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Research Report Modeling and solving a dynamic logistics network design problem with temporary capacity expansion and reduction

Schriftenreihe Logistik der Fakultät für Wirtschaftswissenschaften der htw saar, No. 21

Provided in Cooperation with: Saarland University of Applied Sciences (htw saar), Saarland Business School

Suggested Citation: Correia, Isabel; Melo, Teresa (2023) : Modeling and solving a dynamic logistics network design problem with temporary capacity expansion and reduction, Schriftenreihe Logistik der Fakultät für Wirtschaftswissenschaften der htw saar, No. 21, Hochschule für Technik und Wirtschaft des Saarlandes, Fakultät für Wirtschaftswissenschaften, Saarbrücken

This Version is available at: <https://hdl.handle.net/10419/303044>

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Schriftenreihe Logistik der Fakultät für Wirtschaftswissenschaften der htw saar

Technical reports on Logistics of the Saarland Business School

Nr. 21 (2023)

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ISSN 2193-7761

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Bericht/Technical Report 21 (2023)

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A Matheuristic for a Multi-period Logistics Network Design Problem with Short-term Capacity Adjustments

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Abstract

This study addresses a two-echelon network design problem that determines the location and size of new warehouses, the removal of company-owned warehouses, the inventory levels of multiple products at the warehouses, and the assignment of suppliers as well as customers to warehouses over a multi-period planning horizon. A distinctive feature of our problem is that new warehouses operate with modular capacities that can be expanded or reduced over several periods, the latter not necessarily having to be consecutive. Moreover, in every period, the demand of a customer for a given product has to be satisfied by a single warehouse. This problem arises in the context of warehousing-asa-service, a business scheme that offers flexible conditions for temporary capacity leasing. The associated fixed warehouse lease cost reflects economies of scale in the capacity size and the length of the lease contract. We develop a mixed-integer linear programming formulation and propose a matheuristic to solve this problem, which exploits the structure of the optimal solution of the linear relaxation to successively assign customers to open warehouses and fix other binary variables related to warehouse operation. Additional variable fixing rules are also developed, based on a scheme for managing inventories at warehouses and using the quantities provided by suppliers. Numerical experiments with randomly generated large-sized instances reveal that the proposed matheuristic outperforms a general-purpose solver in 74% of the instances by identifying higher quality solutions in a substantially shorter computing time.

Keywords: network design, temporary warehouse rental, capacity expansion and reduction, mixed integer programming, matheuristic

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1 Introduction

The location of facilities such as manufacturing plants, distribution centers and retail outlets is one of the most critical decisions to make when designing a logistics network. Typically, these decisions are strategic in nature, have a long-term impact, and strongly affect other decisions made at the tactical and operational levels. Location decisions are therefore unlikely to be reversible in the short or medium term (Cordeau et al., 2021; Melo et al., 2009). This is the case when facilities are built or purchased, as these actions require a sizeable financial investment. On the other hand, if facilities are rented or operations are subcontracted, location decisions may be reversible in the medium term. Warehousing-as-a-service is an emerging trend that casts location decisions as a tactical planning problem (Costa and Melo, 2024). This new business model offers flexible, short-term storage space as well as additional logistics services (e.g., goods handling) (Ceschia et al., 2023; Lahy et al., 2022). Thus, companies (e.g., omnichannel retailers) that need extra storage space on a temporary basis to deal with seasonal peaks and variations in demand find this model an opportunity to improve their efficiency and create competitive advantage. Warehousing as a service contrasts with the traditional model that entails long-term contracts, minimum volume commitments, and rigid pricing schemes to access warehouse capacity.

In this paper, we incorporate this new trend into the redesign of a two-echelon logistics network over a multi-period planning horizon. For this purpose, we assume that a company operates a number of warehouses at fixed locations and that there is a set of potential warehouses where additional storage capacity can be temporarily leased. Multiple (non-overlapping) leases can be taken out on the same warehouse for different sizes of capacity, allowing for expansion and reduction of storage space as needed. In addition, a lease contract on a warehouse can be terminated and subsequently resumed with the same or a different capacity. As shown in Figure 1, a set of suppliers provide various products that are consolidated in the (two types of) warehouses before being distributed to a set of customer zones to meet their demand. The aim is to specify a minimum cost schedule for the deployment of warehouses over the planning horizon. This includes discontinuing the operation of company-owned warehouses, leasing storage space at potential warehouses, and deciding how much capacity to lease in those facilities and for how long. Economies of scale are present in the fixed cost of a lease agreement, taking into account the amount of capacity leased and the term length. In addition, procurement, inventory, and distribution decisions for multiple product families also need to be made in each

Figure 1: Two-echelon network structure.

time period.

The main contributions of this study are threefold. First, we model a two-echelon network redesign problem in the context of tactical location planning that extends a particular case recently considered by Correia and Melo (2022). In contrast to the latter work, location decisions are combined with capacity sizing decisions for adding or removing modular units to/from leased warehouses. Furthermore, single-assignment conditions are enforced so that each customer zone is served by exactly one warehouse for a given product family in each period. As our numerical study will show, these settings result in a challenging mixed-integer linear programming (MILP) formulation for which the possibility of solving large-scale instances optimally with an off-theshelf optimization solver in acceptable time is rather limited. Hence, the second contribution is to develop an effective matheuristic, especially for large-sized problem instances resulting from an extended planning horizon and a significant number of customers. A feasible solution is constructed using an iterative scheme that jointly exploits the information provided by the linear (LP) relaxation and the capacity utilization level of the operating warehouses. This knowledge is then used to successively fix a subset of the binary variables. Additional mechanisms are developed to fix further binary variables, taking into account the residual capacities of suppliers and the amount of inventory available in warehouses as a result of decisions taken earlier. Variable fixing yields an MILP problem of smaller size which is then solved exactly using a general-purpose solver within a pre-defined time limit. The third contribution of our study is to evaluate the computational efficiency and quality of the proposed matheuristic for randomly generated problem instances, the larger of which has 48 time periods, 400 customer zones, and more than 1.2 million binary variables.

The remainder of this paper is organized as follows. Section 2 provides an overview of the relevant literature. In Section 3, a detailed description of the problem is given and a mathematical formulation is presented. The proposed matheuristic is detailed in Section 4, while Section 5 reports the results of our computational study. Finally, in Section 6, conclusions and directions for future research are provided.

2 Literature review

Facility location decisions are at the core of logistics network design problems (Cordeau et al., 2021; Melo et al., 2009). They typically involve determining the optimal number and location of facilities (e.g., manufacturing plants, warehouses) among a set of candidate sites. Naturally, these decisions are intertwined with multiple operations within the logistics network and must therefore be taken jointly with other decisions, such as allocating capacity to the selected facilities and setting the flow of products (e.g., procurement, production, distribution) across the network so that customer demand is satisfied at minimum cost or maximum profit. Regarding the planning horizon, logistics network design problems can be viewed from a static perspective (single period) or a dynamic perspective (multi-period). While the former may be appropriate when parameters (i.e., cost drivers, demand, etc.) are relatively stable, the latter allows for estimated parameter variations to be considered at the planning stage (Nickel and Saldanhada-Gama, 2019). In this section, we review the relevant literature, with a focus on multi-period capacitated network design problems, thereby highlighting how our study differs from previous work.

2.1 Multi-period capacitated network design

In a multi-period setting, gradual changes in the network configuration are, among others, triggered by capacity decisions. Not only is it necessary to determine the amount of capacity to be deployed in the new facilities when these are opened, but also to decide whether that capacity needs to be adjusted over time to respond to variations in costs and demand. A common approach is to assume a finite set of capacity levels at each potential location, with their acquisition costs reflecting economies of scale (Correia and Melo, 2016; Cortinhal et al., 2015; Martins et al., 2019; Thanh et al., 2008). In this case, the decision to open a facility is coupled with the selection of a single capacity level among the available options. Another approach is to assume that capacity is represented by modular units. A modular unit may be related to a specific type of equipment or qualified staff (Correia and Captivo, 2006). At each potential location, multiple units of the same module type can be installed provided that the sum of their capacities does not exceed a pre-specified limit. Again, the cost of deploying and operating a given number of modules at a specific location is subject to economies of scale. As shown in the recent survey by Alarcon-Gerbier and Buscher (2022), this form of capacity sizing is gaining increasing attention, with emerging applications in a variety of industries such as forestry, chemicals, healthcare, telecommunications and military logistics, among others.

In addition to capacity acquisition via the opening of facilities, other strategies may be adopted to scale the capacity available on the network over time. This is the case when existing facilities can also be closed, resulting in the reconfiguration of a logistics network already in place. The network redesign problems studied by Correia and Melo (2016), Cortinhal et al. (2015), Delmelle et al. (2014), and Martins et al. (2019) are examples of this strategy, which also allows for gradually expanding the network through opening additional facilities with specific capacity levels over the planning horizon.

Another way of modeling capacity adjustments is to temporarily close a facility and reopen it at a later time. Motivated by an application in the forestry sector, Jena et al. (2015b, 2016) investigate this problem variant. A further strategy for resizing capacity is to move capacity between different facilities in order to be in close proximity to demand markets or suppliers (Allman and Zhang, 2020; Becker et al., 2019; Melo et al., 2012).

The possibility of expanding and reducing the capacity of facilities during their operating term is an approach that has received less attention, but which increases the flexibility of the logistics network to respond to demand shifts. An early contribution addressing this case was

made by Antunes and Peeters (2001). In this study, the capacity of a facility can either be expanded or reduced, but not both, over the planning horizon. By contrast, Wilhelm et al. (2013) allow the configuration of a facility to be changed more than once over time through adding or removing a capacity level. A similar approach is adopted by Correia and Melo (2017, 2021) for a problem variant with customers segmented into two groups that differ in the delivery time they accept for meeting their orders. Jena et al. (2015a, 2017) propose a general model to represent different types of capacity changes. Their framework is based on tracking the number of modular units a facility holds in two consecutive time periods. If these two values differ, then a resizing of the capacity has occurred. This allows modeling not only the expansion and reduction of the capacity of a facility, but also its temporary removal and subsequent reopening. These features are also captured in our study, but in a different context, where decisions on facility location and capacity sizing are tactical rather than strategic in nature. As a result, the length of the planning horizon we consider in our numerical study is significantly longer than the one selected by Jena et al. (2015a, 2017), which greatly increases the size of our problem instances. Moreover, the logistics network in our work includes an additional layer (recall the supplier layer in Figure 1) and customer single-assignment conditions are imposed, thereby further adding to the complexity of the problem.

In the context of location decisions being reversible in the medium or even short term (e.g., quarterly or monthly), the literature is considerably scarcer. An early contribution was made by Thanh et al. (2008) to redesign a three-echelon production and distribution network. Manufacturing plants and company-owned warehouses that are in place at the beginning of the planning horizon can be closed or have their capacity extended over time, but not both. In addition, public warehouses can be rented for periods of time that need not be consecutive. However, a minimum interval of two periods is enforced between two rental contracts at the same public warehouse, which is a rather restrictive condition that we do not consider in our problem. The three-echelon network design problem studied by Badri et al. (2013) and Bashiri et al. (2012) also includes private and public warehouses, but no fixed costs for renting storage space at public facilities are incurred. As a result, economies of scale are not present in the cost of acquiring capacity from these facilities. In the two-echelon logistics network design problem addressed by Darvish and Coelho (2018), distribution centers can be rented with unlimited capacity for a pre-specified number of time periods. By contrast, in the problem we study, the lease term in a selected facility is an endogenous decision, as is the amount of capacity to be deployed (i.e. the number of modular units), with the later being scalable over time. Unnu and

Pazour (2022) also assume that when a so-called on-demand warehouse is rented with a certain capacity level, this facility remains open for a pre-defined number of time periods. In addition, the warehouse rental cost does not take into account economies of scale, but is determined by a fixed rate multiplied by the length of the lease. Recently, Clavijo López et al. (2023) also considered a pre-defined contract duration to operate potential cross-docking facilities owned by different carriers. Successive contracts can be in place with a given carrier, thus allowing the reopening of cross-docking facilities. Moreover, the capacity sizing of these facilities is also addressed through the selection of a capacity level from a set of available options.

The problem investigated in this paper draws on previous work by Correia and Melo (2022), which was the first to integrate the temporary rental of a subset of facilities into a two-echelon network redesign problem and where the duration of lease contracts is an endogenous decision. As will be detailed in the next section, the problem studied here captures additional features, namely it is possible to expand and reduce capacity in facilities that are leased on a temporary basis and single-assignment conditions to meet customer demand for a particular product are enforced. It is worth noting that the latter feature has not been widely studied in the literature. In addition, Correia and Melo (2022) use a general-purpose optimization solver, whereas we propose a specially-tailored heuristic procedure.

2.2 Solution approaches

Multi-period capacitated network design problems belong to the class of $N \mathcal{P}$ -hard optimization problems as they are generalizations of the uncapacitated facility location problem which is a well-known $\mathcal N \mathcal P$ -hard problem (Krarup and Pruzan, 1983). Incorporating decisions beyond that of facility location into the planning of a logistics network configuration makes this type of problems even more challenging in terms of identifying high-quality solutions within reasonable computing time using off-the-shelf optimization solvers (Bashiri et al., 2012; Correia and Melo, 2016, 2017; Cortinhal et al., 2015; Delmelle et al., 2014; Jena et al., 2015a,b; Martins et al., 2019; Thanh et al., 2008; Unnu and Pazour, 2022; Wilhelm et al., 2013). For this reason, a great deal of effort has been devoted to developing optimization techniques (e.g., MILP-based decomposition methods, meta- and matheuristics) capable of providing good solutions to the problem under study within acceptable time, particularly for large-scale instances. While some exact solution approaches such as branch-and-price (Allman and Zhang, 2020) and Benders Decomposition (Clavijo López et al., 2023) have been proposed for this class of location problems,

most contributions resort to heuristic strategies based on, for example, Lagrangean relaxation (Badri et al., 2013; Jena et al., 2016, 2017), local search (Sauvey et al., 2020), simulated annealing (Antunes and Peeters, 2001), tabu search (Melo et al., 2012), evolutionary algorithms (Silva et al., 2021), and DC programming (Thanh et al., 2012), among others.

Matheuristics have become a popular family of solution approaches for handling many optimization problems (Boschetti et al., 2023), including facility location problems. For example, Darvish and Coelho (2018) combine variable neighborhood search with an exact method to solve a two-echelon logistics network design problem. Another way to construct feasible solutions is to use the information gained from the optimal solution to the linear relaxation of the original integer problem. In this case, an (iterative) rounding procedure is typically applied to the fractional variables, together with a mechanism that repairs infeasibilities (Silva et al., 2021; Thanh et al., 2010). The matheuristic that we propose in this paper also draws on information provided by the LP relaxation, but unlike the aforementioned works, it does not employ a rounding procedure. Instead, and since some binary variables take integer values in the LP relaxation (the details will be presented in Section 4), specific rules are developed to decide which of them should be fixed in the original problem. This approach is combined with additional schemes to fix further binary variables. To the best of our knowledge, our study is the first to present a matheuristic for a multi-period logistics network redesign problem at the tactical level, involving location and capacity scalability decisions over a multi-period planning horizon.

3 Problem description and mathematical formulation

The problem investigated in this study is characterized as follows:

- A time horizon for planning, divided into a finite number of periods.
- A set of suppliers offering several product families and having varying capacity over the planning horizon.
- A set of capacitated warehouses belonging to a company or rented from a logistics service provider, and operating at the beginning of the planning horizon. Without loss of generality, these facilities are referred to as company-owned warehouses.
- A set of potential warehouses where capacity can be leased for a variable timeframe. The storage space at each location is set up by the number of modular units that are leased, which cannot be greater than a pre-specified number. For the sake of simplicity, a single type of modular unit with a fixed size is considered at all potential locations.
- Rental of space in a potential warehouse location for multiple periods with varying capacity. Thus, over the planning horizon, the number of modules leased can be extended or reduced at the same facility. Furthermore, the lease periods need not be consecutive. Consequently, multiple lease agreements may be established at the same location, as long as they do not overlap.
- A set of customer zones with known demand for multiple product families in each time period.
- Single-assignment conditions for meeting the demand of a customer zone for a given product family from a single warehouse in each time period.
- Inventories in both company-owned and leased warehouses that can be carried over from one period to the next for the duration of the warehouse's operation and which incur variable holding costs.
- No initial and ending inventories in any storage location.
- Fixed lease costs at new warehouse locations reflecting economies of scale with respect to volume and commitment duration.
- Fixed costs for operating and discontinuing the activity of company-owned warehouses.
- Variable costs for distributing products from suppliers to warehouses and from the latter to customer zones.

The problem considers the distribution of multiple product families from suppliers to customer zones via company-owned and leased warehouses while satisfying demand requirements. This involves defining a schedule for discontinuing the activity of the company-owned warehouses and a schedule for leasing storage space in new locations, as well as sizing their capacity, which may be temporarily expanded or reduced. The objective is to minimize the total cost, which includes fixed costs for leasing new storage space, fixed costs for operating and removing company-owned warehouses, and variable distribution and inventory holding costs.

Next, the notation is introduced and then the mathematical formulation is presented, which is extended from Correia and Melo (2022).

Sets

- T Set of discrete time periods in the planning horizon; the last time period is denoted by n_T .
- S Set of suppliers.
- I^e Set of company-owned warehouses that are operating at the beginning of the planning horizon.
- I^n Set of potential warehouses where storage space can be leased on a temporary basis.
- I Set of all warehouse locations, $I = I^e \cup I^n$ with $I^e \subseteq I$, $I^n \subseteq I$, and $I^e \cap I^n = \emptyset$.
- J Set of customer zones.
- P Set of product families.

Parameters related to suppliers, warehouses, and customer zones

- SQ_{sn}^t Capacity of supplier $s \in S$ for product family $p \in P$ at time period $t \in T$.
- Q_i Available storage capacity of company-owned warehouse $i \in I^e$.
- β_p Amount of capacity used by one unit of product family $p \in P$ stored at warehouse $i \in I$.
- u_{ii}^0 Amount of product family $p \in P$ held in stock in warehouse $i \in I$ at the beginning of the planning horizon. Without loss of generality, it is assumed that $u^0_{ip}=0$ for all $i \in I$ and $p \in P$.
- d^t_i Demand of customer zone $j \in J$ for product family $p \in P$ at time period $t \in T$.
- M_i Capacity of one modular unit at warehouse location i $(i \in Iⁿ)$.
- n_i Maximum number of modular units that can be leased in warehouse i in any time period $(i \in Iⁿ)$.

Cost parameters

- OC^t i_t^t Fixed cost of operating the company-owned warehouse $i \in I^e$ at time period $t \in T.$
- FC_i^t i_t^t Fixed cost of discontinuing the operation of the company-owned warehouse $i \in I^e$ at the *beginning* of time period $t \in T$.
- $L_{ik}^{t,t'}$ $\mathcal{I}_{ik}^{t,t'}$ Total fixed cost of leasing warehouse $i\in I^n$ with k modular units $(k=1,\ldots,n_i)$ from the beginning of time period t until the end of time period t' $(t, t' \in T; t' \geq t)$.
- SC_{sin}^{t} Cost of distributing one unit of product family $p \in P$ from supplier $s \in S$ to warehouse $i \in I$ at time period $t \in T$.
- DC_{ijp}^t Cost of distributing one unit of product family $p \in P$ from warehouse $i \in I$ to customer zone $j \in J$ at time period $t \in T$.
- IC_{ip}^t Cost of storing one unit of product family $p \in P$ in warehouse $i \in I$ at the end of time period $t \in T$.

The decisions that need to be made are represented by three sets of binary variables and two sets of (non-negative) continuous variables.

Binary variables

- y_i^t $i = 1$ if the company-owned warehouse i ceases to be operated at the beginning of time period t, and 0 otherwise $(i \in I^e, t \in T)$.
- $z_{ik}^{t,t'}$ $i=1$ if the new warehouse i is leased with k modular units from the beginning of time period t until the end of time period t' , and 0 otherwise $(i \in I^n, t, t' \in T, t' \geq t$, $k = 1, \ldots, n_i$.
- x_i^t $i=1$ if the demand of customer zone j for product family p is served by warehouse i at time period t, 0 otherwise $(i \in I, j \in J, p \in P, t \in T)$.

Continuous variables

- v_s^t Quantity of product family p distributed from supplier s to warehouse i at time period t $(s \in S, i \in I, p \in P, t \in T)$.
- u_i^t Quantity of product family p held in stock in warehouse i at the end of time period $t (i \in I, p \in P, t \in T).$

The MILP formulation is as follows:

Min
$$
\sum_{i \in I^e} \sum_{t \in T} OC_i^t \left(1 - \sum_{t'=1}^t y_i^{t'}\right) + \sum_{i \in I^e} \sum_{t \in T} FC_i^t y_i^t + \sum_{i \in I^n} \sum_{k=1}^n \sum_{t \in T} \sum_{t' \in T} L_{ik}^{t,t'} z_{ik}^{t,t'} + \sum_{s \in S} \sum_{i \in I} \sum_{p \in P} \sum_{t \in T} SC_{sip}^t v_{sip}^t + \sum_{i \in I} \sum_{j \in J} \sum_{p \in P} \sum_{t \in T} DC_{ijp}^t d_{jp}^t x_{ijp}^t + \sum_{i \in I} \sum_{p \in P} \sum_{t \in T} IC_{ip}^t u_{ip}^t
$$
\n(1)

subject to

$$
\sum_{t \in T} y_i^t \le 1 \qquad i \in I^e \tag{2}
$$

$$
\sum_{k=1}^{n_i} \sum_{m=1}^t \sum_{m'=t}^{|T|} z_{ik}^{m,m'} \le 1 \qquad i \in I^n, \ t \in T \tag{3}
$$

$$
\sum_{i \in I} v_{\text{sip}}^t \le SQ_{\text{sp}}^t \qquad \qquad s \in S, \ p \in P, \ t \in T \tag{4}
$$

$$
u_{ip}^{t-1} + \sum_{s \in S} v_{sip}^t = u_{ip}^t + \sum_{j \in J} d_{jp}^t x_{ijp}^t \qquad i \in I, \ p \in P, \ t \in T
$$
 (5)

$$
\sum_{p \in P} \beta_p u_{ip}^{t-1} + \sum_{s \in S} \sum_{p \in P} \beta_p v_{sip}^t \le Q_i \left(1 - \sum_{t'=1}^t y_i^{t'} \right) \qquad i \in I^e, \ t \in T
$$
\n(6)

$$
\sum_{p \in P} \beta_p u_{ip}^{t-1} + \sum_{s \in S} \sum_{p \in P} \beta_p v_{sip}^t \le M_i \sum_{k=1}^{n_i} \sum_{m=1}^t \sum_{m'=t}^{|T|} k z_{ik}^{m,m'} i \in I^n, t \in T
$$
\n(7)

$$
\sum_{p \in P} \beta_p u_{ip}^{t-1} \leq M_i n_i \left(1 - \sum_{k=1}^{\lfloor n \rfloor} \sum_{t'=t}^{\lfloor T \rfloor} z_{ik}^{t,t'} \right) + M_i \sum_{k=1}^{\lfloor n \rfloor} \sum_{t'=1}^{\lfloor t \rfloor - 1} k z_{ik}^{t',t-1} \qquad i \in I^n, t \in T \setminus \{1\}
$$
\n
$$
(8)
$$

$$
u_{ip}^{|T|} = 0
$$
\n
$$
i \in I, p \in P
$$
\n
$$
j \in J, p \in P, t \in T
$$
\n(9)\n
$$
j \in J, p \in P, t \in T
$$
\n(10)

$$
i \in I^e, t \in T
$$

\n
$$
y_i^t \in \{0, 1\}
$$

\n
$$
i \in I^e, t \in T
$$

\n
$$
i \in I^n, k = 1, ..., n_i,
$$

\n(11)

 $t, t' \in T, t' \geq t$ (12)

$$
x_{ijp}^t \in \{0, 1\}
$$

\n
$$
i \in I, j \in J, p \in P, t \in T
$$

\n
$$
v_{sip}^t \ge 0
$$

\n
$$
s \in S, i \in I, p \in P, t \in T
$$

\n(14)

$$
u_{ip}^t \ge 0 \qquad \qquad i \in I, \ p \in P, \ t \in T \tag{15}
$$

The first two components of the objective function (1) represent the fixed costs to operate and remove company-owned warehouses, respectively. The third component of (1) gives the total fixed cost of leasing storage space in new warehouses. The total costs of distributing the product families from the suppliers to the warehouses and from the latter to the customer zones are calculated in the fourth and fifth components, respectively. The last component determines the total inventory holding cost at the warehouses.

Constraints (2) allow the activity of each company-owned warehouse to be terminated at most once during the planning horizon. Hence, when the warehouse activity is discontinued, it cannot be restored later. Constraints (3) guarantee that multiple contracts cannot be in place at the same new warehouse location with overlapping rental periods. In addition, these constraints also ensure that at each potential warehouse location a single capacity size (i.e., a fixed number of modular units) can be selected during the lease term of a given contract. Inequalities (4) pertain to supplier capacities. At each time period, inventory balance conditions are imposed by constraints (5) for every product family and warehouse location. The capacities of company-owned warehouses and leased warehouses are enforced through constraints (6) and (7) in each time period, respectively. The latter constraints also guarantee that when a lease commitment is not in place on a new warehouse in a given period (i.e., the right-hand side of the associated inequality is zero), the inventory level must be equal to zero at the end of the previous period. Constraints (8) ensure that no inventory is held in a new warehouse at the beginning of the first period in which the lease takes effect, unless another contract was in place at that location in the preceding period. If a given warehouse is leased with m modular units until the end of some period t, and a new lease begins in period $t + 1$ with m' modular units, then constraints (7) and (8) govern the maximum quantity that can be held in stock at the end of each period. If $m < m'$ (i.e., capacity expansion occurs), then the inventory level at the end of period t is at most as large as the total capacity of the m modules. In the opposite case, i.e. $m \geq m'$ (capacity reduction), the stock level at the end of period t cannot exceed the total capacity of m' modular units. Equalities (9) enforce the inventory level to be zero at the end of the planning horizon for any product family and in any warehouse. Constraints (10) dictate that each customer zone be served by exactly one warehouse for a given product family in each period. Finally, binary and non-negativity conditions are imposed by constraints (11) – (15) .

In the following, formulation (1) – (15) will be denoted by (\mathcal{M}) . This formulation differs from that of Correia and Melo (2022) in three ways. First, the storage capacity in new warehouses is given by the number of modular units that are leased, and this number can vary over the planning horizon (i.e., increase or decrease), thus enhancing the flexibility to respond to variations in costs and demand. In the problem studied by Correia and Melo (2022), in each new warehouse, all lease commitments include the same fixed amount of capacity, thereby precluding the adjustment of capacity to respond to variations in demand. Second, since in the new problem there may be multiple consecutive lease agreements at the same warehouse for a varying number of modular units, inventory can be transferred from one contract to the next, a feature that was also not captured by Correia and Melo (2022). The third important difference concerns the fact that each product family has to be distributed by a single warehouse to a customer zone to meet its demand at a given period. The associated single-assignment constraints (10) are not present in the model of Correia and Melo (2022) and pose significant challenges due to the large number of additional binary variables (x) that have to be defined. However, many companies favor this distribution strategy because it simplifies the management of their supply chain and can also reduce operational costs. On the other hand, customers also often prefer to be supplied by a single facility for a particular product, as they can take advantage of lower distribution costs due to higher shipping volumes. Observe that we do not enforce in formulation (M) that each customer zone be served by a single warehouse for all product families, in order to mitigate the risk of supply disruption due to dependence on a single source. Owing to these differences, formulation (M) extends that of Correia and Melo (2022) and results in a very challenging problem for which the chance of a state-of-the-art MILP solver to identify (near-)optimal solutions for large-scale instances within acceptable time is rather limited, as our computational study in Section 5 will demonstrate.

4 Matheuristic

An in-depth analysis of the characteristics of the optimal solution to the LP relaxation of formulation (M) , for a preliminary set of randomly generated problem instances, revealed that a very large number of customer assignment variables x are binary in that solution (an average of 99%). This feature motivated the development of the matheuristic that will be presented in this section. In addition to selecting a subset of the binary variables x in the LP solution that will be retained in the original MILP problem according to specific rules, several additional schemes to fix further binary variables are also embedded in an attempt to obtain feasible solutions of superior quality. Figure 2 summarizes the various steps of the proposed matheuristic, while Algorithm 1 describes the general framework.

Initially, the binary variables x, y and z are free, being gathered in the sets X_{nf} , Y_{nf} and Z_{nf} , respectively (lines 3–6 in Algorithm 1). Throughout the heuristic procedure, some (or all) binary variables will be successively fixed according to different rules, and moved to sets X_f , Y_f and Z_f . In the first phase of the heuristic (lines 8–12), variable fixing decisions build upon infor-

Figure 2: Flowchart of the proposed methodology.

mation drawn from the optimal solution $(\overline{x}, \overline{y}, \overline{z}, \overline{u}, \overline{v})$ to the LP relaxation of a residual problem. The latter corresponds to the original MILP problem (M) with a subset of the binary variables having fixed values. Naturally, the first time this mechanism is employed, the residual problem coincides with the original problem. Procedures AssignCustomersToCompanyWarehouses and AssignCustomersToNewWarehouses (lines 10-11) include the rules governing variable fixing that are applied to the optimal solution of the last relaxed problem solved. They rely on the identification of those warehouses that are operating and whose capacity utilization rate for meeting the demand of selected customer zones and holding stock is equal to or even exceeds a pre-specified threshold α ($0 < \alpha < 1$) in a certain period. Details are provided in Section 4.1. Each time the values of (some) binary variables x, y and z are fixed, the LP relaxation of the resulting residual problem is solved optimally. This process is repeated until no more variable fixing occurs.

In the next phase of the matheuristic (lines 13–23), an attempt is made to fix the values of further binary variables. For this purpose, we first estimate in each time period and for every product family the total quantity provided by suppliers that has not yet been consumed due to decisions related to set X_f . Moreover, we also estimate the inventory level in each warehouse and time period that has not yet been used to serve the customer demands associated with set

 X_f . These calculations are performed in Procedures InitializeSupplyAndInventory and UpdateSupplyAndInventory (lines 13–14), see Section 4.2 for a detailed description. Next, and following Procedure AssignMoreCustomersToCompanyWarehouses (Section 4.3), we try to assign more customer zones to company-owned warehouses with sufficient residual capacity to meet their demand, taking into account the available supply and inventory levels. Preference is given to customer zones with lower unit distribution costs. A similar strategy is also adopted to extend the set X_f with additional assignments of customer zones to leased warehouses (see Procedure AssignMoreCustomersToNewWarehouses in Section 4.3). In this case, we first determine the number of modular units that should be operated in each period in a leased warehouse due to previously having fixed some variables x (Procedure IdentifyModularUnits, line 21). If either or both of these mechanisms succeed (lines 17 and 23), we explore the LP relaxation of the associated residual problem, repeating the cycle in lines 8–12. Otherwise, and since no more binary variables were fixed, we solve a restricted MILP problem with the choices made so far (line 26). To this end, a general-purpose MILP solver is used. If it is not possible to identify a feasible solution to this residual MILP problem within a pre-specified time limit $Tmax$, the capacity threshold α is decreased by a given amount θ . The matheuristic stops when a feasible solution to the original problem is returned or when the parameter α becomes negative, which means that no feasible solution could be identified. We emphasize that in all the computational experiments we have performed, we have always obtained a feasible solution with the initial choice of the capacity threshold (α_0 , see line 1 in Algorithm 1), and therefore it was never necessary to decrease α and re-run the matheuristic.

4.1 Using the LP relaxation for variable fixing

As stated at the beginning of Section 4, in our set of test instances, an average of 99% of the customer assignment variables x take on the value 0 or 1 in the optimal LP solution. While a natural approach would be to retain all these values in the original formulation (\mathcal{M}) , this could lead to some warehouses being in place to serve a relatively small amount of demand in a given period, thus producing a costly solution. To overcome the potential risk of obtaining an inferior solution, we carefully select, from among the variables \bar{x} with value equal to 1, those that we will transfer to the set X_f . This choice is based on the amount of capacity used by a warehouse in a given period for meeting the demand of the (fully) assigned customer zones and holding inventory, according to the components of the LP solution for that warehouse and period. If the warehouse load rate reaches or even exceeds a certain threshold α , then these customer assignments are retained. For company-owned warehouses $i \in I^e$, these steps are described in lines 4–7 of Procedure AssignCustomersToCompanyWarehouses for every period $t \in T$. Fixing one or several variables x_{ijp}^t at one implies that warehouse i has to be open from the beginning of the planning horizon until the period t under consideration. Hence, variables y_i^1,\ldots,y_i^t are also fixed at zero (lines 9—10). Furthermore, due to the single-assignment conditions (10) , we also set $x_{i'jp}^t = 0$ for all warehouses $\imath' \in I^e \setminus \{i\}.$

Algorithm AssignCustomersToCompanyWarehouses: Assignment of customer zones to company-owned warehouses over the planning horizon using information drawn from the optimal solution to the LP relaxation of the residual MILP problem

Input : α , \overline{x} , \overline{u} , x , y , X_f , X_{nf} , Y_f , Y_{nf} **Output:** Additional fixing of variables x, y ; updated sets X_f , X_{nf} , Y_f , Y_{nf} 1 for $i \in I^e$ do 2 for $t \in T$ do
3 $\left| \begin{array}{c} f \text{ or } t \in T \end{array} \right|$ // determine warehouse capacity utilization level to serve demands of assigned customer zones and to hold inventory according to LP solution $4 \mid WCL :=$ \sum $j\in J$, $p\in P$: $\overline{x}_{ijp}^{t} = 1$ $\beta_p d_{jp}^t + \sum$ $\sum_{p\in P}\beta_p\,\overline{u}_{ip}^t$ Q_i $\begin{array}{c|c|c|c} \text{5} & \text{if } WCL \geq \alpha \text{ then} \end{array}$ 6 For all $j \in J$ and $p \in P$ such that $\overline{x}_{ijp}^t = 1$ and $x_{ijp}^t \in X_{nf}$, fix $x_{ijp}^t := 1$ and $x_{i'jp}^t := 0$ for all $i' \in I^e \setminus \{i\}$ τ | | Move all fixed variables from $X_{n,f}$ to X_f \vert 8 \vert \vert // company-owned warehouse i must be open at least until period t 9 | | \int for $\tau := 1$ to t do 10 if $y_i^{\tau} \in Y_{nf}$ then fix $y_i^{\tau} := 0$ and move this variable from Y_{nf} to Y_f 11 end 12 end $_{13}$ end ¹⁴ end 15 return $x, y, X_f, X_{nf}, Y_f, Y_{nf}$

A similar mechanism is applied to locations where storage space can be leased, as described in Procedure AssignCustomersToNewWarehouses. In this case, it is first required to identify for each location $i \in I^n$ and period $t \in T$ the number of modular units (\overline{m}) needed to cover the total quantity processed by that warehouse (line 4). Note that this quantity corresponds to all the demand fully satisfied by the warehouse and the amount of inventory built up in this facility, according to the information drawn from the linear relaxation. After fixing some variables x at 1 (lines 8–9) following the same rule as described before, we determine a lower bound Δ on the number of modular units at location i and period t (line 11), by disregarding the information on inventory holding from the LP relaxation. Observe that the matheuristic is concerned with fixing the values of (a subset of) the binary variables, deferring all decisions about the quantities to be distributed and stored (i.e., the values of the continuous variables

Algorithm AssignCustomersToNewWarehouses: Assignment of customer zones to leased warehouses over the planning horizon using information drawn from the optimal solution to the LP relaxation of the residual MILP problem

Input : α , \overline{x} , \overline{u} , x , z , \overline{X}_f , \overline{X}_{nf} , \overline{Z}_f , \overline{Z}_{nf} **Output:** Additional fixing of variables x, z; updated sets X_f , X_{nf} , Z_f , Z_{nf} 1 for $i \in I^n$ do 2 for $t \in T$ do ³ // identify the number of modular units required to hold inventory and serve demands assigned to warehouse i in period t 4 $\boxed{m} :=$ $\sqrt{ }$ the contract of the contract of the contract of \sum $j\in J, p\in P: \overline{x}_{ijp}^{t} = 1$ $\beta_p d_{jp}^t + \sum$ $\sum_{p\in P}\beta_p\,\overline{u}_{ip}^t$ M_i 1 $\overline{}$ $\overline{1}$ ⁵ // determine the warehouse capacity utilization level 6 | $WCL :=$ \sum $j\in J$, $p\in P$: $\overline{x}_{ijp}^{t} = 1$ $\beta_p d_{jp}^t + \sum$ $\sum_{p\in P}\beta_p\,\overline{u}_{ip}^t$ $\overline{m} \times M_i$ 7 if $WCL \geq \alpha$ then 8 For all $j \in J$ and $p \in P$ such that $\overline{x}_{ijp}^t = 1$ and $x_{ijp}^t \in X_{nf}$, fix $x_{ijp}^t := 1$ and $x_{i'jp}^t := 0$ for all $i' \in I^n \setminus \{i\}$ 9 | | Move all fixed variables from X_{nf} to X_f 10 // identify the minimum number of modular units required to meet the demand of customers assigned to warehouse i in period t due to variable fixing 11 $\Delta :=$ $\sqrt{ }$ $\begin{matrix} \end{matrix}$ $\mathbf{1}$ and $\mathbf{1}$ and $\mathbf{1}$ \sum $j\in J$, $p\in P$: $x_{ijp}^t = 1$ $\beta_p d_{jp}^t$ M_i 1 $\begin{matrix} \end{matrix}$ 12 // \vert // any lease contract covering period t cannot include fewer than Δ modular units 13 for $k := 1$ to $\Delta - 1$ do ¹⁴ for τ := 1 to t do $\begin{array}{|c|c|c|c|c|}\hline \hspace{0.2cm} \text{15} & & \end{array} \hspace{0.2cm} \begin{array}{|c|c|c|c|}\hline \hspace{0.2cm} \text{16} & & \end{array} \hspace{0.2cm} \text{for } \tau' := t \text{ to } |T| \text{ do}$ 16 if $z_{ik}^{\tau,\tau'} \in Z_{nf}$ then fix $z_{ik}^{\tau,\tau'} := 0$ and move this variable from Z_{nf} to Z_f 17 | | | | | end 18 end 19 end 20 Add the following constraint to the LP relaxation of residual problem ensuring that warehouse *i* is leased in period t with at least Δ modular units: $\sum_{i=1}^{n}$ $k=\Delta$ $\sum_{i=1}^{t}$ $\tau=1$ $\frac{|T|}{\sum}$ τ ^{τ} $=t$ $z_{ik}^{\tau,\tau'} \geq 1$ $_{21}$ end 22 end ²³ end 24 return $x, z, X_f, X_{nf}, Z_f, Z_{nf}$

 v and u) to a later stage, where a general-purpose MILP solver is used. This explains the calculation of Δ . Given Δ , it is clear that any lease commitment in place at period t cannot include fewer than Δ modules. As a result, a subset of variables z can be fixed at zero for all leases with k modular units such that $1 \leq k < \Delta$ (lines 13–19). Moreover, the LP relaxation of the resulting residual problem is strengthened by adding an inequality guaranteeing that a valid lease contract at location i and period t must have at least Δ modular units (line 20).

4.2 Identification of available supply and inventory levels

Solving the LP relaxation of a residual problem that no longer allows fixing variables x (and as a result, y and z too) sets the end of the first phase. The associated optimal LP solution serves as a starting point for the next phase, which aims to fix some more binary variables driven by the assignment of additional customer zones to open warehouses. This requires first identifying in every period the quantity of each product family that can be made available by suppliers and that has not yet been used. In addition, it is also necessary to determine the amount of stock in every open warehouse at the end of each period that has not yet been consumed.

For each warehouse and time period, the flow conservation constraints (5) set the link between supply, inventory, and demand for a given product family. However, they do not specify whether demand is entirely satisfied from suppliers, from inventory on hand, or from a combination of both sources. As a result, at the beginning of the second phase we are unable to deduce the exact quantities of each product family that are available to serve customer zones not yet assigned to any warehouse. To overcome this lack of information, we estimate these quantities based on certain assumptions. To this end, we start by creating two vectors, TS and Inv in Procedure InitializeSupplyAndInventory, that aggregate the total quantity of each product family made available by suppliers and the inventory level in each warehouse (according to the optimal LP solution, see lines 2–3) over the planning horizon, respectively. These vectors are initialized without considering the demand already met in the first phase, and will be later updated taking into account this information.

The quantities made available by suppliers in the first and last periods are specified in lines 5 to 8 for each product family. Since company-owned warehouses do not hold stock at the beginning of the planning horizon, any quantity stored at the end of the first period must be provided by the suppliers (see line 6). Thereafter (i.e., for $t = 2, \ldots, |T| - 1$), we decide when and what fraction of a warehouse's inventory is carried over from one period to the next. A

reasonable approach to managing inventories is to assume that when the stock level of product p in warehouse i at the end of period t is larger than the stock level in the preceding period, this results from having transferred the entire stock from $t - 1$ to t . For illustration purposes, suppose that $Inv_{ip}^{t-1} = 40$ and $Inv_{ip}^{t} = 60.$ We assume that all 40 units are carried over to t and the remaining 20 units are provided by suppliers. Hence, Inv_{ip}^{t-1} cannot be used to meet demand, which is indicated by dropping it to zero. Lines 14–17 deal with this case. In the opposite situation, for example, $Inv_{ip}^{t-1} = 100$ and $Inv_{ip}^{t} = 70$, we assume that 70 units are transferred from $t - 1$ to t , and only 30 units can be used to satisfy demand in period t (see line 20).

In Procedure UpdateSupplyAndInventory, the quantities initially recorded in the vectors TS and Inv have to be reduced due to the customer allocation decisions made during the first phase of the matheuristic. After calculating the total demand for product family p that was already allocated to warehouse i in period t (line 5), it is decided from which source (inventory, supply, or both) it will be satisfied (lines 6–13). It is natural to consider that the quantity delivered by the suppliers is only used when the stock on hand is insufficient to cover the demand.

4.3 Further strategies for variable fixing

After having estimated the remaining supply and inventory levels in each time period, we attempt to meet the demand of customer zones not yet allocated. Procedure AssignMoreCustomersTo CompanyWarehouses describes the steps underlying this process for the company-owned warehouses. For each warehouse $i \in I^e$ and period $t \in T$, we determine the total capacity used

until the end of the planning horizon (line 4) that results from the customer assignments fixed in the first phase and the inventory built up (i.e., using the information from the last LP relaxation solved). If this quantity is zero, we assume that the warehouse is not operating in period t , since we choose not to make any additional customer assignments to this facility. In the opposite case, the warehouse must be open throughout the entire planning horizon. Note that even if in one or several intermediate periods the warehouse does not serve any demand or hold stock, it must remain open due to constraints (2) that prevent the warehouse from closing and reopening. The residual warehouse capacity is calculated in line 7 and used in Procedure AssignCustomers that will be detailed later. Furthermore, a positive capacity utilization rate prevents the warehouse activity from being discontinued before period t . Therefore, the associated y variables are set to zero (line 11) unless this has already occurred in the first phase.

Regarding the potential locations $i \in I^n$, Procedure IdentifyModularUnits starts by finding the total number of periods during which a warehouse is leased and the number of modular units needed in each period. Recall that some customer zones may have already

Algorithm IdentifyModularUnits: For each new warehouse identify the total number of time periods during which the warehouse is leased and the total number of modular units in use

```
Input : \overline{u}, x
   Output: nTotalPeriods, nTotalModUnits, nModUnits: vectors with total number of
              periods and modular units in leased warehouses
 1 nT otal Periods<sub>i</sub> := 0 and nT otal ModUnits<sub>i</sub> := 0 for all i \in I<sup>n</sup>2 nModUnits_i^t := 0 for all i \in I^n, t \in T3 for i \in I^n do
 4 for t \in T do
 5 // identify the number of modules required to hold inventory and serve
                demands assigned to warehouse i in period t due to fixing variables x6 nModUnits_i^t :=\sqrt{ }

                                        \sumj\in J, p\in P: x_{ijp}^t = 1\beta_p d_{jp}^t + \sum\sum_{p\in P}\beta_p\,\overline{u}_{ip}^tM_i1

 7 \mid end\text{ } s \quad \text{ } nTotalMod Units_i := \sumt \in TnModUnits_i^t9 \int nTotalPeriods_i := \text{sum of all periods } t \in T \text{ for which } nModUnits_i^t > 010 end
11 return nTotal Periods, nTotalMod Units, nMod Units
```
been assigned to this type of facility in the first phase (see line 11 of Algorithm 1). This information is then used in Procedure AssignMoreCustomersToNewWarehouses to decide on further customer allocations. Since the fixed costs of leased warehouses reflect economies of scale, we rank these facilities, giving preference to those that have a higher mean number of modular units per period (line 1). Next, we examine each of the facilities in this ordered list. Suppose, for example, that according to the decisions made in the first phase, a certain warehouse is leased in periods 2, 3 and 5 with 4, 1 and 3 modular units, respectively. In period 4, the warehouse is not used. Due to economies of scale, it will certainly be more advantageous to have a lease agreement that runs continuously from period 2 to period 5. Furthermore, since the cost per unit of capacity decreases as the number of modular units grows, we can increase the current capacity level, thereby enhancing the opportunity to meet the demand from additional customer zones. In our example, the warehouse is leased with an average of 3 modules per period $([4+1+3)/3]$. We compare this mean value to the actual number of modules in each period, and select the largest one. Thus, we assume that the warehouse is running on 4 modules in period 2 and on 3 modules in each of periods 3, 4 and 5. Line 6 describes this step.

After having decided the number of modular units the warehouse has in period t , its residual

Algorithm AssignMoreCustomersToNewWarehouses: Serve further customer demands from leased warehouses over the planning horizon $\begin{aligned} \text{Input} \quad & : \overline{\bm{u}}, \ \overline{\bm{x}}, \overline{\bm{z}}, \overline{X_f}, \overline{X_{nf}}, \overline{Z_f}, \overline{Z_{nf}}, \textit{TS}, \textit{Inv}, \textit{nTotalPeriods}, \textit{nTotalModUnits}, \end{aligned}$ nModUnits **Output:** Additional fixing of variables x, z; updated sets X_f , X_{nf} , Z_f , Z_{nf} ; updated vectors TS and Inv due to demand satisfaction 1 Create list I with all the warehouses $i \in I^n$ that are leased (i.e. $nTotalMod Units_i > 0$); sort these facilities by non-increasing values of $nTotalMod Units_i/nTotalPeriods_i$, i.e., by mean number of modular units in use per period ² repeat 3 Extract the first warehouse from the sorted list \mathcal{I} , say i' 4 for $t \in T$ do $\begin{array}{c|c|c|c|c} 5 & / \end{array}$ // consider the largest number of modular units in period t $\begin{aligned} \mathfrak{s} \end{aligned} \quad \quad \begin{aligned} \textit{nModUnits}_{\textit{i}^{\textit{t}}}^{t} := \max\left\{ \textit{nModUnits}_{\textit{i}^{\textit{t}}}^{t}, \right. \end{aligned}$ $\int nTotalMod Units_{i'}$ $nTotal Periods_{i'}$ ן ך τ $\begin{array}{|c|c|c|c|c|}\hline \end{array}$ // determine residual capacity of warehouse \imath' in period t $\mathbf{R} = nModUnits^t_{i'} \times M_{i'} - \sum_{\mathbf{R} \in \mathcal{R}}$ j∈J, p∈P: $x_{i'jp}^t=1$ $\beta_p d_{jp}^t - \sum_{\sigma}$ $\sum_{p \in P} \beta_p \overline{u}_{i'p}^t$ $\begin{array}{ll} \texttt{9} & \end{array} \begin{array}{ll} \end{array} \begin{array}{ll} \texttt{Assigma}(\textit{u}',t,\textit{RQ},\textit{\textbf{x}},\textit{X}_f,\textit{X}_\textit{nf},\textit{TS},\textit{Inv}) \end{array}$ 10 // identify the minimum number of modular units required to meet the demand of customers assigned to warehouse \imath' in period t due to variable fixing ¹¹ ∆ := $\sqrt{ }$ $\Big\}$ $\overline{1}$ The company of the company of the \sum j∈J, p∈P: $x_{i'jp}^t=1$ $\beta_p d_{jp}^t$ $M_{\iota'}$ 1 $\begin{matrix} \end{matrix}$ $\overline{1}$ ¹² // warehouse ı ′ cannot be leased with less than ∆ modules in period t 13 for $k := 1$ to $\Delta - 1$ do $\mathbf{14}$ for $\tau := 1$ to t do $\begin{array}{|c|c|c|c|}\n\hline\n & & \text{for $\tau' := t$ to nT do}\n\end{array}$ 16 if $z_{i'k}^{\tau,\tau'} \in Z_{nf}$ then fix $z_{i'k}^{\tau,\tau'} := 0$ and move this variable from Z_{nf} to Z_f 17 \parallel \parallel \parallel end 18 | | | end 19 end 20 Add the following constraint to the LP relaxation of residual problem ensuring that warehouse i' is leased in period t with at least Δ modular units: $\sum_{i=1}^{n_i}$ $k=\Delta$ $\sum_{i=1}^{t}$ $\tau = 1$ $\frac{n}{\sum}$ τ ^{τ} $=t$ $z_{i'k}^{\tau,\tau'} \geq 1$ ²¹ end 22 until $\mathcal{I} = \emptyset$ 23 return $x, z, X_f, X_{nf}, Z_f, Z_{nf}, TS, Inv$

capacity is determined (line 8) and Procedure AssignCustomers is invoked with this information. We emphasize that the associated storage capacity is not final, and it can be changed at a later stage of the matheuristic (recall the cycle in lines 7–25 in Algorithm 1). Next, steps similar to those of Procedure AssignCustomersToNewWarehouses are performed with respect to fixing the values of z variables and strengthening the LP relaxation bound of the resulting residual problem (recall Section 4.1).

Algorithm AssignCustomers: Assignment of additional customer zones to a given warehouse i^* in time period t **Input** : i^* , t : selected warehouse and period; RQ: residual capacity of warehouse i^* in period t ; $x, X_f, X_{nf}, \textbf{TS}, \textbf{Inv}$ **Output:** Additional fixing of variables x; updated sets X_f , X_{nf} ; updated vectors TS and Inv due to demand satisfaction 1 while $RQ > 0$ and $X_{nf} \neq \emptyset$ do
2 | // identify unassigned // identify unassigned customer zones and product families in period t for which there is sufficient capacity and supply to serve their demands by warehouse i^* in that period 3 Create set A with pairs (j, p) such that $x_{i^*jp}^t \in X_{nf}$, $\beta_p d_{jp}^t \leq RQ$ and $d_{jp}^t \leq TS_p^t + Inv_{i^*p}^{t-1}$ $\begin{array}{c|c} 4 & // \end{array}$ identify the pair with lowest unit distribution cost from warehouse \imath^* 5 $(j^*, p^*) := \arg \min_{(j,p)\in \mathcal{A}} \{DC_{i^*jp}^t\}$ $\begin{array}{rcl} \mathbf{6} & \quad \quad \text{if} \,\, d_{j^*p^*}^t \leq Inv_{i^*p^*}^{t-1} \,\, \text{then} \end{array}$ τ $\begin{array}{|c|c|c|c|}\hline & {\quad\quad} / {\quad\quad} \text{ demand of (j^*,p^*) is fully served from stock on hand in warehouse i^* at j^*} \hline \end{array}$ the beginning of period t **8** Fix $x_{i^*j^*p^*}^t := 1$ and $x_{i'j^*p^*}^t := 0$ for all $i' ∈ I \setminus \{i^*\}$ 9 Move all fixed variables from X_{nf} to X_f 10 | | // update residual capacity and inventory level of the warehouse 11 $RQ = RQ - \beta_{p^*} d_{j^*p^*}^t$ $\begin{array}{|c|c|c|} \hline \text{1}} & \text{1} &$ 13 else 14 | | // demand is partly served by stock on hand and supply since $d_{j^*p^*}^t \leq TS_{p^*}^t + Inv_{i^*p^*}^{t-1}$ 15 Fix $x_{i^*j^*p^*}^* := 1$ and $x_{i'j^*p^*}^* := 0$ for all $i' \in I \setminus \{i^*\}$ 16 Move all fixed variables from X_{nf} to X_f 17 | // update residual capacity, supply and inventory level of warehouse 18 $RQ = RQ - \beta_{p^*} d_{j^*p^*}^t$ 19 $TS_{p^*}^t := TS_{p^*}^t - \left(d_{j^*p^*}^t - Inv_{i^*p^*}^{t-1}\right)$ 20 $Inv_{i^*p^*}^{t-1} := 0$ ²¹ end ²² end 23 return x, X_f, X_{nf}, TS, Inv

Finally, Procedure AssignCustomers governs the allocation of unsatisfied demand to a given warehouse $\imath^*\in I$ with available capacity in period $t.$ Among all customer zones j and product families p eligible to be served by the warehouse in that period (line 3), the pair (j, p) with the lowest unit distribution cost from facility i^* is identified (line 5). Observe that to achieve eligibility, it is not enough that the demand associated with this pair is not greater than the residual capacity in the warehouse. In addition, this demand must also not exceed the available supply in period t plus the inventory held at the end of period $t - 1$ in the warehouse. If the demand of the selected customer zone is not more than the available stock, the latter is used to fully serve this demand. As a consequence, the inventory level and the residual warehouse capacity are adjusted accordingly (lines $11-12$). Otherwise, the demand is satisfied jointly by the amount of supply and stock available. In this case, the supply quantity and the residual capacity are decreased and the inventory level drops to zero (lines 18–20). Moreover, a successful demand allocation results in fixing all the variables x related to this customer zone, product family, warehouse, and period, as stated in lines 8 and 15.

5 Computational study

In this section, we evaluate the computational efficiency of the proposed matheuristic and the quality of the solutions obtained for a set of randomly generated problem instances. In addition, we compare the heuristic solutions against the solutions identified by CPLEX within a given time limit. In Section 5.1, we describe the settings used to generate the problem instances. The numerical results are presented in Section 5.2. Finally, in Section 5.3, relevant insights into the features of the heuristic solutions are discussed.

5.1 Problem instances

For the current study, we generated a total of 160 instances using the parameters given in Table 1. Assuming that a time period represents one month, the values of $|T|$ shown in this table refer to timeframes of 1, 2, 3, and 4 years. We emphasize that the length of the planning

Description	Parameter	Value(s)
No. of periods		12, 24, 36, 48
No. of suppliers	S	3
No. of warehouses		10, 20
No. of company-owned / potential warehouses	$ I^e \; / \; I^n $	$5/5$, $10/10$
No. of customer zones	\boldsymbol{J}	2 I , 5 I , 10 I , 20 I
No. of product families	Р	3
Max. no. of modular units in a leased warehouse	n_i $(i \in I^n)$	5
Unit capacity consumption factor	β_n $(p \in P)$	

Table 1: Parameter settings.

horizon in our instances is significantly longer than what is often reported in the literature dedicated to multi-period facility location problems (see e.g., Becker et al., 2019; Correia and Melo, 2017; Cortinhal et al., 2015; Jena et al., 2015a, 2017; Sauvey et al., 2020), thus greatly impacting the size of the instances in our testbed.

For each combination of the parameter values in Table 1, five instances were randomly generated. Observe that the larger instances have 48 time periods, 10 company-owned warehouses, 10 potential locations for leasing storage capacity, and 400 customer zones, resulting in formulation (M) having over 1.2 million binary variables, as shown in Table 2. The customer assignment variables x account for 95% of this number. The table also gives the total number of continuous variables and the total number of constraints. It can be seen that our computational study includes medium- and large-sized problem instances.

T			$# \n binary variables$		$\#$ continuous	$#$ constraints	
		\boldsymbol{x}	\boldsymbol{y}	\boldsymbol{z}	variables		
12	min	7200	60	1950	1440	1458	
	avg	83250	90	2925	2160	6048	
	max	288000	120	3900	2880	15768	
24	min	14400	120	7500	2880	2886	
	avg	166500	180	11250	4320	12051	
	max	576000	240	15000	5760	31476	
36	min	21600	180	16650	4320	4314	
	avg	249750	270	24975	6480	18054	
	max	864000	360	33300	8640	47184	
48	min	28800	240	29400	5760	5742	
	avg	333000	360	44100	8640	24057	
	max	1152000	480	58800	11520	62892	
All	avg	208125	225	20813	5400	15053	

Table 2: Size of problem instances.

In each instance, three product families with distinct demand and supply patterns are considered, two of which exhibiting seasonality profiles. Product family 1 undergoes irregular demand variations over the planning horizon that range from -5% to $+5%$ between two consecutive periods. By contrast, product family 2 is subject to advertising campaigns (e.g., Black Friday, Cyber Monday, Christmas promotions), which increase its demand in the last three periods of each 12-period block. For example, for $|T| = 24$, demand peaks occur in periods 10, 11, 12, 22, 23, and 24. Many products in the consumer electronics industry exhibit this type of pattern. As for product family 3, its demand faces significant growth in the middle of each set of 12 consecutive periods. This pattern represents products with higher sales in the summer season (e.g., air coolers and air conditioners). For instance, in a 3-year planning horizon ($|T| = 36$), peak demand occurs in periods 6, 7, 8, 18, 19, 20, 30, 31, and 32. Detailed information on the random generation of the three demand profiles is presented in the appendix.

The suppliers' capacities are also generated randomly, and are associated with the individual demand profiles of the product families. Accordingly, for family 1, the capacity of each supplier is 25 to 50% higher than the average demand in each time period. For families 2 and 3, the supplier capacity increases in the three periods prior to the start of each peak demand season. This scheme reflects common practices for seasonal commodities, whereby production occurs ahead of time to respond to the projected growth in demand. The appendix details how the suppliers' capacities are generated for each family. Note that the occurrence of significant fluctuations in demand in our problem instances induces variations in storage capacity over time, thus triggering the need to increase and decrease the number of modular units leased in new warehouses. In addition, the mismatch between supply and demand may also prompt the need to hold inventory at some facilities in individual periods so that demand can be met in later periods.

Additional parameters (i.e., capacities of the company-owned warehouses, capacity of a modular unit, and cost parameters) are also described in the appendix. We highlight that the generation of the fixed costs for warehouse leasing $(L^{t,t'}_{ik})$ accounts for economies of scale that favor leasing a facility with a larger number of modular units for a longer rental term. Economies of scale are also present in the fixed costs of operating company-owned warehouses (OC_i^t) .

5.2 Numerical results

Formulation (M) was coded in C^{++} and embedded in IBM ILOG Concert Technology with IBM ILOG CPLEX 20.1. A limit of 5 hours of CPU time was set for each solver run. The matheuristic was implemented in C^{++} , and CPLEX was also employed to solve the LP relaxations of the various residual problems as well as the last residual MILP problem (recall lines 9 and 26 of Algorithm 1). For solving the latter problem, a time limit of 20 minutes was imposed. Moreover, CPLEX was always used with default settings under a deterministic parallel mode. All experiments were performed on a dual AMD EPYC[™] 7702 workstation, with each processor having 64 cores, 256 MB cache, 2 to 3.35 GHz, and 512 GB/3200 RAM.

Table 3 summarizes the quality of the solutions returned by CPLEX according to the length of the planning horizon in the problem instances (column 1). Column 2 indicates the number of instances for which CPLEX found a feasible solution ($#$ inst. solved) and the number of instances for which CPLEX could not identify a single feasible solution within the specified time limit $(\#$ inst. no sol. found). We remark that our data generation scheme ensures that all

T	$\#$ inst. solved [*] / $\#$ inst. no sol. found		MIP gap $(\%)$	UB gap $(\%)$
12	40/0	min	0.68	1.96
		avg	4.87	6.29
		max	26.43	36.19
24	40/0	min	1.93	3.03
		avg	5.83	6.90
		max	26.66	36.55
36	40/0	min	2.82	3.21
		avg	9.15	10.97
		max	33.62	50.84
48	39/1	min	3.72	3.96
		avg	10.07	11.90
		max	20.66	26.34
All	159/1	avg	7.46	9.00

Table 3: Quality of the solutions identified by CPLEX within a 5 h time limit. (*) no instance was solved to guaranteed optimality.

instances have feasible solutions. The optimality gap as reported by CPLEX upon termination is given in column 4 (MIP gap). This gap is determined by $(z^{UB} - z^{LB})/z^{UB} \times 100$, with z^{UB} denoting the objective value of the best feasible solution returned by CPLEX for an individual instance, and z^{LB} representing the best lower bound identified by CPLEX for that instance. The 'UB gap' in column 5 measures the quality of z^{UB} with respect to the linear relaxation bound, i.e., $(z^{UB} - z^{LP}) / z^{LP} \times 100$, where z^{LP} is the LP bound. Table 3 reports the minimum, average, and maximum values of the performance measures MIP gap and UB gap. The last row (All) of this table provides information over all problem instances.

Although CPLEX identifies feasible solutions for all but one problem instance within the 5-hour time limit, it could not prove the optimality of any of them. This suggests that we are facing a challenging problem, even for medium-sized instances with planning horizons with 12 periods. This feature is also confirmed by the optimality gaps reported by CPLEX. A great deal of spread around the average MIP gap of 7.46% is observed, regardless of the length of the planning horizon. As expected, the quality of the solutions deteriorates as the planning horizon increases. While only 3 instances exhibit an optimality gap greater than 10% when $|T| = 12$, this number increases to 17 for $|T| = 48$. A few instances even have rather large deviations up to about 34%. Since the linear relaxation provides a very good lower bound (as will be shown in Table 6), the inferior quality of many solutions is also reflected in the 'UB gap', which can be as high as 51%. In short, an off-the-shelf optimization solver such as CPLEX is not a suitable choice for obtaining optimal or near-optimal solutions to this challenging problem in a reasonable amount of time.

In contrast to CPLEX, the matheuristic identifies a feasible solution to every tested instance and for all values of the capacity threshold α selected. To evaluate the quality of the heuristic solutions, a comparison was carried out with the best solutions returned by CPLEX, pertaining to 159 instances. Table 4 presents the results obtained for different performance measures. For each value of $|T|$, columns 2–5 indicate the number of heuristic solutions with better (# superior) and worse (# inferior) quality compared to CPLEX for $\alpha \in \{0.6, 0.7, 0.8, 0.9\}$. Given a problem instance, let $z^{H(\alpha)}$ denote the objective function value of the heuristic solution obtained for a particular choice of the parameter α , and let z^{UB} be the best objective value achieved by CPLEX for that instance. For those heuristic solutions with superior quality compared to CPLEX (i.e., $z^{H(\alpha)} < z$), the associated improvement is calculated as follows: $(z^{UB} - z^{H(\alpha)})/z^{UB} \times 100$. Conversely, for those heuristic solutions with lower quality, their performance is measured by $(z^{H(\alpha)}-z^{UB})/z^{UB} \times 100$. For each value of the capacity threshold, columns 7–10 show the minimum, average, and maximum performance deviations, with the best values highlighted in boldface. The last row of the table summarizes the results obtained for the 159 instances.

Table 4: Performance of the matheuristic compared to CPLEX (results reported for 159 instances).

In general, increasing the capacity threshold α favors obtaining more solutions by the matheuristic with higher quality than those found by CPLEX (e.g., 59.7% for $\alpha = 0.6$ against 68.6% for $\alpha = 0.9$). This feature is explained by the fact that when a relatively low capacity utilization rate is taken at a warehouse (e.g., $\alpha = 0.5$), this translates into considering more warehouses as being open. As a result, a larger number of binary variables x, y , and z are fixed, thus yielding in turn a residual MILP problem with smaller size. In this restricted MILP problem, which is then solved with CPLEX, the network configuration is already largely defined. The opposite effect is observed when the capacity threshold is increased, for example, to 0.9. In this case, fewer warehouses meet the minimum capacity utilization level and, consequently, the size of the last residual problem is larger since fewer binary variables were fixed. This means that there is still some leeway for deciding on the final network configuration, thus enabling a feasible solution with higher quality to be obtained. However, this may be offset by the fact that additional computing time is required to solve this larger residual problem to optimality, and the 20-minute time limit that we impose may be insufficient to achieve this goal. Figure 3 substantiates these observations by displaying the average percentage of binary variables x, y , and z that are fixed by the matheuristic. Furthermore, this feature is also reflected in the number of iterations performed in the first phase of the matheuristic (recall lines 8–12 in Algorithm 1) that range, on average, from 7 ($\alpha = 0.6$) to 12.7 ($\alpha = 0.9$). This is also observed for the average number of iterations carried out in the second phase (recall lines 7–25 in Algorithm 1), that vary from 2.7 ($\alpha = 0.6$) to 3.7 iterations ($\alpha = 0.9$).

Figure 3: Average percentage of binary variables fixed by the matheuristic.

According to Table 4, the performance achieved by our matheuristic competes very favorably with CPLEX regardless of the value selected for α . Among the heuristic solutions with higher quality than the CPLEX solutions, the average improvement ranges from 6.22% to 6.92%. For

some instances, the matheuristic even finds substantially superior solutions, whatever the length of the planning horizon (and thus the problem size). The latter yield a total cost reduction of up to 32% compared to CPLEX (see $|T| = 36$). On the other hand, when the matheuristic returns more expensive solutions than the solutions obtained by CPLEX, the deterioration in quality is less than 5%, with the exception of ten instances (over all values of α). Although there is no warehouse capacity threshold that consistently performs the best, in practice this is not a drawback since computing time is not a critical issue in this case as shown by Table 5 (columns 7–10), even for the largest problem instances with 48 time periods. Thus, a decision maker could re-run the matheuristic for different values of the parameter α before deciding which configuration of the logistics network he/she would like to retain. In addition, when reoptimization is required to perform 'what-if' analyzes and a problem has to be solved repeatedly with different data sets, the reduced computational burden required by the matheuristic makes it possible to handle very large instances quite successfully.

T	# residual MILP problems solved optimally/not optimally within time limit					CPU (sec.)			
	$\alpha = 0.6$	$\alpha = 0.7$	$\alpha = 0.8$	$\alpha = 0.9$		$\alpha = 0.6$	$\alpha = 0.7$	$\alpha = 0.8$	$\alpha = 0.9$
12	40/0	39/1	38/2	36/4	min avg max	3.6 48.5 479.9	4.0 77.8 1283.8	5.7 142.5 1500.1	6.9 315.7 1597.0
24	40/0	40/0	38/2	29/11	min avg max	11.1 108.2 345.8	16.5 180.6 1554.8	15.7 339.6 2083.5	30.9 755.9 2112.5
36	40/0	40/0	38/2	22/18	min avg max	25.9 200.5 624.0	21.1 280.1 852.8	23.7 496.9 2025.3	107.4 1164.4 3537.5
48	40/0	38/2	34/6	24/16	min avg max	34.8 368.6 1294.9	39.8 501.5 2050.9	52.1 890.6 2920.0	117.4 1577.4 5224.1
All	160/0	157/3	148/12	111/49	avg	181.4	260.0	467.4	953.3

Table 5: CPU time performance of the matheuristic.

For each length of the planning horizon, Table 5 also presents the number of instances for which the corresponding residual MILP problem could be solved either to optimality or approximately within the 20-minute time limit (columns 2–5). The impact of the selected warehouse capacity threshold is in line with the analysis of the results in Table 4 and Figure 3. Clearly, an increment in the value of α reduces the number of binary variables that can be fixed by the matheuristic, and as a result, the size of the restricted MILP problem increases. This feature is particularly noticeable for $\alpha = 0.9$, where 30.6% (49/160) of the instances could not be solved to proven optimality within 20 minutes. However, the best feasible solution found for each of these residual problems is near-optimal. More specifically, the optimality gaps as reported by CPLEX do not exceed 0.08% for the three instances occurring with $\alpha = 0.7$, and vary between 0.02% and 0.34% for $\alpha = 0.8$ (12 instances). For $\alpha = 0.9$, the optimality gap ranges from 0.03% to 0.94%, with an average of 0.3% over 49 instances. Interestingly, for 48.1% (77/160) of the problem instances, the best feasible heuristic solution is obtained for the highest capacity threshold. By contrast, only 7 instances (4.4%) run with $\alpha = 0.6$ yielded the best heuristic solutions. Moreover, considering all the values selected for the parameter α , we observe that there are 118 instances (74%) where there is at least one heuristic solution of higher quality than the one returned by CPLEX (this value also includes the instance with $|T| = 48$ for which CPLEX could not identify any feasible solution within 5 h). This means that CPLEX outperforms the matheuristic for only 42 instances (26%), half of which are among the smallest (i.e., $|T| = 12$).

Next, we analyze the quality of the lower bound provided by the linear relaxation of formulation (M) . To ensure a fair evaluation, we choose to compare the LP bound with the best feasible solution available, whether this was obtained by CPLEX or by the matheuristic. Accordingly, the following ratio is calculated for every problem instance: $(z^{UB^*}-z^{LP})/z^{UB^*}\times 100$, with z^{LP} denoting the LP bound and z^{UB^\ast} representing the objective value of the best feasible solution available for the individual instance, i.e. $z^{UB^*} = \min\{z^{UB}, \min_{\alpha \in \{0.6,0.7,0.8,0.9\}}\{z^{H(\alpha)}\}\}.$ For the single instance for which CPLEX was unable to identify a feasible solution within the 5-hour time limit, $z^{UB} = +\infty$. Table 6 gives the minimum, average, and maximum deviations measured as a percentage. We do not include in this table the computing times required to solve the linear relaxation of formulation (M) to optimality because they were negligible in view of the size of the instances: on average, only 45.1 sec. were needed, while the largest instance used 312.5 sec.

	$\left\vert T\right\vert$				All
	12	24	36	48	instances
min avg max	1.79 2.88 5.07	1.80 3.26 7.02	1.72 3.41 7.60	1.59 3.40 5.28	1.59 3.24 7.60

Table 6: Comparison of the lower bound of the linear relaxation with the objective value of the best feasible solution available $(\%)$.

Formulation (M) consistently produces quite good LP bounds for all instances. This feature is very useful, as it allows the quality of the feasible solutions identified by the matheuristic to be evaluated, including the instance with $|T| = 48$ that CPLEX could not solve within the time limit. In this case, the performance of the matheuristic can only be measured by comparison to the LP bound of that instance. Table 7 presents the minimum, average, and maximum gaps between the objective value of the heuristic solution for a given capacity threshold $(z^{H(\alpha)}).$ and the LP bound (z^{LP}) , i.e., $(z^{H(\alpha)} - z^{LP})/z^{LP} \times 100$. The best average values are shown in boldface. The results report to all 160 instances. The average deviations presented in this table reinforce the high quality performance of the matheuristic that had already been observed through other metrics, especially when the fixing of the binary variables x, y , and z is associated with a minimum warehouse capacity utilization rate α closer to 1. Gaps of more than 10% were obtained for a reduced number of instances, more precisely, 7 instances with $\alpha = 0.6, 2$ instances with $\alpha = 0.7$, 4 instances with $\alpha = 0.8$, and 6 instances with $\alpha = 0.9$.

T		Deviation of heuristic solution to LP bound $(\%)$				
		$\alpha = 0.6$	$\alpha = 0.7$	$\alpha = 0.8$	$\alpha = 0.9$	
12	min	2.04	1.92	1.86	1.82	
	avg	4.49	3.82	3.79	3.72	
	max	8.38	7.28	8.30	11.26	
24	min	2.11	2.09	1.85	1.83	
	avg	4.90	4.36	4.21	4.43	
	max	10.46	10.46	12.78	11.20	
36	min	2.31	1.98	1.80	1.75	
	avg	4.98	4.44	4.32	4.57	
	max	14.28	10.59	11.21	13.33	
48	min	1.98	1.85	1.76	1.62	
	avg	5.19	4.35	4.48	4.99	
	max	13.37	9.97	11.74	14.45	
All	avg	4.89	4.24	4.20	4.43	

Table 7: Comparison of the objective value of the solutions identified by the matheuristic with the LP bound.

In summary, our numerical results indicate that the proposed matheuristic consistently provides good to very good feasible solutions in significantly shorter computing time than CPLEX.

5.3 Additional insights

To assist decision makers in understanding how warehouse sizing decisions are affected by the flexible settings provided by our model, we have selected a representative problem instance with a 24-period planning horizon, 400 customer zones, and 20 warehouses, half of which are owned by the company and the remaining ones (numbered 11 through 20) can be leased on a temporary basis. In total, this instance has nearly 592,000 binary variables (of which 97.4% are customer-assignment variables) and 5,760 continuous variables. Taking $\alpha = 0.9$, the matheuristic identifies a feasible solution with a total cost that is 25.4% lower than the total cost of the best solution returned by CPLEX. Moreover, the heuristic solution deviates only 1.83% from the LP bound, which testifies to the very good quality of this solution. Of the 10 existing warehouses, 6 are closed at the beginning of the planning horizon, one is closed at the start of period 6, and the remaining 3 warehouses are retained. Figures 4 (a)–(c) show

Figure 4: Number of modular units leased in an instance with 24 periods, 10 potential warehouse locations, and 400 customer zones.

the capacity sizing decisions at the 10 selected candidate sites, while Figure 4 (d) displays the total number of modular units that are deployed in the network in every period of the planning horizon.

Due to peak demand particularly in periods 10–12 and 22–24 driven by seasonality, the total capacity leased in new warehouses reaches a high value in these periods as well as in the immediately preceding periods (i.e., $t = 9, 21$). As expected, the growth in capacity is not sudden but gradual. This is clearly noticeable in periods 6–8 and later in periods 18–20, where demand for product family 3 reaches its peak (see Figure 4 (d)). Several warehouses contribute to capacity variations, owing to the leasing of a changing number of modular units. This is the case, for example, of warehouse 16 (Figure 4 (a)), where capacity expansion occurs from period 11 (3 modules) to period 12 (4 modules), followed by a capacity reduction in period 13 (2 modules). Warehouse 11 also undergoes a gradual capacity contraction, but in periods 23 and 24. The acquisition of capacity for short periods of time, a feature of our problem, is observed in warehouses 15 and 19 (Figure 4 (b)). On the other hand, warehouses 12, 13, 14, 17, and 18 (Figure 4 (c)) are leased with as many modular units as possible and do not undergo any capacity change over their lease terms.

Table 8 reports further characteristics of warehouse-related decisions in the best solutions identified by the matheuristic. For both types of warehouses, this table shows the minimum, average and maximum number of sites operated (columns 3, 4 and 6). The advantages of temporary access to variable capacity leasing are reflected in a significantly high number of contracts signed (column 7) combined with a relatively large number of company-owned warehouses closed (column 4). From the small number of operating periods of the latter warehouses (column 5), we realize that most of them are discontinued early in the planning horizon, which is in line with the example presented in Figure 4. This is due to the fact that it is not possible to change their capacities to match demand fluctuations, unlike new facilities. In addition, the wide range of lease terms in new warehouses (column 8) is also evidence that many oscillations in the capacity sizing of these facilities can occur, prompted by variations in demand. Finally, the storage capacity utilization rate per period, reported in column 9, reveals a high usage level of the open facilities. To some extent, the available spare capacity will allow to handle situations where future demand is higher than the estimated quantity, without incurring additional costs for leasing more warehouses.

Table 8: Characteristics of warehouse decisions in the best heuristic solutions.

6 Conclusions

We have introduced, modeled, and solved a multi-period logistics network redesign problem involving warehouse location, capacity sizing, distribution, and inventory holding decisions in a multi-product two-echelon network. In contrast to classical facility location problems, flexible conditions are in place regarding the amount of storage space that can be leased in new warehouses and the timeframe of each lease contract. This setting stems from warehousing-asa-service, which allows storage capacity to be scaled over the planning horizon (i.e., capacity can be expanded or reduced, and even discontinued for multiple periods at a given location). In addition, customer single-assignment constraints have also been considered which greatly affect the size of the proposed MILP formulation, especially when the planning horizon is extensive and the number of customer zones is large, as is usually the case in practice.

We have developed the first heuristic for this new problem which exploits the structure of the optimal solution to the LP relaxation. Thus, when the capacity utilization rate of the operating warehouses in the LP solution reaches a given threshold, the customer zones that are fully allocated to them have their variables set to one in the original MILP problem. This strategy also drives the fixing of several other binary variables. Each time a subset of binary variables is fixed, the LP relaxation of the associated residual problem is solved. This procedure is repeated until no more variables can be fixed. When that happens, the second

phase of the matheuristic is started. To this end, additional variable fixing rules are applied together with a scheme for managing inventories at the warehouses and using the product amounts made available by the suppliers. Numerical experiments with randomly generated problem instances, some of which with a very large size, reveal that the proposed matheuristic is effective both in terms of computational efficiency and solution quality. Regardless of the length of the planning horizon and the number of customer zones, the matheuristic always identifies a feasible solution to every problem instance, unlike a state-of-the-art MILP solver such as CPLEX. Moreover, it requires a significantly shorter computing time. Considering all the feasible solutions obtained with different choices for the capacity threshold, the matheuristic outperforms CPLEX in 74% of the instances, with an average improvement of 6.4%. On the other hand, when the matheuristic underperforms, the average deterioration is less than 1% compared to CPLEX. Another important finding of our study is that the MILP formulation we have developed provides a tight LP bound. This feature, together with the very good performance of the matheuristic, has a practical relevance, since it enables solving large-scale problems with various parameter combinations (e.g., different demand estimates), and thus understanding how the configuration of the logistics network and the associated total cost are affected.

A future research venue would be to integrate uncertainty into the problem, taking into account that demands, capacities of suppliers and rental warehouses as well as costs are unknown parameters at the time of planning. Naturally, this would further increase the complexity of an already challenging problem. In this case, the study carried out in this work would also be relevant for the development of a mathematical model and a specially-tailored solution procedure.

Acknowledgements

This work was partially supported by Fundação para a Ciência e a Tecnologia (Portuguese Foundation for Science and Technology) through the projects UIDB/00297/2020 ((https://doi.org/10. 54499/UIDB/00297/2020) and UIDP/00297/2020 (https://doi.org/10.54499/UIDP/00297/2020) (Center for Mathematics and Applications). This support is gratefully acknowledged.

Appendix: Data generation

Problem instances were generated using a random procedure that extends the scheme developed by Correia and Melo (2022). Let $\mathcal{U}[a, b]$ denote the generation of random numbers over the range $[a, b]$ according to a continuous uniform distribution.

Each of the three product families follows an individual demand pattern that reflects the fluctuations that many consumer products face in practice. To model the different profiles, random numbers are drawn from three uniform distributions, namely $\delta^t_j \in \mathcal{U}[0.95,\, 1.05]$, $\gamma^t_j \in$ $\mathcal{U}[1.2, 1.3]$, and $\rho_j^t \in \mathcal{U}[0.8, 0.9]$, for $t \in T$ and $j \in J$.

For product family 1, the demand of each customer zone $j \in J$ undergoes irregular fluctuations over time as follows:

$$
d_{j1}^1 = \lceil \mathcal{U}[20, 100] \rceil \qquad d_{j1}^t = \lceil \delta_j^t d_{j1}^{t-1} \rceil \qquad t = 2, ..., |T|,
$$

where $\lceil x \rceil$ denotes the smallest integer greater than or equal to x. Therefore, variations of $\pm 5\%$ in demand can occur from one period to the next in a given customer zone. In contrast, seasonal peaks take place at different time periods over the planning horizon for the other two product families.

For $|T| = 12$, the scheme defined for family 1 is also used in the first nine periods for family 2, followed by a seasonal peak in the last three periods. Under the assumption that a time period represents one month, this demand pattern is related to a product family facing a demand peak in the last quarter of the year. Accordingly, for every $j \in J$ we set:

$$
d_{j2}^{1} = \begin{bmatrix} \mathcal{U}[20, 100] \end{bmatrix}
$$

\n
$$
d_{j2}^{t} = \begin{bmatrix} \delta_{j}^{t} d_{j2}^{t-1} \\ \gamma_{j}^{t} d_{j2}^{t-1} \end{bmatrix} \qquad t = 2, ..., 9
$$

\n
$$
d_{j2}^{t} = \begin{bmatrix} \gamma_{j}^{t} d_{j2}^{t-1} \\ t = 10, 11, 12. \end{bmatrix}
$$

This demand pattern is repeated for each 12-period block. Hence, for a planning horizon with $|T| = 12 k$ periods $(k = 1, 2, 3, 4)$, demand peaks occur in periods $t = 12 \ell + 10, \ldots, 12 (\ell + 1)$ with $\ell = 0, \ldots, k - 1$.

Regarding product family 3, given $|T| = 12 k$ ($k = 1, 2, 3, 4$), demand faces a sharp increase in periods $t = 12 \ell + 6, 12 \ell + 7, 12 \ell + 8$ (i.e., in the middle of the year), and declines in the following three periods $t = 12 \ell + 9$, $12 \ell + 10$, $12 \ell + 11$, with $\ell = 0, \ldots, k - 1$. For $|T| = 12$, the following generation scheme is used for every $j \in J$:

$$
d_{j3}^{1} = \begin{bmatrix} \mathcal{U}[20, 100] \\ d_{j3}^{t} = \begin{bmatrix} \delta_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \begin{bmatrix} \gamma_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \begin{bmatrix} \gamma_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \begin{bmatrix} \rho_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \begin{bmatrix} \delta_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \begin{bmatrix} \delta_{j}^{t} d_{j3}^{t-1} \\ d_{j3}^{t} = \end{bmatrix} \end{bmatrix} & t = 12.
$$

This pattern repeats itself in every set of 12 consecutive periods when $|T| = 12 k$ and $k = 2, 3, 4$.

For generating the suppliers' capacities, random numbers $\widetilde{\gamma}^t$ drawn from $\mathcal{U}[1.25,\, 1.50]$ are used. For product family 1, the capacity of supplier $s \in S$ in period $t \in T$ is 25 to 50% larger than the average demand per period and supplier:

$$
SQ_{s1}^{t} = \left[\widetilde{\gamma}^{t} \frac{\sum\limits_{t \in T} \sum\limits_{j \in J} d_{j1}^{t}}{|T| \cdot |S|} \right].
$$

For product families facing seasonal demand variations, suppliers increase their production capacities close to the peak season. Therefore, for family 2, which has a demand peak in the last three periods of a 12-period block, the capacity of supplier $s \in S$ grows in periods 7, 8, and 9 as follows:

$$
SQ_{s2}^{t} = \begin{bmatrix} \min_{t \in T} \left\{ \sum_{j \in J} d_{j2}^{t} \right\} \\ \widetilde{\gamma}^{t} & |S| \end{bmatrix} \qquad t = 1, ..., 6 \text{ and } t = 10, 11, 12,
$$

and

$$
SQ_{s2}^{t} = \begin{bmatrix} \max_{t \in T} \left\{ \sum_{j \in J} d_{j2}^{t} \right\} \\ \widetilde{\gamma}^{t} & |S| \end{bmatrix} \qquad t = 7, 8, 9.
$$

The above scheme is repeated for all other 12-period blocks in planning horizons with 24, 36, and 48 periods.

For product family 3, the capacity of supplier $s \in S$ is generated in such a way that it increases in the three periods just before the demand peak season occurs. Hence, for $|T| = 12$ we consider:

$$
SQ_{s3}^{t} = \begin{bmatrix} \frac{\sum_{i=1}^{2} \sum_{j \in J} d_{j3}^{t}}{2|S|} \\ \frac{\sum_{i=1}^{2} \sum_{j \in J} d_{j3}^{t}}{2|S|} \end{bmatrix} \qquad t = 1, 2,
$$

$$
SQ_{s3}^{t} = \begin{bmatrix} \frac{\max}{\gamma t} \frac{\sum_{i=6}^{2} \sum_{j \in J} d_{j3}^{t}}{|S|} \\ \frac{\sum_{i=6}^{2} \sum_{j \in J} d_{j3}^{t}}{7|S|} \end{bmatrix} \qquad t = 3, 4, 5
$$

This procedure is used in each 12-period block for instances with $|T| \in \{24, 36, 48\}$.

The capacity of each company-owned warehouse takes into account the average demand per time period and facility. This value is perturbed by a random number $\widetilde{\delta}_i \in \mathcal{U}[2, 3]$.

$$
Q_i = \begin{bmatrix} \sum_{j \in J} \sum_{p \in P} \sum_{t \in T} d_{jp}^t \\ |T| \cdot |I| \end{bmatrix} \quad i \in I^e
$$

The capacity of a modular unit at a potential warehouse location is fixed in a similar way:

.

$$
M_i = \begin{bmatrix} \sum_{j \in J} \sum_{p \in P} \sum_{t \in T} d_{jp}^t \\ n_i \cdot |T| \cdot |I| \end{bmatrix} \quad i \in I^n.
$$

The fixed operating costs of company-owned warehouses are generated in such a way as to reflect economies of scale. Thus, the larger the capacity of a warehouse $i \in I^e$, the lower the associated operating cost.

$$
OC_i^1 = \mathcal{U}[0, 100] + \mathcal{U}[1800, 2000] \sqrt{Q_i} \qquad OC_i^t = \mu^t OC_i^{t-1} \qquad t = 2, ..., |T|,
$$

with $\mu^t \in \mathcal{U}[1,\,{}1.01].$ This means that the fixed cost of operating a company-owned warehouse

can increase by as much as one percent between two consecutive periods. Furthermore, the fixed cost to remove the warehouse is assumed to be half of its operating cost, i.e., $FC_i^t\,=\,0.5\,OC_i^t$ $(i \in I^e; t \in T).$

At each potential warehouse location $i \in I^n$, economies of scale are captured in the fixed lease costs, taking into account the number of modular units selected and the length of the lease term, as follows:

$$
L_{ik}^{1,1} = \mathcal{U}[0, 100] + \mathcal{U}[2200, 2300] \sqrt{k M_i} \qquad k = 1, ..., n_i,
$$

\n
$$
L_{ik}^{t,t} = \mu^t L_{ik}^{t-1,t-1}
$$

\n
$$
L_{ik}^{t,t'} = L_{ik}^{t,t} + 0.8 \sum_{m=t+1}^{t'} L_{ik}^{m,m}
$$

\n
$$
k = 1, ..., n_i, t = 2, ..., |T|,
$$

\n
$$
k = 1, ..., n_i, t = 2, ..., |T|,
$$

with $\mu^t \in \mathcal{U}[1,\, 1.01].$ Clearly, the cost incurred by a lease agreement for $t'-t+1$ periods is lower than the sum of the costs for one-period leases, i.e., $L^{t,t'}_{ik} <$ $\sum_{i=1}^{t}$ $m=t$ $L^{m,m}_{ik}$, for a fixed number of modular units, k .

The unit distribution costs from supplier $s \in S$ to warehouse $i \in I$ and from the latter to customer zone $j \in J$ for product family $p \in P$ in time period $t \in T$ are generated in such a way that they increase at a rate ranging from 1 to 3% per period according to the following scheme:

$$
SC_{sip}^1 = U[15, 20] \t DC_{ijp}^1 = U[25, 30] \nSC_{sip}^t = \xi^t SC_{sip}^{t-1} \t DC_{ijp}^t = \xi^t DC_{ijp}^{t-1} \t t = 2, ..., |T|,
$$

with $\xi^t \in \mathcal{U}[1.01, \, 1.03].$ We also assume that shipments from suppliers to warehouses are less expensive than shipments from warehouses to customer zones per unit delivered, as the former are associated with large quantities compared to the latter, as is typically the case in practice.

Finally, the unit inventory holding cost for product family $p \in P$ in warehouse $i \in I$ at time period $t \in T$ is generated as follows:

$$
IC_{ip}^1 = \mathcal{U}[1, 2] \qquad \qquad IC_{ip}^t = \mu^t IC_i^{t-1} \qquad t = 2, ..., |T|,
$$

with $\mu^t \,=\, \mathcal{U}[1,\, 1.01].$ Therefore, inventory holding costs are monotonic increasing, with a growth rate not higher than 1% per period.

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ISSN 2193-7761