.2	Equal weight	0	0.582477
3a	0.2, 0.2, 0.2, 0, 0.4	$a_\pi = a_y = a_m = 0.2$ , optimizing $a_u$ when $a = 0.4 - a_u$	1	0.577883
3b	0.2, 0.2, 0.2, 0.04*, 0.36	$a_\pi = a_y = a_m = 0.2$ , optimizing $a_u$ when $a = 0.4 - a_u$	1	0.576750
4a	0.2, 0.2, 0.25, 0, 0.35	$a_\pi = a_y = 0.2$ , optimizing $a_v$ and $a_u$ when $a_m = 0.6 - a_v - a_u$	2	0.577109
4b	0.2, 0.2, 0, 0.17*, 0.43	$a_\pi = a_y = 0.2$ , optimizing $a_v$ and $a_u$ when $a_m = 0.6 - a_v - a_u$	2	0.576230
4c	0.2, 0.2, 0.03*, 0.17*, 0.4	$a_\pi = a_y = 0.2$ , optimizing $a_v$ and $a_u$ when $a_m = 0.6 - a_v - a_u$	2	0.576582
5a	0, 0, 0.37, 0.37, 0.26	$a_\pi = a_y, a_m = a_v$ , optimizing $a_y$ and $a_v$ when $a_u = 1 - 2a_y - 2a_v$	2	0.499951
5b	0.16*, 0.16*, 0.13, 0.13, 0.4	$a_\pi = a_y, a_m = a_v$ , optimizing $a_y$ and $a_v$ when $a_u = 1 - 2a_y - 2a_v$	2	0.474088
6a	0, 0, 0.47, 0.18, 0.35	$a_\pi = a_y$ , optimizing $a_m, a_v$ and $a_u$ when $a_{\pi,y} = (1 - a_m - a_v - a_u) / 2$	3	0.496629
6b	0.165*, 0.165*, 0.11, 0.13, 0.43	$a_\pi = a_y$ , optimizing $a_m, a_v$ and $a_u$ when $a_{\pi,y} = (1 - a_m - a_v - a_u) / 2$	3	0.474051
7a	0.2, 0.41, 0.17, 0, 0.22	$a_\pi = 0.2$ , optimizing $a_m, a_v$ and $a_u$ when $a = 0.8 - a_m - a_v - a_u$	3	0.576203
7b	0.2, 0.42, 0, 0.12*, 0.26	$a_\pi = 0.2$ , optimizing $a_m, a_v$ and $a_u$ when $a = 0.8 - a_m - a_v - a_u$	3	0.574744
7c	0.2, 0.61, 0.06*, 0, 0.13	$a_\pi = 0.2$ , optimizing $a_m, a_v$ and $a_u$ when $a = 0.8 - a_m - a_v - a_u$	3	0.578171
7d	0.2, 0.42, 0*, 0.12*, 0.26	$a_\pi = 0.2$ , optimizing $a_m, a_v$ and $a_u$ when $a = 0.8 - a_m - a_v - a_u$	3	0.574744
8a	0, 0.09, 0.44, 0.15, 0.32	optimizing $a_y, a_m, a_v$ and $a_u$ when $a_\pi = 1 - a_y - a_m - a_v - a_u$	4	0.496512
8b	0.16*, 0, 0.32, 0.21, 0.31	optimizing $a_y, a_m, a_v$ and $a_u$ when $a_\pi = 1 - a_y - a_m - a_v - a_u$	4	0.474937
8c	0.17*, 0.13*, 0.15, 0.15, 0.4	optimizing $a_y, a_m, a_v$ and $a_u$ when $a_\pi = 1 - a_y - a_m - a_v - a_u$	4	<b>0.473981</b>
9a	0, 0.31, 0.4, 0.29, 0	$a_u = 0$ , Taylor (1993) rule and Quantity Equation (Friedman, 1970), optimizing $a_y, a_m$ and $a_v$ when $a_u = 0$ , and $a_\pi = 1 - a_y - a_m - a_v$	3	0.502298
9b	0.16*, 0.32, 0.24, 0.28, 0	$a_u = 0$ , Taylor (1993) rule and Quantity Equation (Friedman, 1970), optimizing $a_y, a_m$ and $a_v$ when $a_u = 0$ , and $a_\pi = 1 - a_y - a_m - a_v$	3	0.481483

10a	0, 0.98, 0, 0, 0.02	$a_m = a_v = 0$ , Taylor (1993) rule and Phillips (1958) curve, optimizing $a_y$ and $a_u$ when $a_m = a_v = 0, a_\pi = 1 - a_y - a_u$	2	0.512049
10b	0.17*, 0.66, 0, 0, 0.17	$a_m = a_v = 0$ , Taylor (1993) rule and Phillips (1958) curve, optimizing $a_y$ and $a_u$ when $a_m = a_v = 0, a_\pi = 1 - a_y - a_u$	2	0.488556
11	0, 0, 0.47, 0.18, 0.35	$a_\pi = a_y = 0$ , Quantity Equation (Friedman, 1970) and Phillips (1958) curve, optimizing $a_v$ , and $a_u$ when $a_\pi = a_y = 0, a_m = 1 - a_v - a_u$	2	0.496629
12a	0, 0, 0.46, 0.1, 0.44	$a_y = 0$ , optimizing $a_m, a_v$ , and $a_u$ when $a_y = 0, a_\pi = 1 - a_m - a_v - a_u$	3	0.497407
12b	0.16*, 0, 0.32, 0.21, 0.31	$a_y = 0$ , optimizing $a_m, a_v$ , and $a_u$ when $a_y = 0, a_\pi = 1 - a_m - a_v - a_u$	3	0.474937
13	0, 0, 0.51, 0.49, 0	$a_\pi = a_y = a_u = 0$ , Quantity Equation (Friedman, 1970), optimizing $a_v$ when $a_m = 1 - a_v$	1	0.509102
14	0, 0, 0, 0, 1	$a_\pi = a_y = a_m = a_v = 0, a_u = 1$ , Phillips (1958) curve	0	0.571153
Average	N/A	The average of the above 27 curves	0	0.510363

Curve 1 represents the Taylor (1993) rule assuming  $a_\pi = a_y = 0.5, a_m = a_v = a_u = 0$ . The sum of squares is relatively high at  $S = 0.830774$ . Curve 2 assumes equal 0.2 weight for the five parameters. The sum of the squared differences is lower at  $S = 0.582477$ , i.e. a 29.96% decrease compared with the Taylor (1993) rule in curve 1. Hence equal weights for the five parameters explain the interest rate  $i_t$  better than the Taylor (1993) rule. Curves 3a and 3b assume one free choice variable, where  $a_u$  is optimized assuming  $a_v = 0.4 - a_u$ . That causes an even lower sum of squared differences  $S = 0.577883$ , but with the optimal parameter  $a_v = 0$ . That suggests that the corresponding sign in (1) may be negative. A negative sign before  $\text{Log} \left( \frac{v_t}{v_t} \right)$  in (1) causes the optimal parameters  $a_v = 0.04$  and  $a_u = 0.36$ , and a marginally lower sum of squared differences  $S = 0.576750$ . Curves 3a and 3b suggest that the weight  $a_u$  assigned to unemployment, not present in the Taylor (1993) rule, may potentially be relatively high, which becomes clearer as we proceed. Curves 4a, 4b, and 4c assume two free choice variables, where  $a_v$  and  $a_u$  are optimized assuming  $a_m = 0.6 - a_v - a_u$ . That causes a similar sum of squared differences  $S = 0.577109$  in curve 4a. Again, the optimal parameter is  $a_v = 0$ . Hence, curve 4b tests the negative sign for  $\text{Log} \left( \frac{v_t}{v_t} \right)$  in (1). That causes a slightly lower sum of squares  $S = 0.576230$  compared with curve 4a, but with the optimal parameter  $a_m = 0$ . Assuming negative signs for  $\text{Log} \left( \frac{m_t}{m_t} \right)$  and  $\text{Log} \left( \frac{v_t}{v_t} \right)$  in (1) cause the optimal parameters  $a_m = 0.03$  and  $a_v = 0.17$  in curve 4c, and a similar

sum of squared differences  $S = 0.576582$ . Curves 4a, 4b, and 4c also suggest that the weight  $a_u$  may be relatively high. Curves 5a and 5b assume two free choice variables, where  $a_y$  and  $a_v$  are optimized assuming  $a_\pi = a_y$ ,  $a_m = a_v$ , and  $a_u = 1 - 2a_y - 2a_v$ . That causes a lower sum of squared differences  $S = 0.499951$  in curve 5a, but interestingly with the two optimal parameters  $a_\pi = a_y = 0$ . Assuming negative signs before  $(\pi_t - \pi_t^*)$  and  $\text{Log}\left(\frac{y_t}{y_t^*}\right)$  in (1) yield an even lower sum of squared differences  $S = 0.474088$  compared with curve 5a. Curves 6a and 6b assume three free choice variables, where  $a_m$ ,  $a_v$  and  $u$  are optimized assuming  $a_\pi = a_y = (1 - a_m - a_v - a_u)/2$ . That causes a similar sum of squared differences  $S = 0.496629$ , but also with the optimal parameters  $a_\pi = a_y = 0$ . Hence, curve 6b assumes negative signs before  $(\pi_t - \pi_t^*)$  and  $\text{Log}\left(\frac{y_t}{y_t^*}\right)$  in (1). That causes a lower sum of squared differences  $S = 0.474051$  compared with curve 6a. Curves 5a, 5b, 6a and 6b suggest negative signs before  $(\pi_t - \pi_t^*)$  and  $\text{Log}\left(\frac{y_t}{y_t^*}\right)$  in (1). Curves 7a, 7b, 7c, and 7d also assume three free choice variables, where  $a_m$ ,  $a_v$  and  $u$  are optimized assuming  $a_\pi = 0.2$ . That causes the sum of squared differences  $S = 0.576203, 0.574744, 0.578171$  and  $0.574744$ , respectively, which are higher compared with curves 5a, 5b, 6a and 6b. The higher sum of squares in curves 7a, 7b, 7c and 7d suggests that the weight  $a_y$  assigned to  $(\pi_t - \pi_t^*)$  should be lower than 0.2.

Curves 8a, 8b and 8c assume four free choice variables, where  $a_y$ ,  $a_m$ ,  $a_v$  and  $a_u$  are optimized assuming  $a_\pi = 1 - a_y - a_m - a_v - a_u$ . That causes the sum of squared differences  $S = 0.496512$  in curve 8a, but with optimal parameter  $a_\pi = 0$ . A negative sign before  $(\pi_t - \pi_t^*)$  in (1) causes the optimal parameters  $a_\pi = 0.16$  and  $a_y = 0$ , and a marginally lower sum of squared differences  $S = 0.474937$  compared with curve 8a. Hence, curve 8c assumes negative signs before  $(\pi_t - \pi_t^*)$  and  $\text{Log}\left(\frac{y_t}{y_t^*}\right)$  in (1), which causes the lowest sum of squared differences  $S = 0.473981$  so far, and also the lowest overall in Table 1, and thus marked in bold, i.e. a 42.95% decrease compared with the Taylor (1993) rule in curve 1. The corresponding optimal parameter values are  $a_\pi = 0.17$ ,  $a_y = 0.13$ ,  $a_m = 0.15$ ,  $a_v = 0.15$ ,  $a_u = 0.4$ . This again suggests that the weight  $a_u$  assigned to unemployment rate should be relatively high.

Curves 9a and 9b assume three free choice variables and represents the combination of the Taylor (1993) rule and the Quantity Equation (Friedman, 1970), where  $a_y$ ,  $a_m$ , and  $a_u$  are optimized assuming  $a_u = 0$  and  $a_\pi = 1 - a_y - a_m - a_v$ . That causes a sum of squared differences  $S = 0.502298$  in curve 9a, but with the optimal parameter  $a_\pi = 0$ . A negative sign before  $(\pi_t - \pi_t^*)$  in (1) causes a lower sum of squared differences  $S = 0.481483$  compared with curve 9a. Thus, the combination of the Taylor (1993) rule and the Quantity Equation (Friedman, 1970) explains the interest rate  $i_t$  better than the Taylor (1993) rule in curve 1.

Curves 10a and 10b assume two free choice variables and represent the combination of the Taylor (1993) rule and the Phillips (1958) curve, where  $a_y$  and  $a_u$  are optimized assuming  $a_m = a_v = 0$  and  $a_\pi = 1 - a_y - a_u$ . That causes a sum of squared differences  $S = 0.512049$  in curve 10a, but again with the optimal parameter  $a_\pi = 0$ . Thus, curve 10b assumes the negative sign for  $(\pi_t - \pi_t^*)$  in (1). That causes a slightly lower sum of squared differences  $S = 0.488556$  compared with curve 10a. The combination of the Taylor (1993) rule and the Phillips (1958) curve also explain the interest rate  $i_t$  better than the Taylor (1993) rule in curve 1.

Curve 11 assumes two free choice variables and represents the combination of the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve, where  $a_v$  and  $a_u$  are optimized assuming  $a_\pi = a_y = 0$ , and  $a_m = 1 - a_v - a_u$ . That causes a sum of squared differences  $S = 0.496629$ , i.e., a 40.22% decrease compared with the Taylor (1993) rule in curve 1. The combination of the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve also explain the interest rate  $i_t$  better than the Taylor (1993) rule in curve 1.

Curves 12a and 12b assume three free choice variables, where  $a_m$ ,  $a_v$  and  $a_u$  are optimized assuming  $a_y = 0$ , and  $a_\pi = 1 - a_m - a_v - a_u$ . That causes a sum of squared differences  $S = 0.497407$  in curve 12a, but again with the optimal parameter  $a_\pi = 0$ . Assuming a negative sign before  $(\pi_t - \pi_t^*)$  in (1) causes for curve 12b the second lowest sum of squared differences  $S = 0.474937$  in Table 1. The result happens to be the same as in curve 8b.

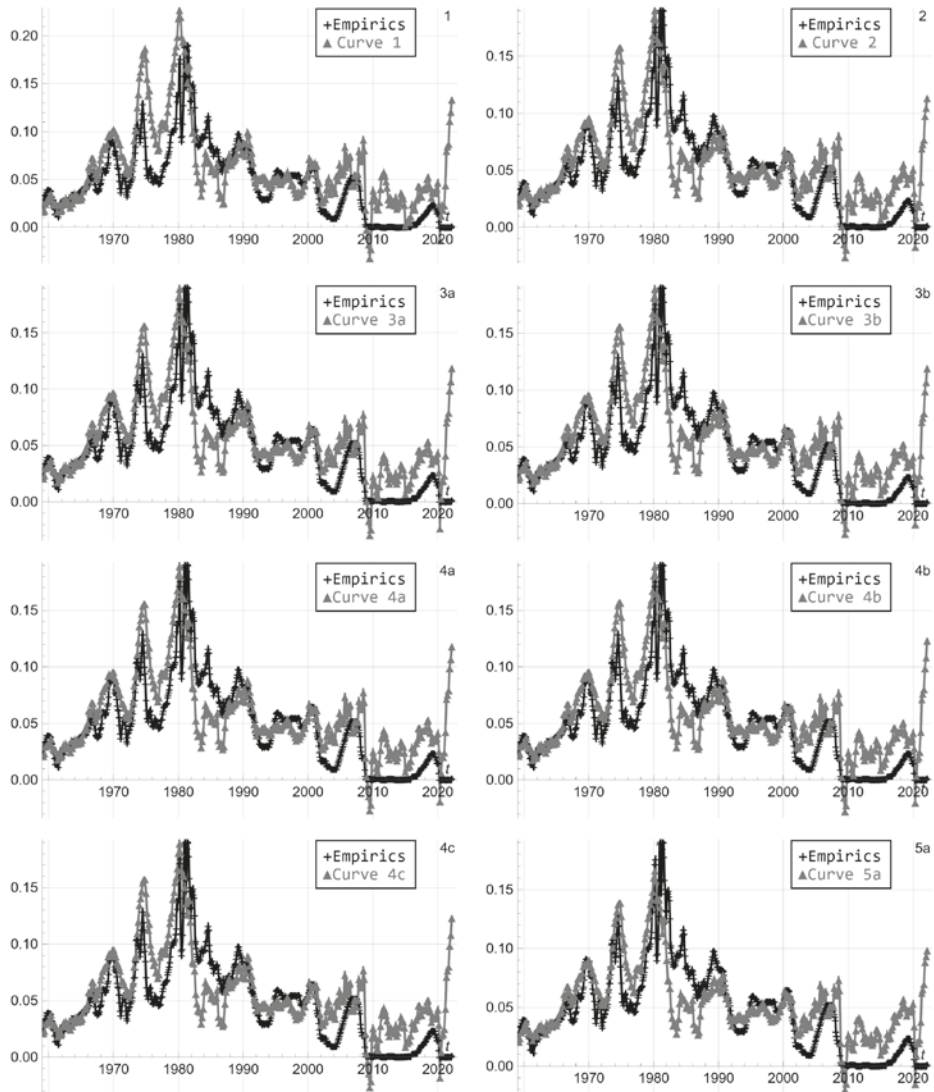
Curve 13 assumes one free choice variable and represents the Quantity Equation (Friedman, 1970), where  $a_v$  is optimized assuming  $a_\pi = a_y = a_u = 0$ , and  $a_m = 1 - a_v$ . That causes a sum of squared differences  $S = 0.509102$ . That suggests that the Quantity Equation (Friedman, 1970) explains the interest rate  $i_t$  better than the Taylor (1993) rule in curve 1.

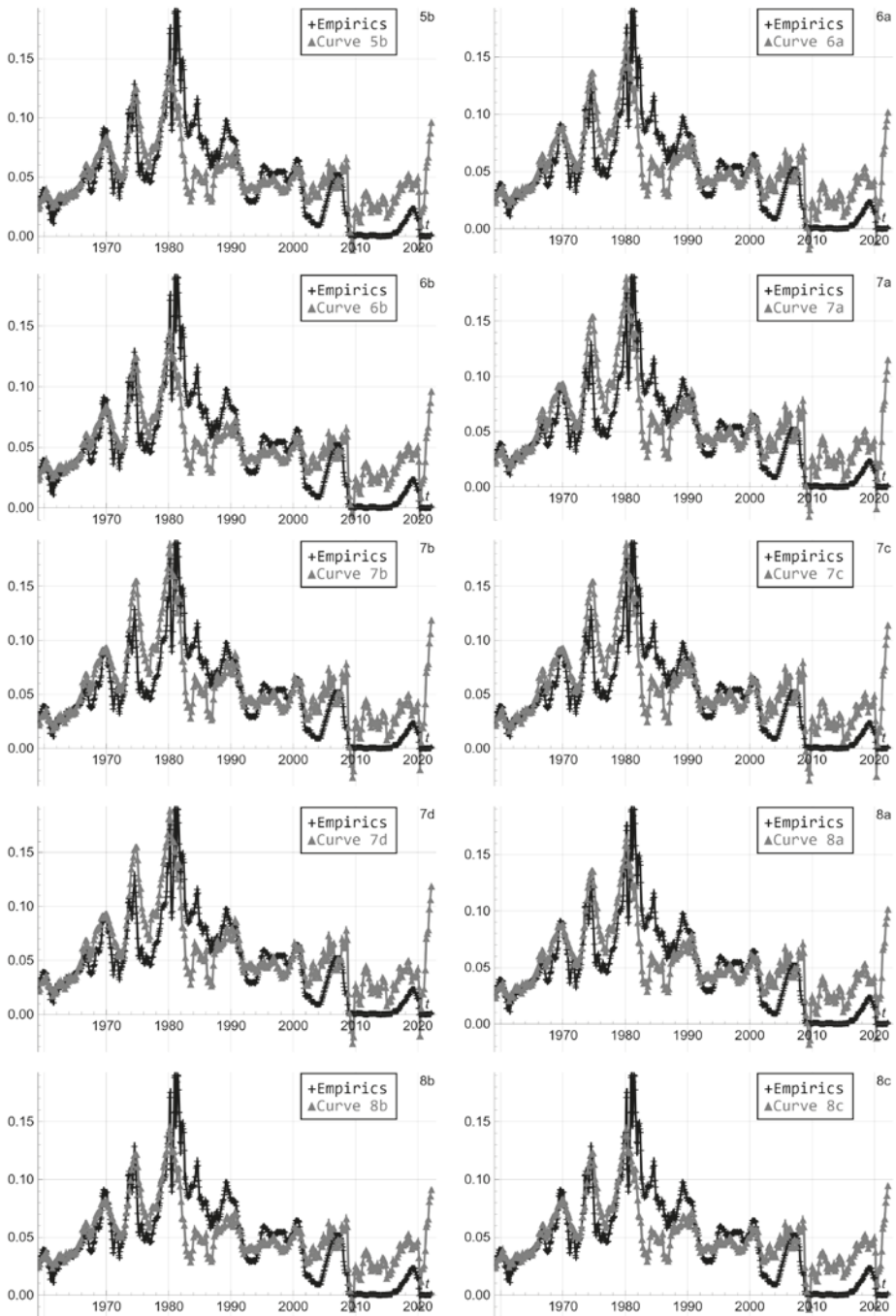
Curve 14 assumes no free choice variables and that only the Phillips (1958) curve is explanatory, i.e.  $a_\pi = a_y = a_m = a_v = 0$ ,  $a_u = 1$ . The sum of squared differences is  $S = 0.571153$ .

Curve Average calculates the average of these 27 curves. The corresponding sum of squared differences  $S = 0.510363$ , i.e. a 38.57% decrease compared with the Taylor (1993) rule in curve 1. Curve Standard deviation calculates the standard deviation on these 27 curves.

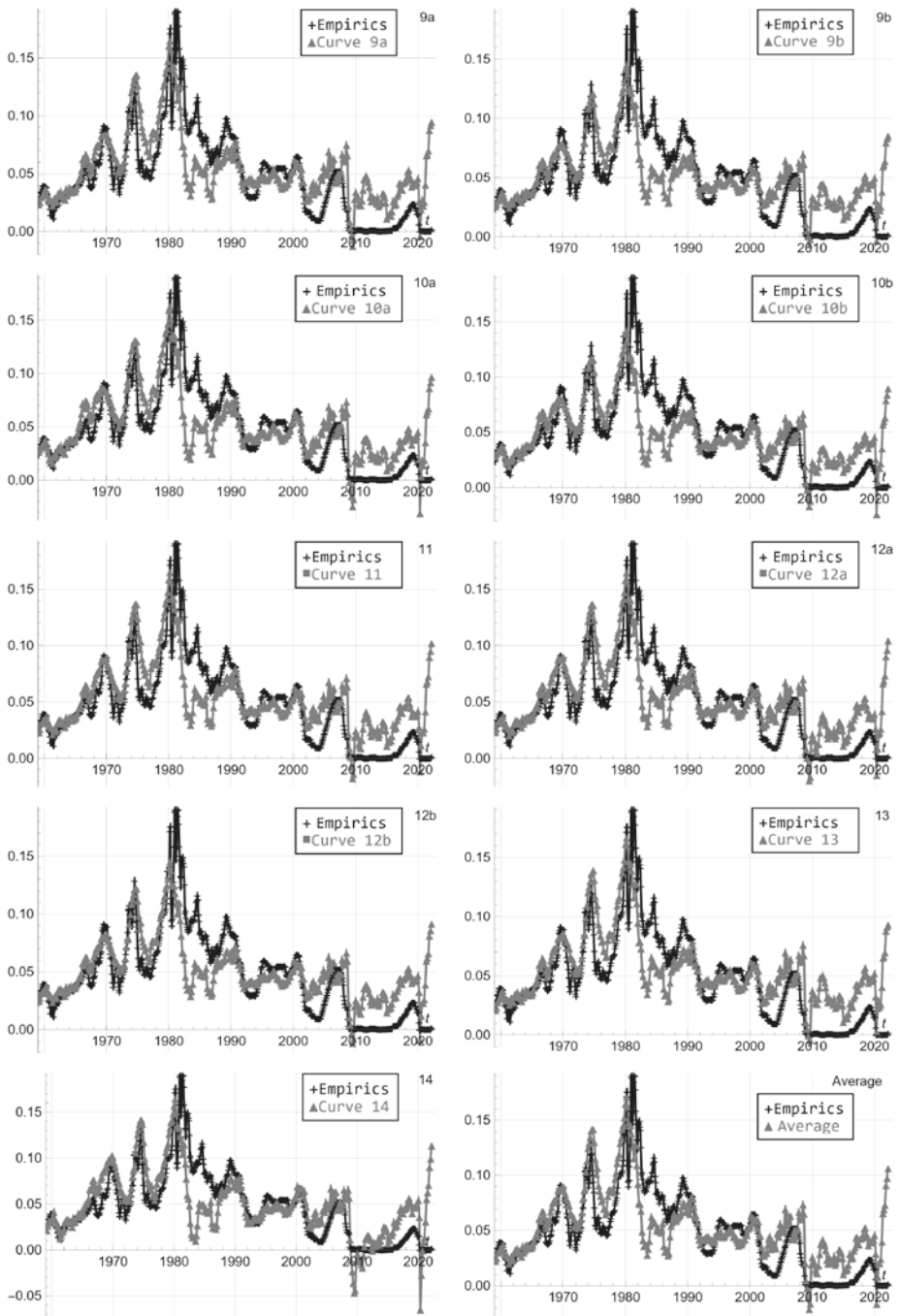
Figure 1 plots the empirical interest rate  $i_t$  with black "+", together with 27 curves for the interest rate  $i_t$  in (1) with red filled triangles according to Table 1. The

average and the standard deviation of these 27 curves are shown in the last two panels, which gives 29 panels.











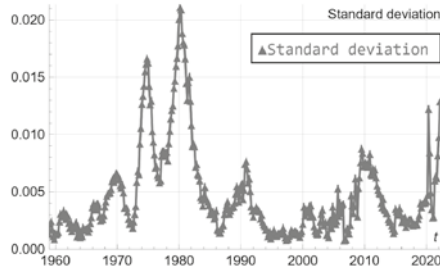


Figure 1. The Monthly US January 1, 1959 to March 31, 2022 empirical interest rate  $i_t$  and the interest rate  $i_t$  based on (1) with the following parameter values. Curve 1:  $a_\pi = a_y = 0.5, a_m = a_v = a_u = 0$ . Curve 2:  $a_\pi = a_y = a_m = a_v = a_u = 0.2$ . Curve 3a:  $a_\pi = a_y = a_m = 0.2, a_v = 0, a_u = 0.36$ . Curve 3b:  $a_\pi = a_y = a_m = 0.2, a_v = 0.04^*, a_u = 0.36$ . Curve 4a:  $a_\pi = a_y = 0.2, a_m = 0.25, a_v = 0, a_u = 0.35$ . Curve 4b:  $a_\pi = a_y = 0.2, a_m = 0, a_v = 0.17^*, a_u = 0.43$ . Curve 4c:  $a_\pi = a_y = 0.2, a_m = 0.03, a_v = 0.17^*, a_u = 0.4^*$ . Curve 5a:  $a_\pi = a_y = 0, a_m = a_v = 0.37, a_u = 0.26$ . Curve 5b:  $a_\pi = a_y = 0.16^*, a_m = a_v = 0.13, a_u = 0.42$ . Curve 6a:  $a_\pi = a_y = 0, a_m = 0.47, a_v = 0.18, a_u = 0.35$ . Curve 6b:  $a_\pi = a_y = 0.165^*, a_m = 0.11, a_v = 0.13, a_u = 0.43$ . Curve 7a:  $a_\pi = 0.2, a_y = 0.41, a_m = 0.17, a_v = 0, a_u = 0.22$ . Curve 7b:  $a_\pi = 0.2, a_y = 0.42, a_m = 0, a_v = 0.12^*, a_u = 0.26$ . Curve 7c:  $a_\pi = 0.2, a_y = 0.61, a_m = 0.06^*, a_v = 0, a_u = 0.13$ . Curve 7d:  $a_\pi = 0.2, a_y = 0.42, a_m = 0^*, a_v = 0.12^*, a_u = 0.26$ . Curve 8a:  $a_\pi = 0, a_y = 0.09, a_m = 0.44, a_v = 0.15, a_u = 0.32$ . Curve 8b:  $a_\pi = 0.16^*, a_y = 0, a_m = 0.32, a_v = 0.21, a_u = 0.31$ . Curve 8c:  $a_\pi = 0.17^*, a_y = 0.13^*, a_m = 0.15, a_v = 0.15, a_u = 0.4$ . Curve 9a:  $a_\pi = 0, a_y = 0.31, a_m = 0.4, a_v = 0.29, a_u = 0$ . Curve 9b:  $a_\pi = 0.16^*, a_y = 0.32, a_m = 0.24, a_v = 0.28, a_u = 0$ . Curve 10a:  $a_\pi = 0, a_y = 0.98, a_m = 0, a_v = 0, a_u = 0.02$ . Curve 10b:  $a_\pi = 0.17^*, a_y = 0.66, a_m = 0, a_v = 0, a_u = 0.17$ . Curve 11:  $a_\pi = 0, a_y = 0, a_m = 0.47, a_v = 0.18, a_u = 0.35$ . Curve 12a:  $a_\pi = 0, a_y = 0, a_m = 0.46, a_v = 0.1, a_u = 0.44$ . Curve 12b:  $a_\pi = 0.16^*, a_y = 0, a_m = 0.32, a_v = 0.21, a_u = 0.31$ . Curve 13:  $a_\pi = 0, a_y = 0, a_m = 0.51, a_v = 0.49, a_u = 0$ . Curve 14:  $a_\pi = 0, a_y = 0, a_m = 0, a_v = 0, a_u = 1$ . Curve Average: The average of these 27 curves. Curve Standard deviation: The standard deviation of these 27 curves. A superscript star \* after a number means that the corresponding sign in (1) is changed from plus to minus. No superscript star \* after a number means that only the plus signs in (1) are used.

These 27 curves are similar in some regards, but they are unique and present different features. Curve 1 presents the Taylor (1993) rule, i.e. assuming  $a_\pi = a_y = 0.5, a_m = a_v = a_u = 0$ . Among the 27 curves, the peak in 1980 for curve 1 is highest compared with the peaks in 1980 for all the 27 curves. Curve 1 predicts negative interest rate  $i_t$  from January 2009 to May 2009, and in March 2020. Curve 2 assumes  $a_\pi = a_y = a_m = a_v = a_u = 0.2$ , which fits the empirical interest rate  $i_t$  better than the Taylor (1993) rule. The peak of curve 2 in 1980 is close to the empirical interest rate  $i_t$ . The last two curves show the average interest rate  $i_t$  of the 27 curves, and the standard deviation of the interest rate  $i_t$ , respectively. Overall, the 27 curves show especially high variation for 1980, as the curve Standard deviation shows.

Table 2 shows that the Pearson correlation coefficients are high, ranging from 0.71 to 0.75 between the empirical interest rate  $i_t$  and the 27 curves. The correlations are even higher, ranging from 0.92 to 1 among the 27 curves.



**Table 2 Pearson correlation coefficients between the empirical interest rate  $i_t$  and the 27 curves - continued**

Curves	(16)	(17)	(18)	(19)	(20)	(21)	(22)	(23)	(24)	(25)	(26)	(27)	(28)	(29)
(1) Empirical														
(2) Curve1														
(3) Curve2														
(4) Curve3a														
(5) Curve3b														
(6) Curve4a														
(7) Curve4b														
(8) Curve4c														
(9) Curve5a														
(10) Curve5b														
(11) Curve6a														
(12) Curve6b														
(13) Curve7a														
(14) Curve7b														
(15) Curve7c														
(16) Curve7d	1.00													
(17) Curve8a	1.00	1.00												
(18) Curve8b	1.00	1.00	1.00											
(19) Curve8c	0.99	1.00	1.00	1.00										
(20) Curve9a	1.00	1.00	0.99	0.99	1.00									
(21) Curve9b	0.99	0.99	1.00	0.99	1.00	1.00								
(22) Curve10a	0.99	0.99	0.99	0.99	0.99	0.99	1.00							
(23) Curve10b	0.99	0.99	0.99	0.99	0.99	0.99	1.00	1.00						
(24) Curve11	1.00	1.00	1.00	1.00	1.00	0.99	0.99	0.99	1.00					
(25) Curve12a	1.00	1.00	1.00	1.00	0.99	0.99	0.99	0.99	1.00	1.00				
(26) Curve12b	1.00	1.00	1.00	1.00	0.99	1.00	0.99	0.99	1.00	1.00	1.00			
(27) Curve13	0.99	0.99	0.99	0.99	1.00	1.00	0.98	0.98	0.99	0.99	0.99	1.00		
(28) Curve14	0.95	0.97	0.97	0.97	0.94	0.95	0.97	0.98	0.97	0.97	0.97	0.93	1.00	
(29) Curve Average	1.00	1.00	1.00	1.00	1.00	1.00	0.99	0.99	1.00	1.00	1.00	0.99	0.96	1.00

## 4. Discussion

This article expands the Taylor (1993) rule by introducing three additional variables, i.e. the money supply, the money velocity, and the unemployment rate. The article also tests the various weights assigned to the deviations in inflation rate, real GDP, money supply, money velocity, and unemployment rate. Five results in the previous section are noteworthy. First, the Taylor (1993) rule does not explain the US empirical interest rate well. Among the Taylor (1993) rule, the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve, the Quantity Equation (Friedman, 1970) gives the lowest sum of the squared differences between the empirical interest rate and the predicted interest rate, followed by the Phillips (1958) curve and the Taylor (1993) rule, respectively. Second, the combination of the Taylor (1993) rule, the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve causes a substantially better result than the Taylor (1993) rule. Thus, incorporating the money supply, the money velocity and the unemployment rate substantially improves the accuracy compared with the Taylor (1993) rule. Third, the weight assigned to the unemployment rate should be relatively high. The Taylor (1993) rule assigns equal 0.5 weight to the deviation in inflation rate and the deviation in real GDP. The findings show that that may not be a good weight combination. Fourth, equal 0.2 weight to the deviations of inflation rate, real GDP, money supply, money velocity and unemployment rate decreases the sum of squared differences compared with the Taylor (1993) rule. Fifth, assuming two combinations, the Taylor (1993) rule and the Quantity Equation (Friedman, 1970) gives best result, followed by the Taylor (1993) rule and the Phillips (1958) curve, and finally, the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve. The results of these three combinations are similar.

The endogeneity problem, i.e. that some independent variables are not independent of the dependent variable, is commonly assessed related to the Taylor (1993) rule. Endogeneity is often problematic in an econometric approach, but can also arise in economics more generally. This article does not apply an econometric approach. The authors believe that endogeneity is a limited or not a problem for this article for the following reasons: The article assumes that the sum of the five weight parameters is one. The authors believe that the three additional variables are not highly correlated. The article does not introduce the money supply and the money velocity into the Taylor (1993) rule directly in (1). The term  $\text{Log} \left( \frac{m_t}{m_t} \right)$  for the money supply is a ratio which eliminates the scaling impact of the money supply. The term  $\text{Log} \left( \frac{v_t}{v_t} \right)$  for the money velocity is a ratio which eliminates the scaling impact of the money velocity. The term  $\text{Log} \left( \frac{y_t}{y_t} \right)$  for the GDP is a ratio which eliminates the scaling impact of the real GDP. Instead, these are loga-

rhythms of ratios, and thus not linear combinations of the relevant variables, which eliminates the scaling impact of these variables. A stationary test of endogeneity is common in time series analysis. This article does not use a time series analysis technique. Thus it is not feasible to conduct a stationary test. Instead this article conducts a robustness test by exploring various weights assigned to the five variables.

## 5. Limitations and future research

Conrad and Eife (2012) point out that the weights discussed in the previous sections are not fixed over time. One limitation of the Taylor (1993) rule, and also of this article assuming additional terms, is thus the assumption of constant weights through time. Future research may explore how these weights change dynamically over time.

Other potential limitations of the Taylor (1993) rule, combined or not combined with the other rules in this article, are the uncertainty of the level of potential real GDP, the long term real equilibrium interest rate, and the natural unemployment rate. One common challenge of the Taylor (1993) rule is to estimate the potential real GDP and thus the real GDP gap, i.e. the difference between the real GDP and the potential real GDP. Orphanides (2001) points out that the real GDP gap can look quite differently today as compared to the view in retrospect in some years. Hence, future research may find a better way to dynamically estimate the real GDP gap. This article assumes that the long term equilibrium real interest rate is 2%, which is commonly accepted, also in the Taylor (1993) rule. Laubach and Williams (2003) suggest that the equilibrium real interest rate is not stable over time. Thus, future research may find a way to better estimate the long term equilibrium real interest rate.

The central bank may adjust interest rates to the desired level gradually, i.e. "interest smoothing" (Judd & Rudebusch, 1998). Future research may incorporate additional lagged variables into the model, and explore non-lagged variables. Another limitation of this article and the Taylor (1993) rule is that these are backward looking approaches. In contrast, Clarida et al. (2000) explore a forward looking interest rate rule and recommend being forward looking in future research.

This article and the Taylor (1993) rule apply an in-sample fit approach. Qin and Enders (2008) compare the properties of the in-sample fit approach and the out-sample fit approach in the Taylor (1993) rule. They suggest that an

out-of-sample fit approach may be useful in selecting the alternative interest rate functional forms.

Future research may connect the interest rates in multiple countries and treat the global financial system as a whole. The interaction between interest rates, monetary policy and macroprudential policy may be examined. The data for various countries during different time periods may be explored accounting for specific economic changes. Interest rate rules during times of changes between positive and negative interest rates may be explored (Wang & Hausken, 2022a).

Other factors impacting interest rates may also be explored, e.g. economic crises, fiscal deficits, global interest rates, financial variables such as house prices, stock prices, leverage, oil and commodity prices (Kahn, 2010). Broader economic and financial theories may be incorporated to investigate potential further underlying mechanisms impacting interest rates.

## 6. Policy implications

Research on interest rates has progressed at a torrid pace in recent years. But central banks still face challenges when choosing monetary policy and determining interest rates, perhaps especially after the 2021-2022 pandemic crisis. The findings in this article provide insights relevant for the policy makers including central banks. First, the Taylor (1993) rule performs poorly in explaining the empirical interest rate. Hence, it is beneficial for the central bank to consider more factors beyond the Taylor rule when determining the interest rate. Second, the article presents a generalized interest rate rule, which combines the Taylor rule, the Quantity Equation (Friedman, 1970) and the Phillips (1958) curve. The model performs better than the Taylor rule. Three additional variables, i.e. the money supply, the money velocity and the unemployment rate help explain the interest rate more convincingly. Therefore, the central bank may consider these additional variables when determining the interest rate. Third, Taylor (1993) assigns equal 0.5 weight to the deviation in the inflation rate and the deviation in the real GDP. However, the article shows that these weights are not optimal. Higher weights assigned to the deviation in the unemployment rate, the deviation in the money supply and the deviation in the money velocity are appropriate. Fourth, interest rates impact households, firms and other actors substantially. For example, a lower interest rate may boost consumption, spending and borrowing. It may also encourage an entrepreneur to borrow funds for expansion, make new investments, and hire more workers. The findings of this article are believed to be

helpful for researchers, financial analysts, investors, entrepreneurs, consumers, etc., who may better predict interest rates and make better decisions.

## 7. Conclusion

This article provides a broad view of monetary policy starting from the Taylor (1993) rule. The article generalizes the Taylor rule to account for the money supply, the money velocity, and the unemployment rate. Thus, the article explores and tests various combinations of the Taylor rule, the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve. Five parameters are introduced and estimated; i.e. the weights assigned to the deviation in inflation rate, real GDP, money supply, money velocity, and the unemployment rate. The Taylor rule only has two parameters, i.e. the weights assigned to the deviation in real GDP and the deviation in the inflation rate. Various combinations of parameter values are explored and tested.

The generalized equation is tested using the monthly US January 1, 1959 to March 31, 2022 data. First, the Taylor rule is evaluated against the empirics. Second, equal weight to the five parameters is evaluated. Third, various values for these five parameters are explored and tested, such as equal weight to the deviation in the inflation rate and the deviation in the real GDP, equal weight to the deviation in the money supply and the deviation in the money velocity, and the values that represent various combinations of the Taylor (1993) rule, the Quantity Equation (Friedman, 1970), and the Phillips (1958) curve. The findings show that the generalized equation fits the empirical interest rate better and has a lower sum of squares compared with the Taylor rule. Notably, for the optimal values for the five parameters, the weights assigned to the deviation in inflation rate and the deviation in real GDP decrease compared with the Taylor rule. Meanwhile, the weight assigned to the deviation in unemployment rate is relatively high compared with the weights assigned to the deviation in inflation rate and the deviation in real GDP. The weights assigned to the deviation in money supply and the deviation in money velocity are moderate compared with the weights assigned to the deviation in inflation rate and the deviation in real GDP.

## Appendix A: Nomenclature

### *Parameters*

- $a_\pi$  Weight assigned to deviation in inflation,  $0 \leq a_\pi \leq 1$   
 $a_y$  Weight assigned to deviation in real GDP,  $0 \leq a_y \leq 1$   
 $a_m$  Weight assigned to deviation in money supply,  $0 \leq a_m \leq 1$   
 $a_v$  Weight assigned to deviation in money velocity,  $0 \leq a_m \leq 1$   
 $a_u$  Weight assigned to deviation in the unemployment rate,  $0 \leq a_m \leq 1$

### *Variables*

- $i_t$  Interest rate at time  $t$ ,  $i_t \in \mathbb{R}$   
 $\pi_t$  Inflation rate,  $\pi_t \in \mathbb{R}$   
 $\pi_t^*$  Target inflation rate,  $\pi_t^* \in \mathbb{R}$   
 $r_t^*$  Equilibrium real interest rate,  $r_t^* \in \mathbb{R}$   
 $y_t$  Real GDP (Gross Domestic Product),  $y_t \geq 0$   
 $\bar{y}_t$  Real potential GDP,  $\bar{y}_t \geq 0$   
 $m_t$  Money supply at time  $t$ ,  $m_t > 0$   
 $u_t$  Unemployment rate,  $u_t \geq 0$   
 $\bar{u}_t$  Natural rate of unemployment,  $\bar{u}_t \geq 0$   
 $t$  Time,  $t > 0$



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